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Simulation Supported Decision Making

Allen, Gene

Monterey, California: Naval Postgraduate School

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**SI4000 Summer 2010
Systems Engineering Colloquium
Naval Postgraduate School
15 July 2010**

Simulation Supported Decision Making

**Gene Allen
Naval Surface Warfare Center Carderock Division**

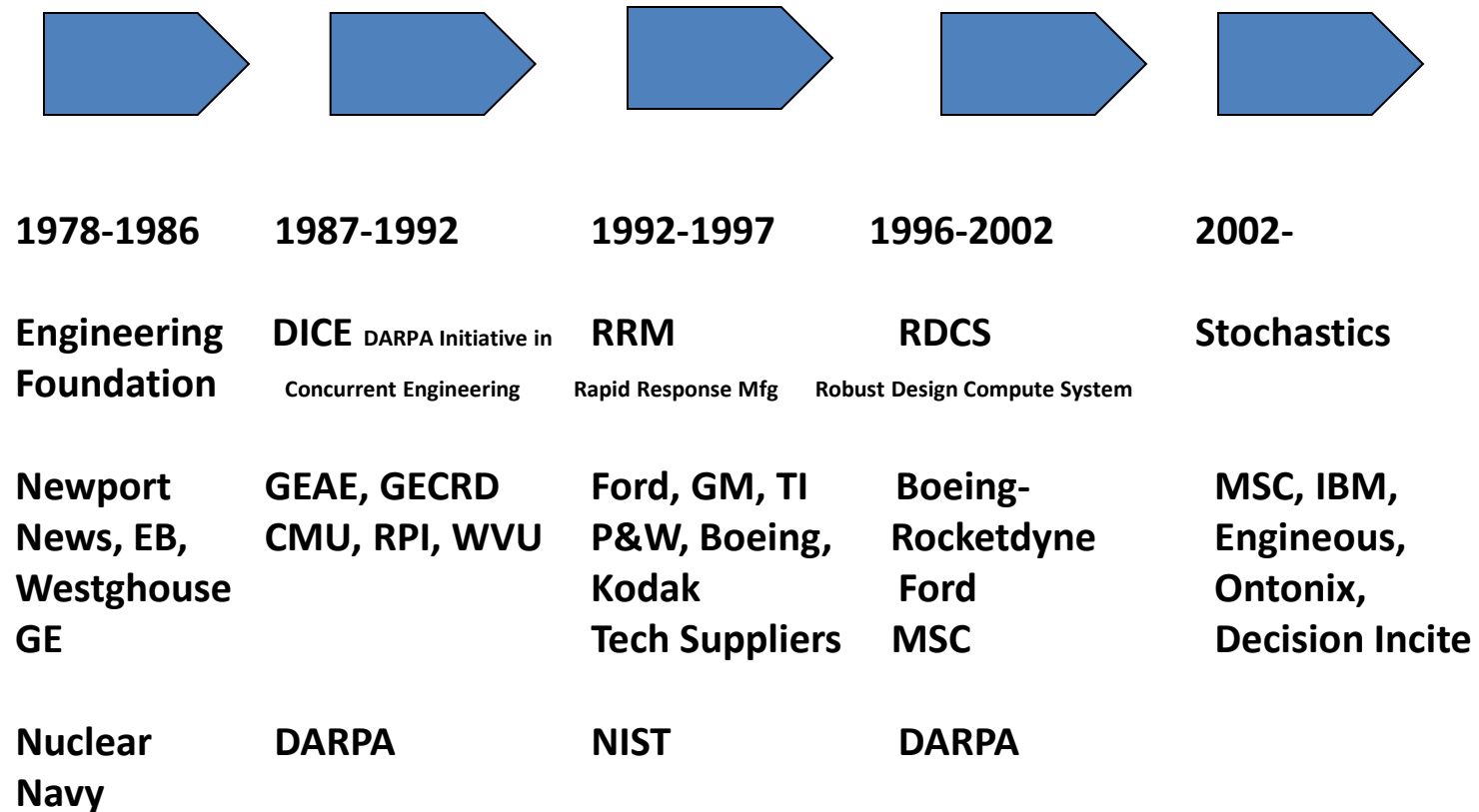
Gene Allen - Introduction

- **OBJECTIVE: TO PASS ON WHAT I KNOW on SIMULATION**
- **CAREER FOCUS:**
HOW TO USE COMPUTERS TO DO HELP MAKE BETTER DECISIONS
- **PRACTICE USED:**
User-driven **COLLABORATION** to commercialize technology
- **EXPERIENCE:**
 - Private sector: 1993-2008 MSC Software, Decision Incite
 - Non-profit: 1989-1993 NCMS
 - Government:
 - Hill – Senate Majority leader staff, 1987-1989
 - U.S. Navy
 - Active (5 yrs) - Qualified Nuclear Engineer/SWO, CGN Command Duty Officer, Wartime OOD, Nuclear Training Officer, PreCom CRA
 - Reserve Officer on CNO staff (15 yrs - N4, OP611)
 - SSBN Acquisition (Booz, Allen & Hamilton - 3 yrs)
 - Presently with Navy Surface Warfare Center Carderock
- **EDUCATION: Nuclear Engineering, MIT, 1978**



GEA Background in


Development of Computer Simulation Technology






Decisions Result in Actions

**BEWARE OF OUTLIERS –
THEY ARE NOT
'JUST ANOMALIES'**



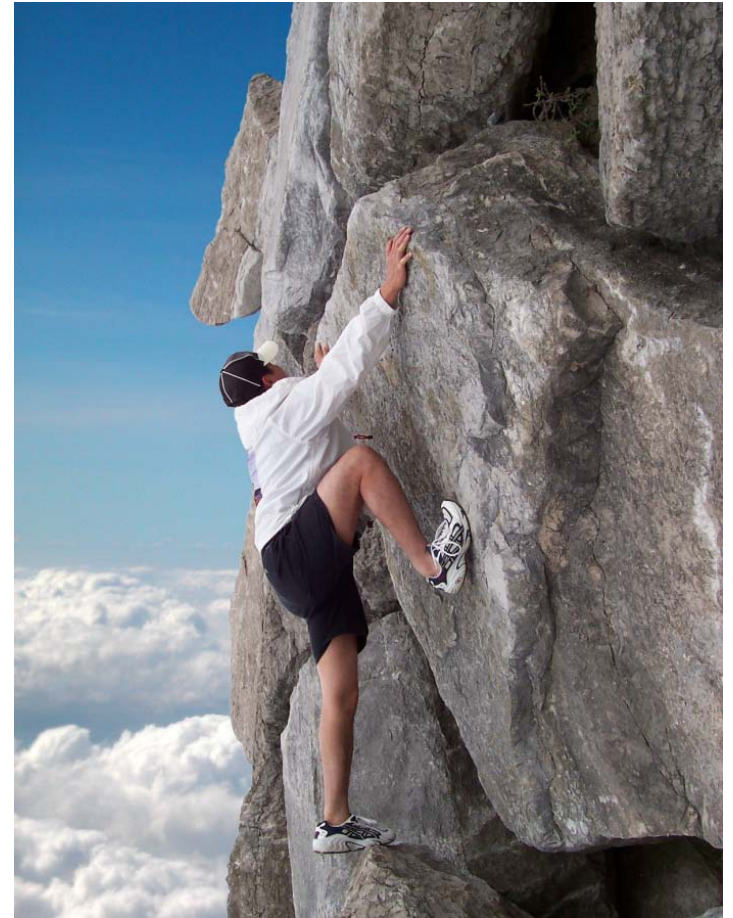
**Bad Decisions Result
when all possibilities
are not taken into account**

Good Decisions

- 
- A detailed image of a Mars rover, likely the Curiosity rover, on the surface of Mars. The rover is a six-wheeled vehicle with a complex body, featuring solar panels, a camera mast, and various scientific instruments. It is positioned on a vast, flat, reddish-brown landscape with subtle undulations and a hazy horizon. The lighting suggests a bright day on Mars, with long shadows cast by the rover.
- Based On Understanding:
 - All possible results
 - BEFORE taking action

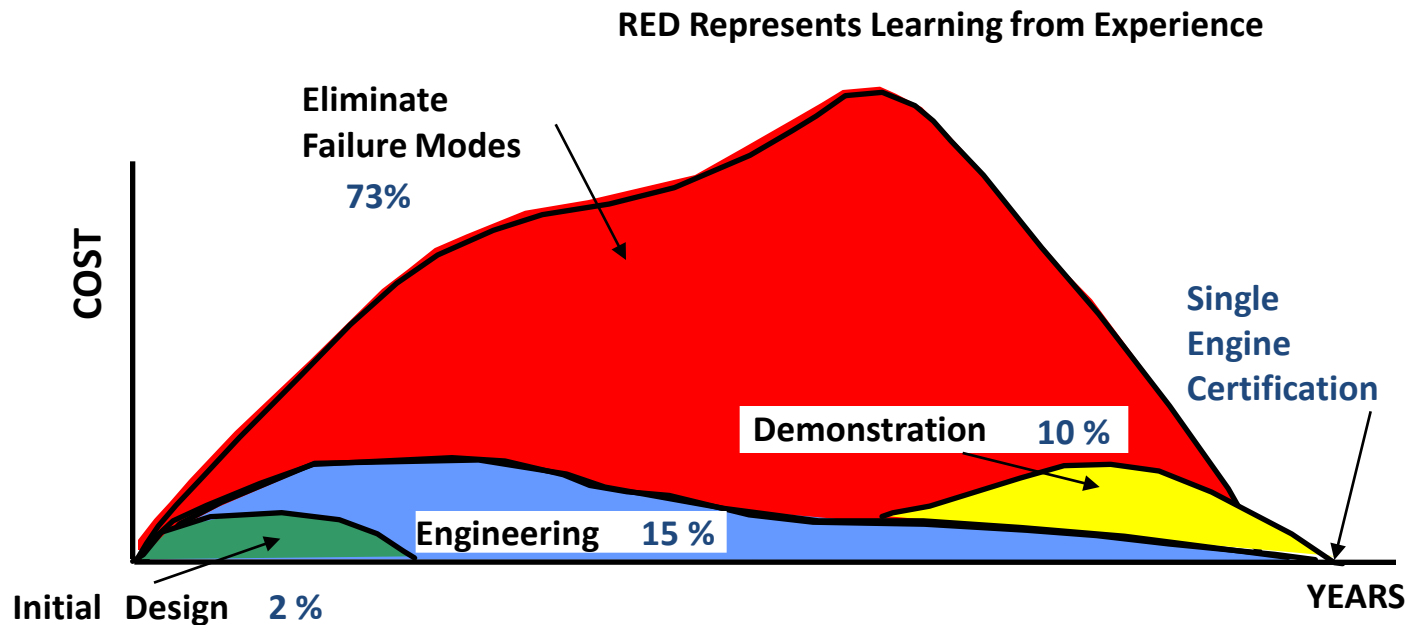
Understanding from Knowledge

**Knowledge is based on
Education & Experience**



Experience

- Takes Time and Money
 - Von Braun had hundreds of V2 failures before the Saturn V



- Graph for Saturn V rocket engines: \$2.2 Billion, 9 years

Engineering **before** Computers

Successful Engineering Cultures

- **U.S. Aerospace Industry**

- Produced: U-2, X-15, Saturn V, C-130, B-52



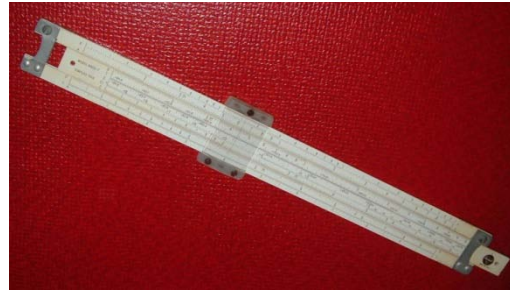
- **U.S. Navy Nuclear Program**

- Decades of dynamic operations of hundreds of nuclear power plants without casualties

- **Combined Theory and Practice**

Tools Engineers use to help do better engineering:

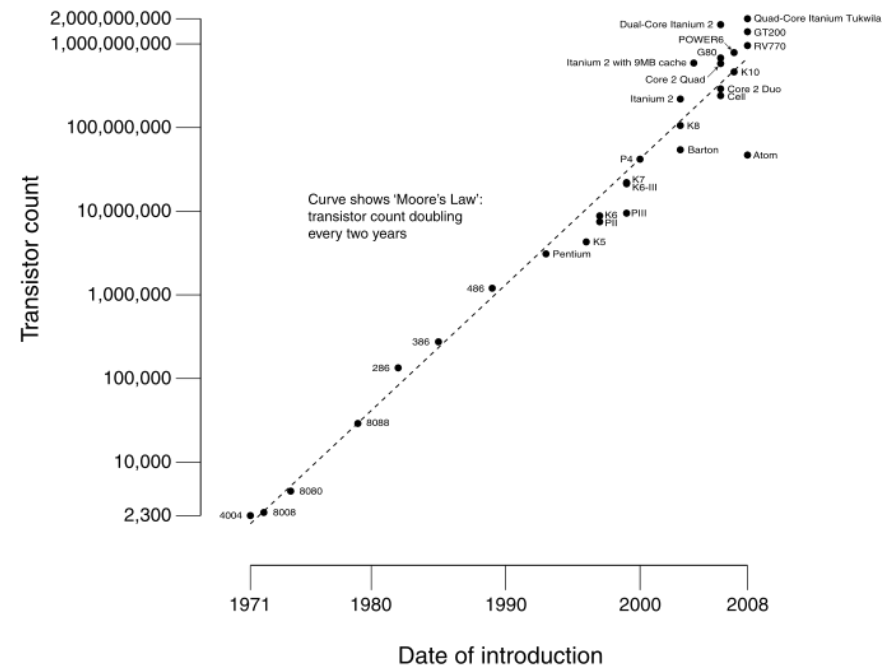
- Slide Rule
- Calculator



Moore's Law has provided an unprecedented capability

CPU Transistor Counts 1971-2008 & Moore's Law

- “Commodity” computing
- CPU/hr costs in ¢
- We have not yet taken advantage of this



Simulation can *Accelerate* Experience

- Understand How Products/Processes Function
- **New Processes to Forecast Risk**
 - Complexity used as metric.
- Identify:
 - Major factors driving functionality or contributing to potential failure.
 - Combinations of factors that lead to unexpected situations (outliers) that lead to failures.
 - Trends towards unstable situations.
- **These Abilities Exist Today!**
 - Due to advances in compute capability



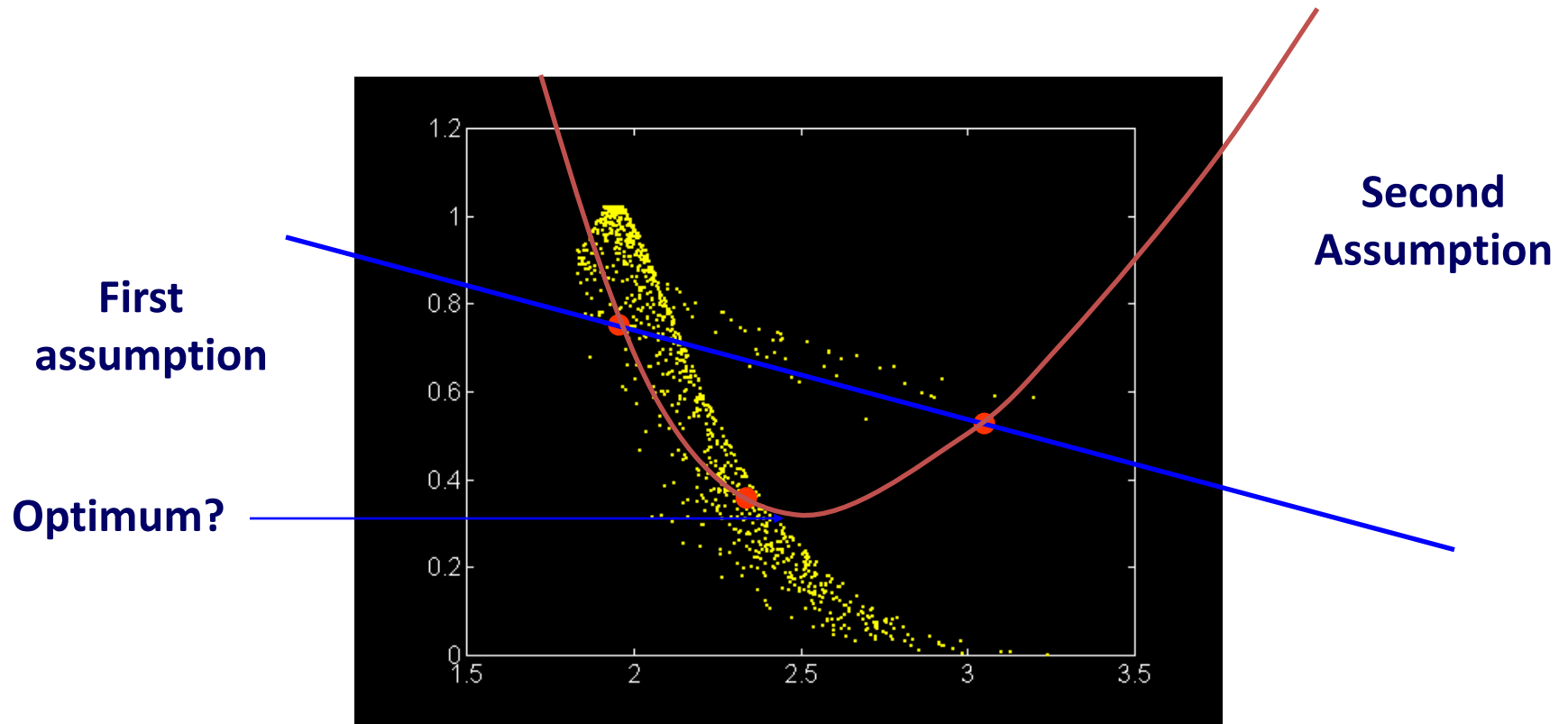
Commodity Computing can be used to provide tools to simulate reality to:

- **Compliment experience**
- **Learn what we do not know**

Tools need to be:

- **Accurate**
 - **Results readily verified**
 - **Independent results replication**
- **Easy to Use**
- **Interoperable**

Improved Understanding

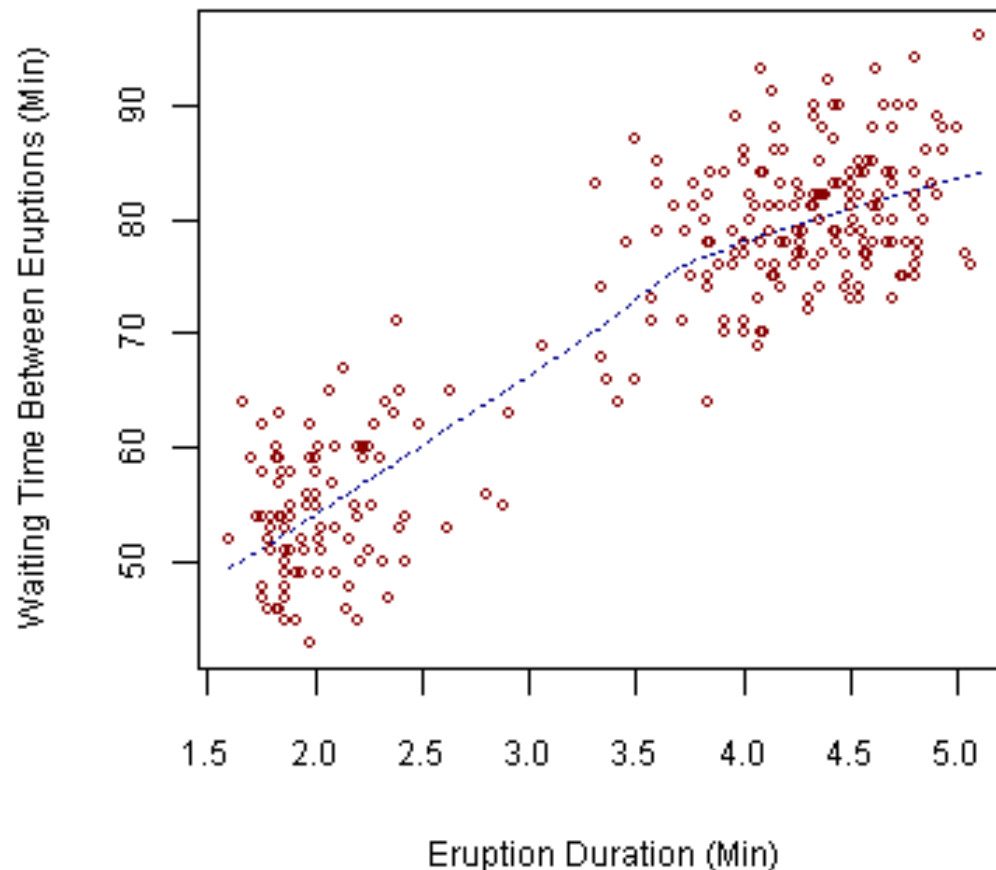


Reality - Each Point:

- May be the result of a test, or an analysis.
- Is the result of different combinations of variables.

EXPERIENCE – Forms Engineering Knowledge Base

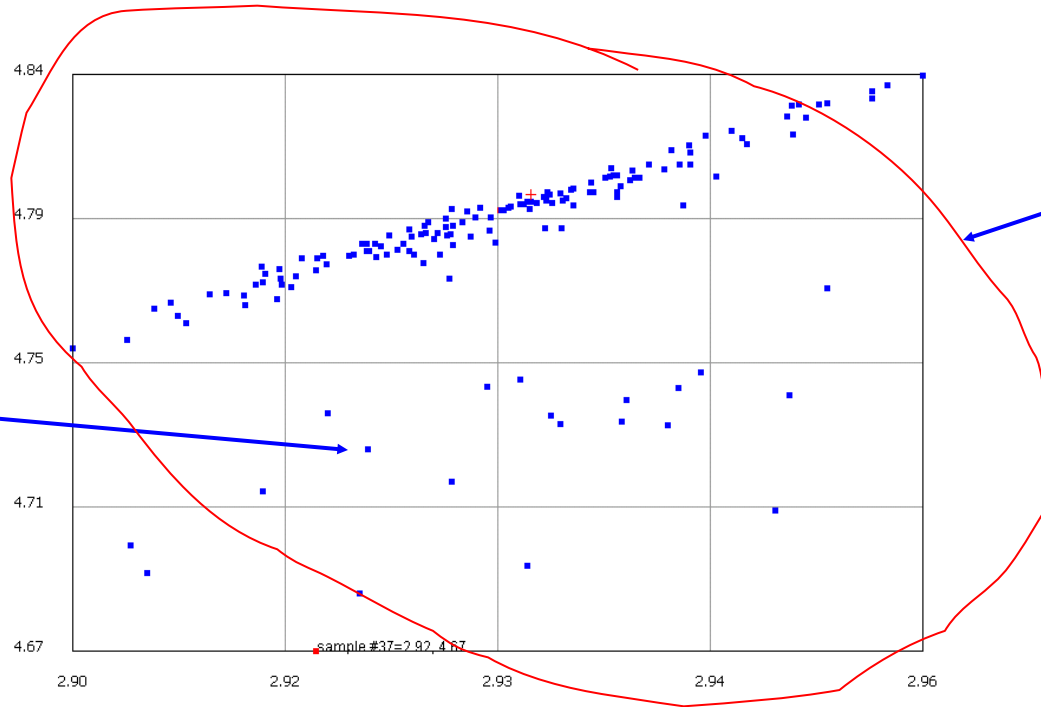
Old Faithful Eruptions



Analysis vs. Simulation

One run vs. Many runs

Single
computer
run =
Analysis



Multiple
computer
runs =
Simulation

Understanding = Knowing the topology and structure of the data cloud.

Simulation must address Variation

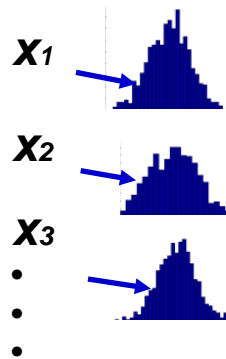
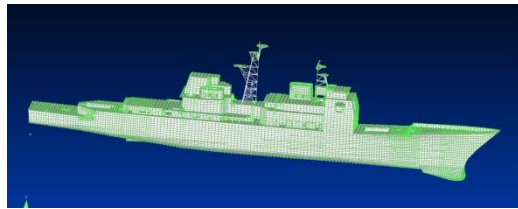
- Material Variation Examples

MATERIAL	CHARACTERISTIC	VARIATION
Metallic	Rupture	8-15%
	Buckling	14%
Carbon Fiber	Rupture	10-17%
Screw, Rivet, Welding	Rupture	8%
Bonding	Adhesive strength	12-16%
	Metal/metal	8-13%
Honeycomb	Tension	16%
	Shear, compression	10%
	Face wrinkling	8%
Inserts	Axial loading	12%
Thermal protection (AQ60)	In-plane tension	12-24%

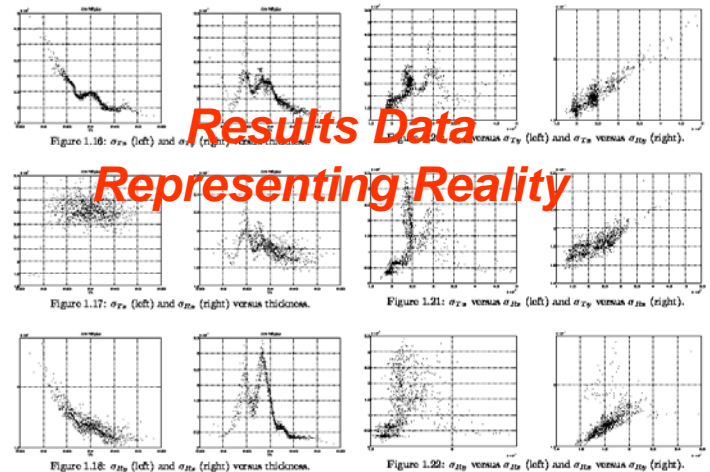
- Similar Variation with Geometry
- More Variation with Forces

It's the Way the World Is

Simulation from an Analysis Model



100 +
runs



1.

2.

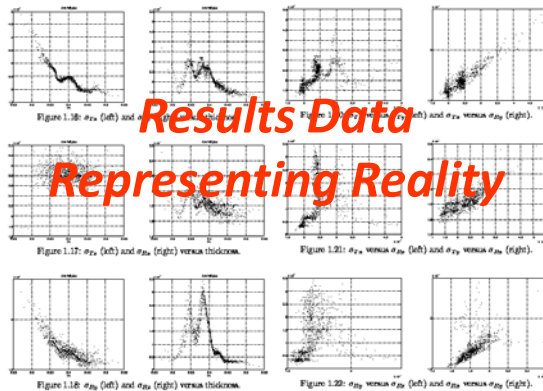
3.

4.

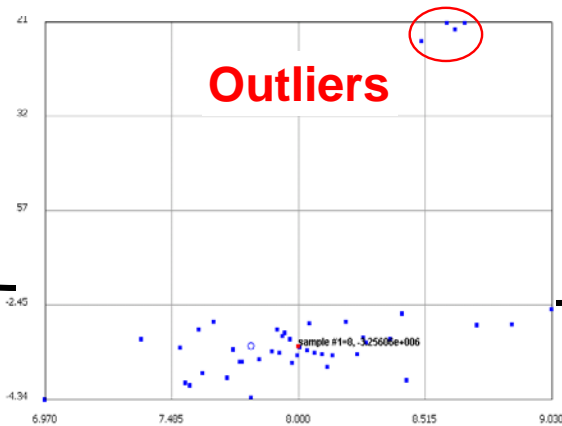
PROCESS STEPS

1. Start with a product or process computer analysis model
2. Replace all discrete inputs with ranges and distributions
3. Run model $\approx 100 +$ times randomly changing all variables
4. Result is a Multi-dimensional data cloud that represents reality

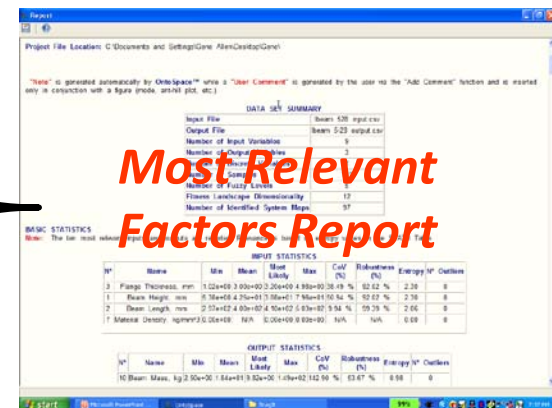
Simulation Results to Information



Insight Map



Most Relevant Factors Report



The CHALLENGE

**PREVENT FAILURES
Of Complex Systems
& Programs**



**We Don't Know
What We
Don't Know**

To LEARN WHAT WE DO NOT KNOW

We Need To

MINIMIZE ASSUMPTIONS

Common Foundation Assumptions:

- Continuity
- Mathematical Constructs
 - Gödel's incompleteness theorems:
 - Any computable axiomatic system that is consistent, cannot be complete;
 - The consistency of the axioms cannot be proved within the system.
- General Over-Simplifications

Assumption that Violates Physics

$$\frac{\partial f}{\partial x}$$

This is NOT true



$$\begin{aligned} y &= a \\ z &= b \end{aligned}$$

From Analysis Models to Knowledge



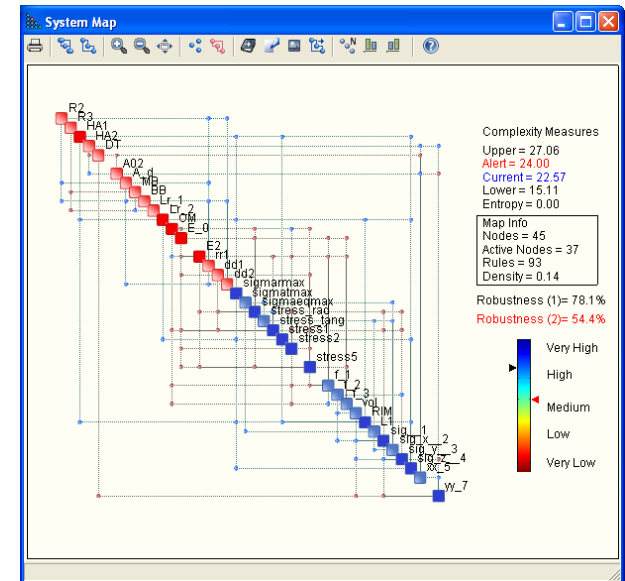
Model



Simulation



Data

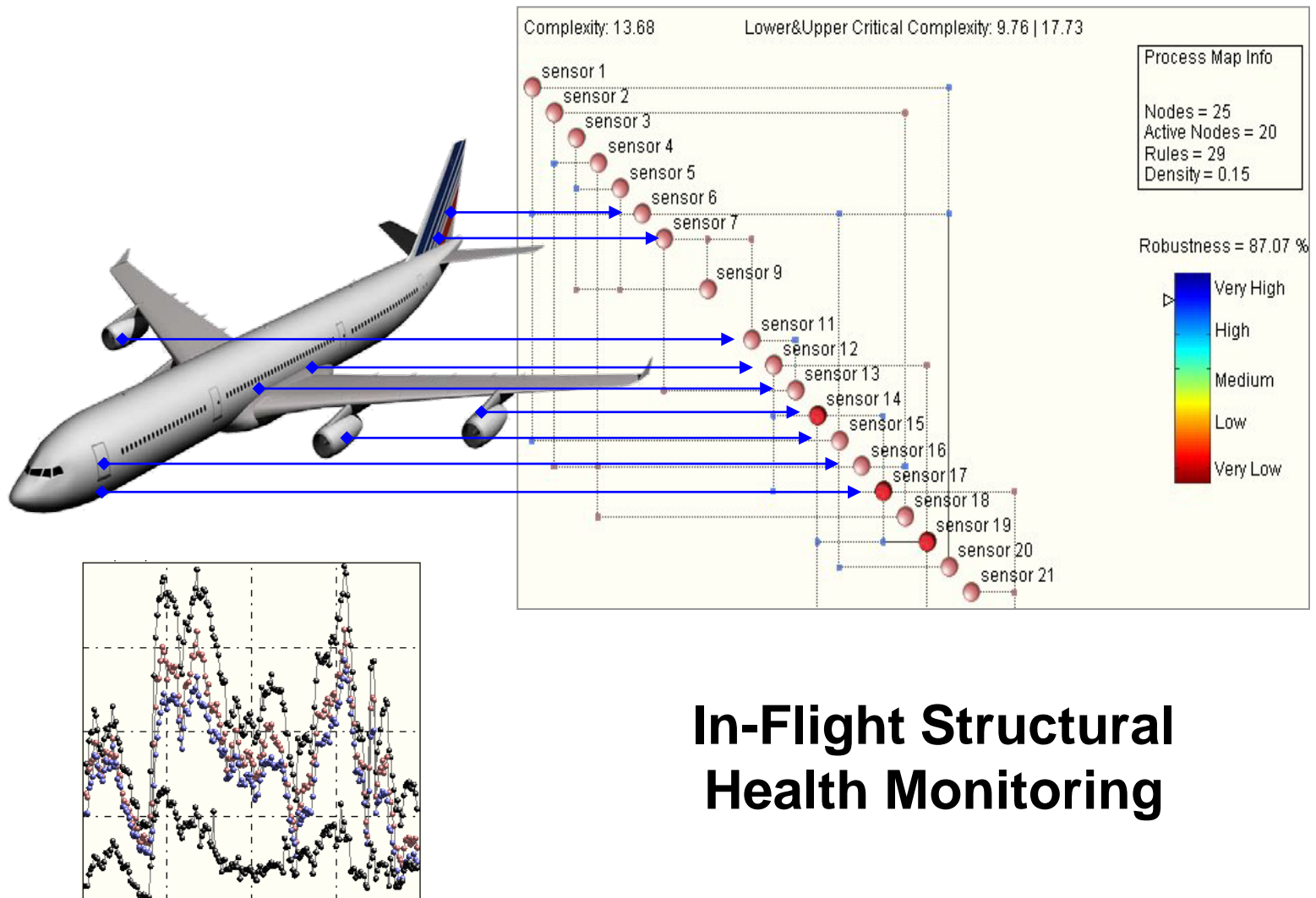


System Map

The System Map shows:

- Relationships between parameters
- Complexity levels
- Outliers

From Raw Data to Knowledge

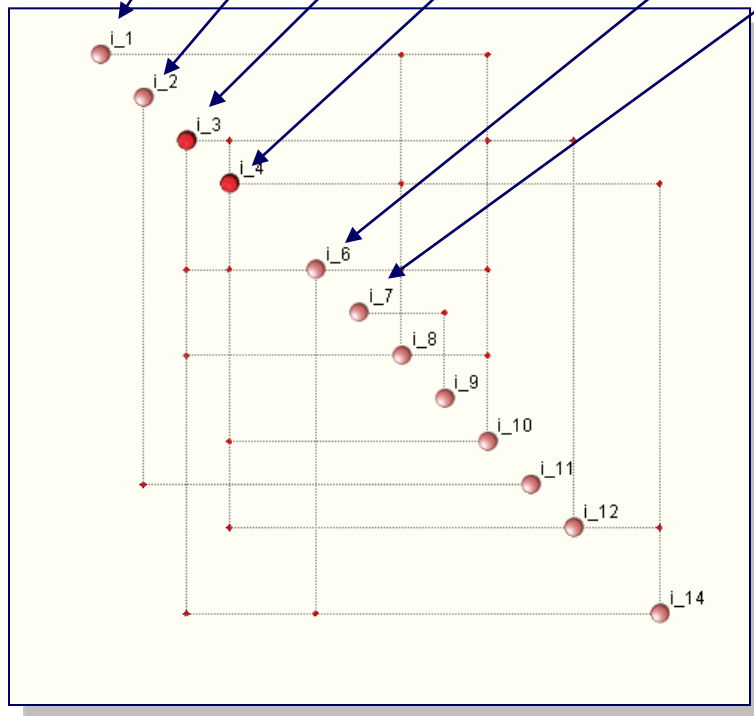


In-Flight Structural Health Monitoring

Complexity and System Maps

Complexity is a system **attribute** which reflects how information is organized and flows. Complexity can be measured and managed.

	Variable 1	Variable 2	Variable 3	Variable 4	Variable 5	Variable 6	Variable 7	Variable 8	Variable 9	Variable 10	Variable 11	Variable 12	Variable 13	Variable 14
measurement 1	2.7202898e+003	7.4722596e+001	3.3732330e+001	1.0184837e+002	9.0967402e+001	1.3025740e+000	5.8491109e+002	2.0983948e+003	5.7746246e+002	2.0745664e+003	7.7027814e+001	4.7343477e+001	9.3212680e+001	1.4980173e+000
measurement 2	2.7202588e+003	7.4722596e+001	3.3732330e+001	1.0184837e+002	9.0967402e+001	1.3025740e+000	5.8491109e+002	2.0983948e+003	5.7746246e+002	2.0745664e+003	7.7027814e+001	4.7343477e+001	9.3212680e+001	1.4980173e+000
measurement 3	2.7472810e+003	7.5259340e+001	3.2769872e+001	9.9563658e+001	9.0359902e+001	1.2958545e+000	5.7800692e+002	2.1200529e+003	5.7044970e+002	2.1071991e+003	7.7609260e+001	4.4859857e+001	9.2513456e+001	1.4691249e+000
.														
measurement 498	2.6963742e+003	7.4267584e+001	3.2300819e+001	9.9709857e+001	9.0880438e+001	1.2846033e+000	5.0231885e+002	2.0989936e+003	5.9500231e+002	2.0844376e+003	7.6470372e+001	4.7246972e+001	9.2445500e+001	1.4934932e+000
measurement 499	2.7161385e+003	7.4648496e+001	3.1284797e+001	9.7180980e+001	8.9747118e+001	1.2855390e+000	5.7932586e+002	2.1128403e+003	5.7174746e+002	2.1006561e+003	7.7008998e+001	4.2349411e+001	9.3013352e+001	1.4359544e+000
measurement 500	2.6995332e+003	7.5451365e+001	3.4156452e+001	1.0258146e+002	9.0543986e+001	1.3110797e+000	5.7014063e+002	2.0590153e+003	5.6257964e+002	2.0467060e+003	7.7843365e+001	4.4955206e+001	9.2165592e+001	1.4766825e+000



A system can be represented as:

- Nodes with each node representing a characteristic of the system, and
- Links between nodes representing the relationships between characteristics.

System maps are built on **analysis models or raw user data**.

- Links are established **automatically** using Ontospace software.

The Complexity of a system is based on the number and nature of the nodes and links.

Complexity x Uncertainty = Fragility

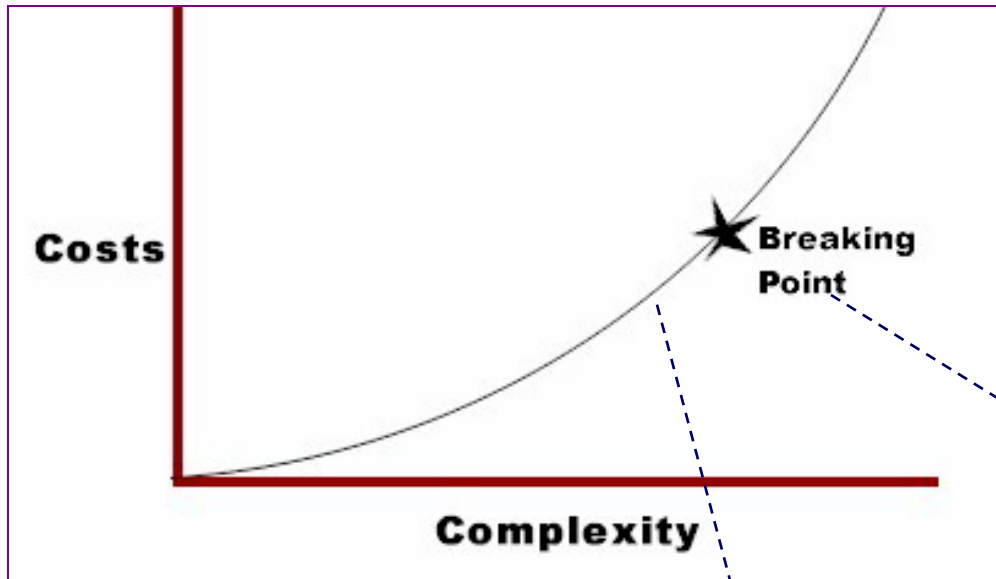
Applies to product and enterprise:

$$\begin{array}{c} C_{\text{business model}} \\ \times \\ U_{\text{environment}} \\ = \\ F_{\text{enterprise}} \end{array}$$



Managing Complexity

- More complex systems provide greater functionality and can be more stable in having redundancy and flexibility.
- However, complexity cannot grow indefinitely, and has a maximum, called **critical complexity**. A system becomes fragile and vulnerable near this point.

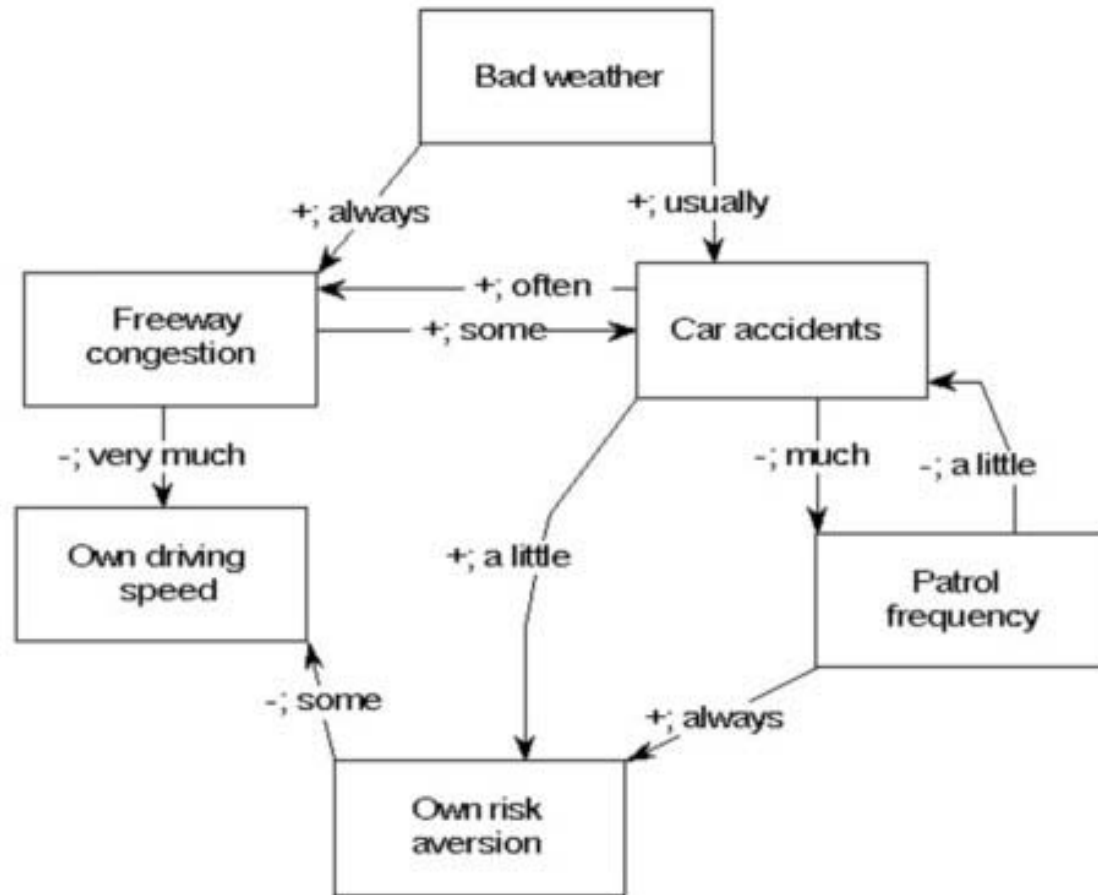


As complexity increases, the cost of managing the complexity increases at an exponential rate until the system finally collapses.

Thomas Frey, The da Vinci Institute



FUZZY COGNITIVE MAP

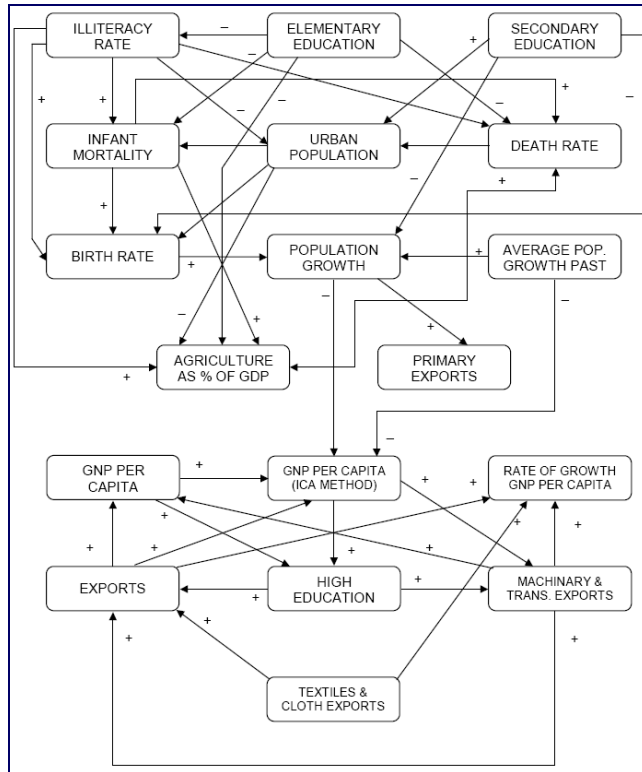


This Fuzzy Cognitive Map shows how bad weather can affect how fast you drive on a California freeway in the daytime.

From *"Fuzzy Thinking"* by Bart Kosko (Flamingo, 1994).

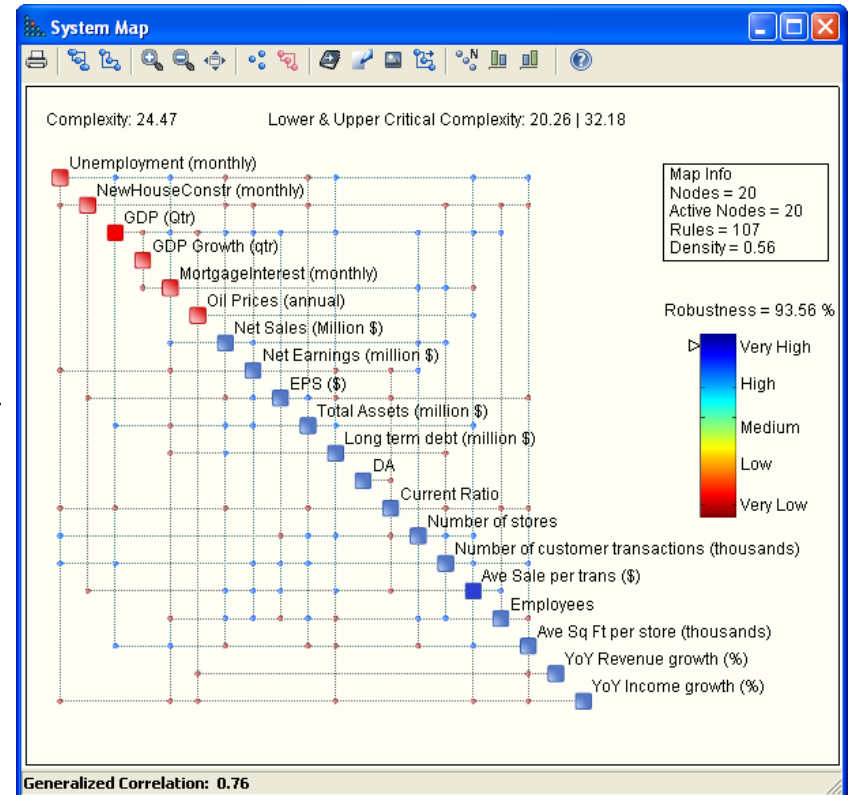
Decision Maps for Understanding Influence and Information Flow

Past



Hand drawn, subjective

Today



**Computer generated,
extracts information from data**

Simulation - Input to Knowledge

- Can compliment education and experience
- Can be validated by all members of a team



A good team will beat a superstar

Simulation-generated Information Infrastructure

- The pieces are in place
 - Computer HW, SW, IT, Web technologies
 - Advance “Proven” and new methods to leverage these capabilities:
 - Incorporate variability
 - Manage complexity
 - Methods are scalable
 - Expertise
- provides transparent credibility

USE **INFORMATION FROM SIMULATION**

TO LEARN What We Do Not Know

Inputs

- **Less Assumptions**
- **More Variables**

Outputs - Identify WHAT'S IMPORTANT

- **Significant Variables**
- **Outliers**

Process

- **Scalable to people and disciplines**
- **Replicable**

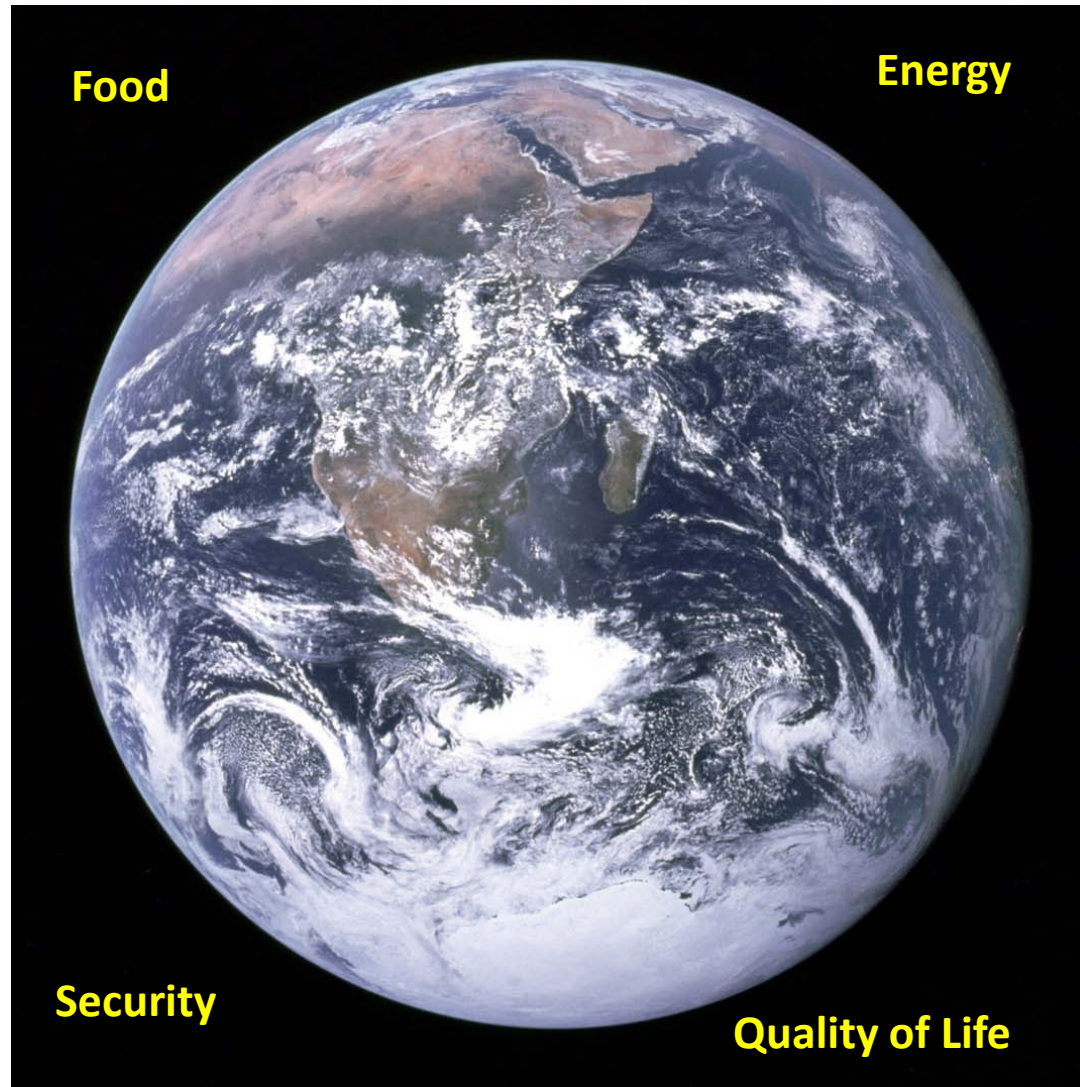
Simulation for Better Understanding

- **Leverage Commodity Computing**
- **Augment and Compliment Experience**

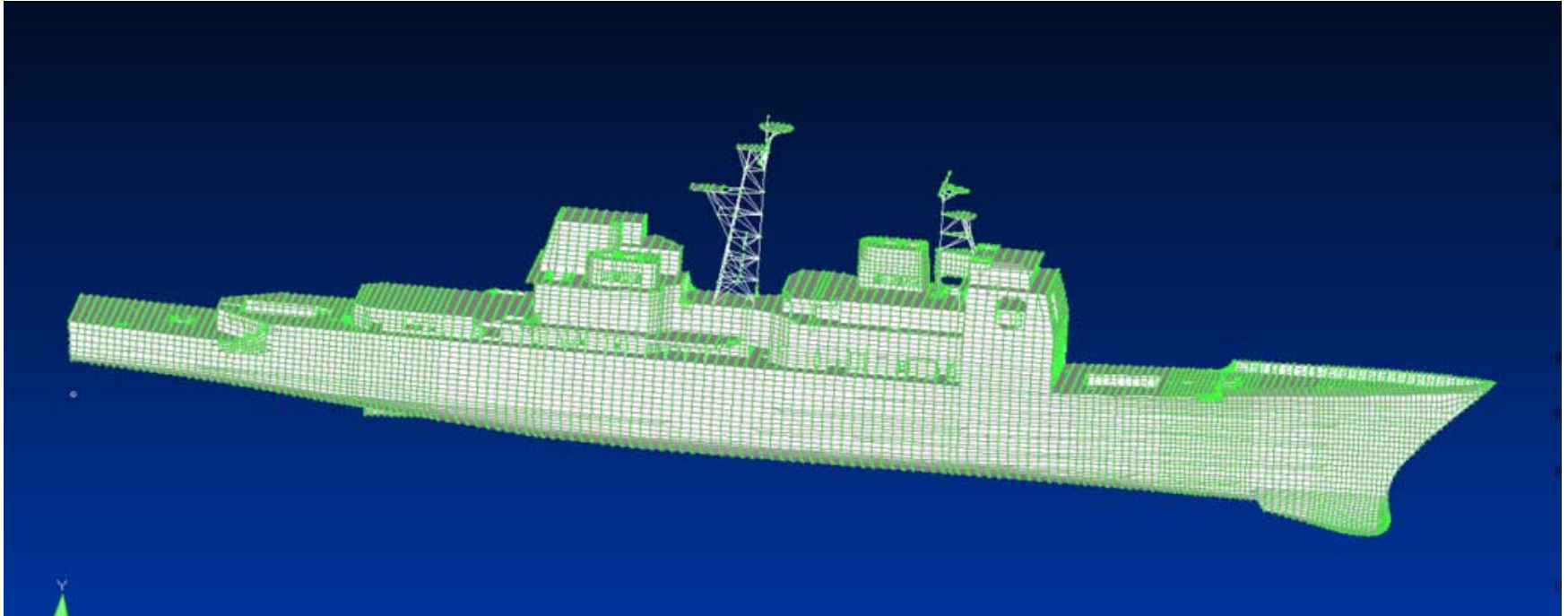
**Can we learn from
Virtual Experience?**

Simulation for Better Understanding

Can We Afford not to LEARN?



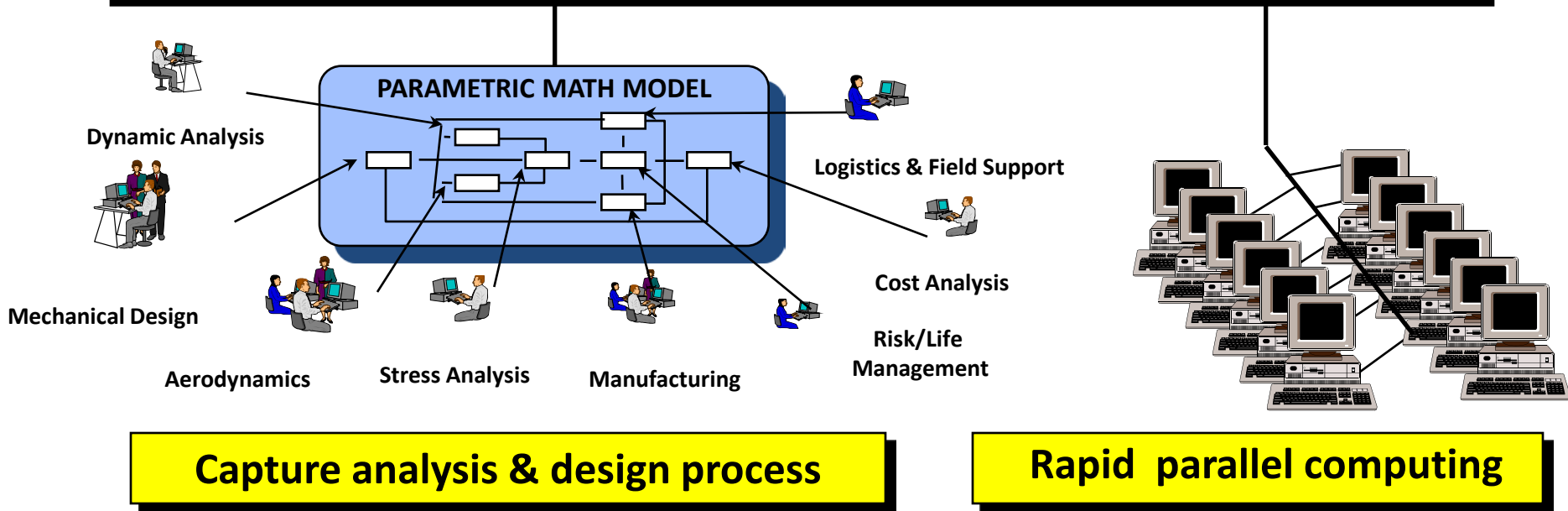
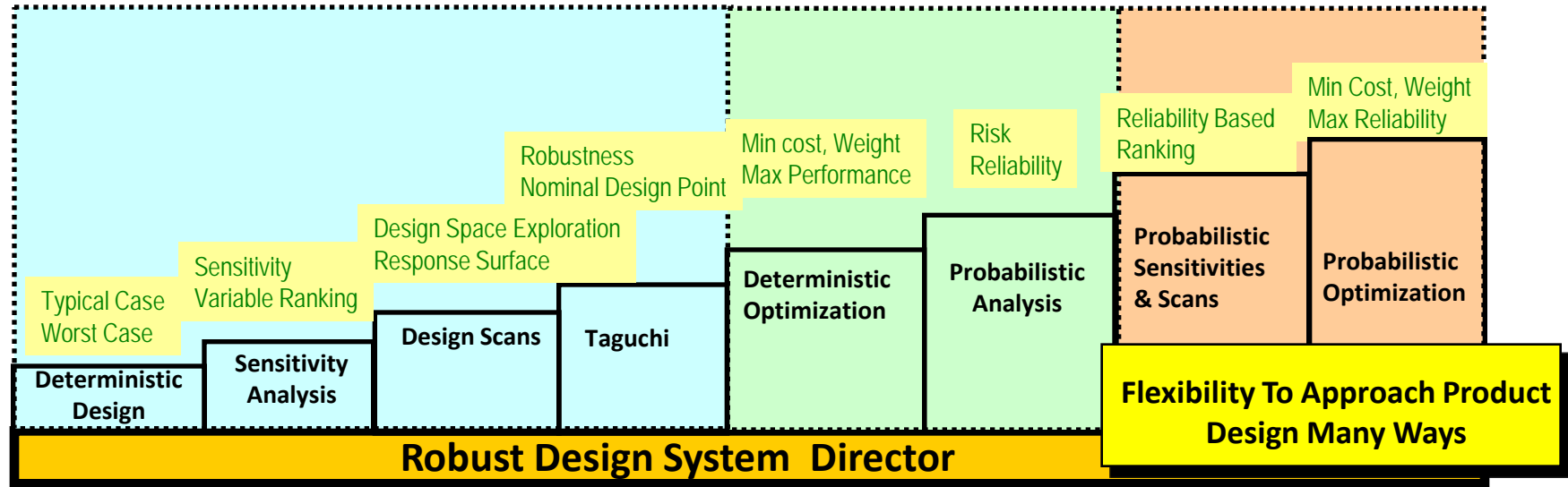
Back-Up Slides



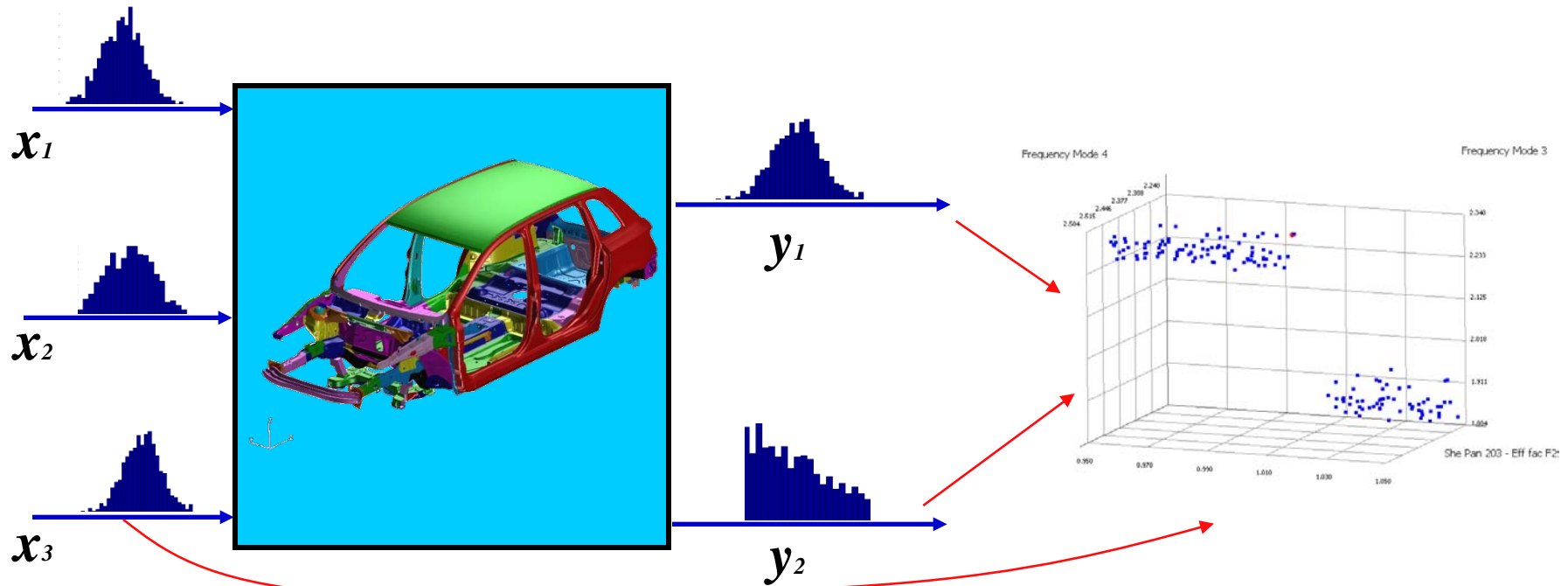
CG 53 FEM from ABS

- 118,855 elements
- 3 loading conditions:
 - Still Water, Sagging and Hogging in 25 ft waves
- 243 MB file takes 33 minutes to run on laptop

MSC Robust Design Overview



MONTE CARLO METHOD



Sources of Variability

- Material Properties
- Loads
- Boundary and initial conditions
- Geometry imperfections
- Assembly imperfections
- Solver
- Computer (round-off, truncation, etc.)
- Engineer (choice of element type, algorithm, mesh band-width, etc.)

Solution:

Establish tolerances for the input and design variables.

Measure the system's response in statistical terms.

Monte Carlo Simulation Background

- Allows engineers to **introduce hundreds of thousands of stochastic variables** into the problem, and still call the solver only 100 times to obtain correct results.
- The power lies in the fact that the **cost**, i.e. the number of solver calls, **is independent of the number of variables** in a problem.

Why Stochastic Analysis

Address the Curse of Dimension

“Monte Carlo simulation was developed by the Los Alamos team (the people who developed the nuclear bomb for the US during the 1940's). They had high-dimensional integrals to solve, and traditional methods of numerical integration failed them because of the curse of dimensionality.

What is so fantastic about Monte Carlo simulation is the fact that its precision is proportional to the square root of the number of scenarios used, and **THIS RESULT IS ENTIRELY INDEPENDENT OF THE NUMBER OF DIMENSIONS OF THE PROBLEM**. Effectively, Monte Carlo simulation was developed to break the curse of dimensionality. The history of World War II might have been different if it were never invented.”

Monte Carlo Simulation Results

Number of 2D Views of Results = Sum of all integers from 1 to (Number of Variables - 1)

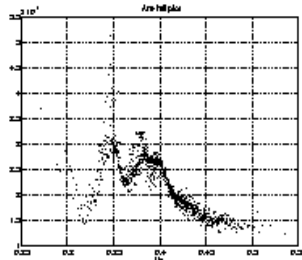
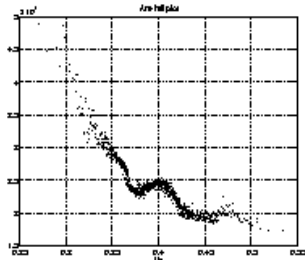


Figure 1.16: σ_{Tx} (left) and σ_{Ty} (right) versus thickness.

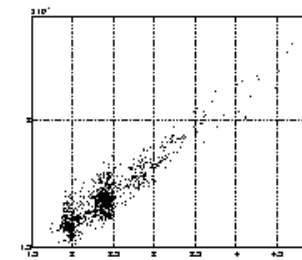
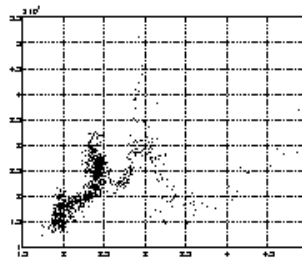


Figure 1.20: σ_{Tx} versus σ_{Ty} (left) and σ_{Tx} versus σ_{Rx} (right).

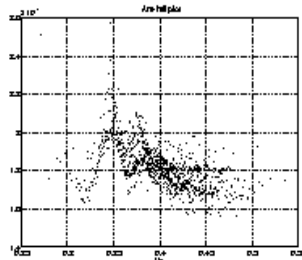
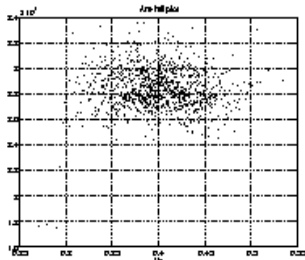
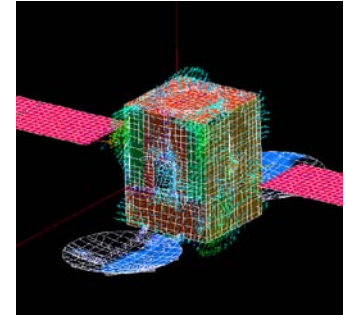


Figure 1.17: σ_{Tx} (left) and σ_{Rx} (right) versus thickness.

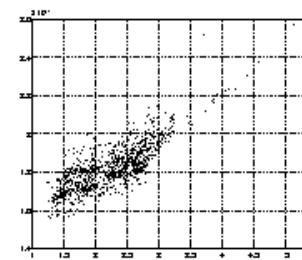
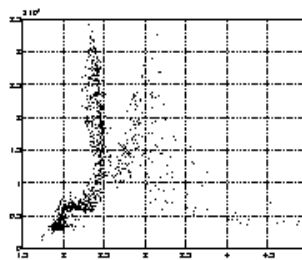


Figure 1.21: σ_{Tx} versus σ_{Rx} (left) and σ_{Ty} versus σ_{Rx} (right).

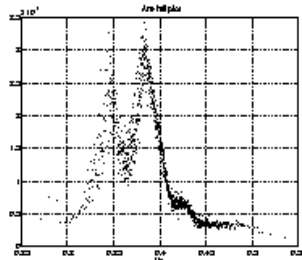
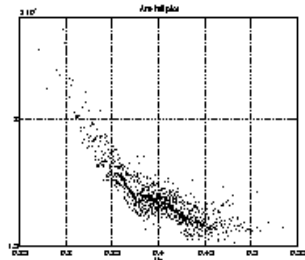


Figure 1.18: σ_{Ry} (left) and σ_{Rx} (right) versus thickness.

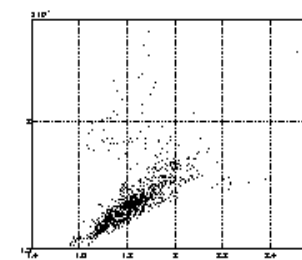
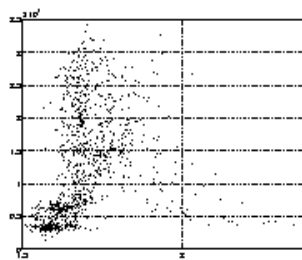


Figure 1.22: σ_{Ry} versus σ_{Rx} (left) and σ_{Rx} versus σ_{Ry} (right).

12 of the 78
2D views that
resulted from a
simulation with
6 outputs from
a scan of 7
inputs with
uniform
distributions.

SIMULATION-SUPPORTED ENGINEERING

Key Validation Events

MSC Robust Design, 2002- 2005

- **MSC CTO Dr. Ed Stanton focuses on probabilistic analysis following:**
 - **RDCS experience at MSC and Boeing**
 - **Attending 2001 Stochastic Simulation Conference in Germany**
 - **Crystal Ball use**
- **MSC hired Dr. Jacek Marczyk**
- **2003 Innovation of the Year Award - German CAD-CAM Magazine**
- **Positive Feedback from Customers and Application Engineers**
- **Limited to Nastran applications**
- **Needed ability to change geometry, run with other solvers**

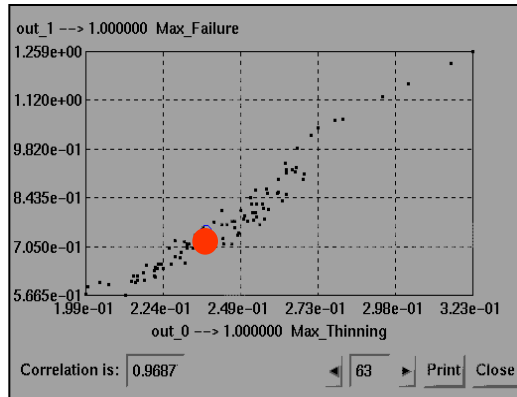
Process Validation

- **Dr. Schueller - MIT 2005 keynote presentation**
- **Dr. Hazelrigg - NSF meeting**
- **MIT mathematician K. Keilmeyer –**

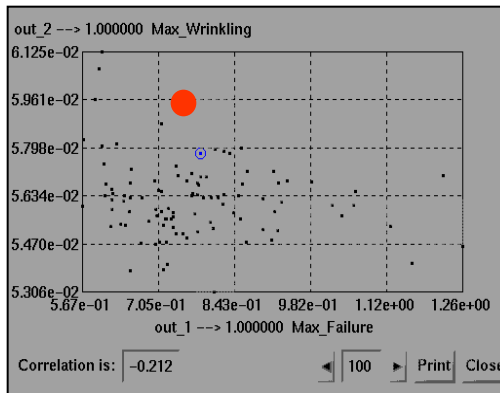
“Monte Carlo Simulation is not elegant, it just gives the right answers.”

Why Stochastic Analysis

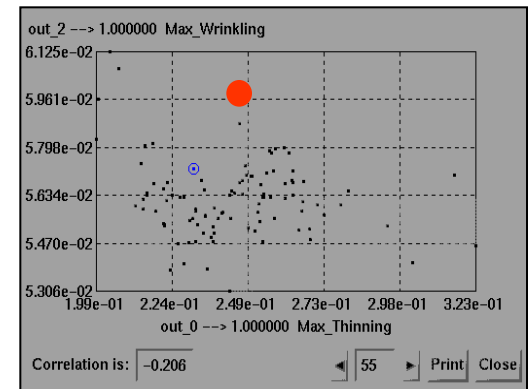
The most likely behavior (practically) never corresponds to the most likely values of input/design variables.



Max. Failure vs.
Max. Thinning



Max. Failure vs.
Max. Wrinkling



Max. Thinning vs.
Max. Wrinkling

● Result of
Nominal Run

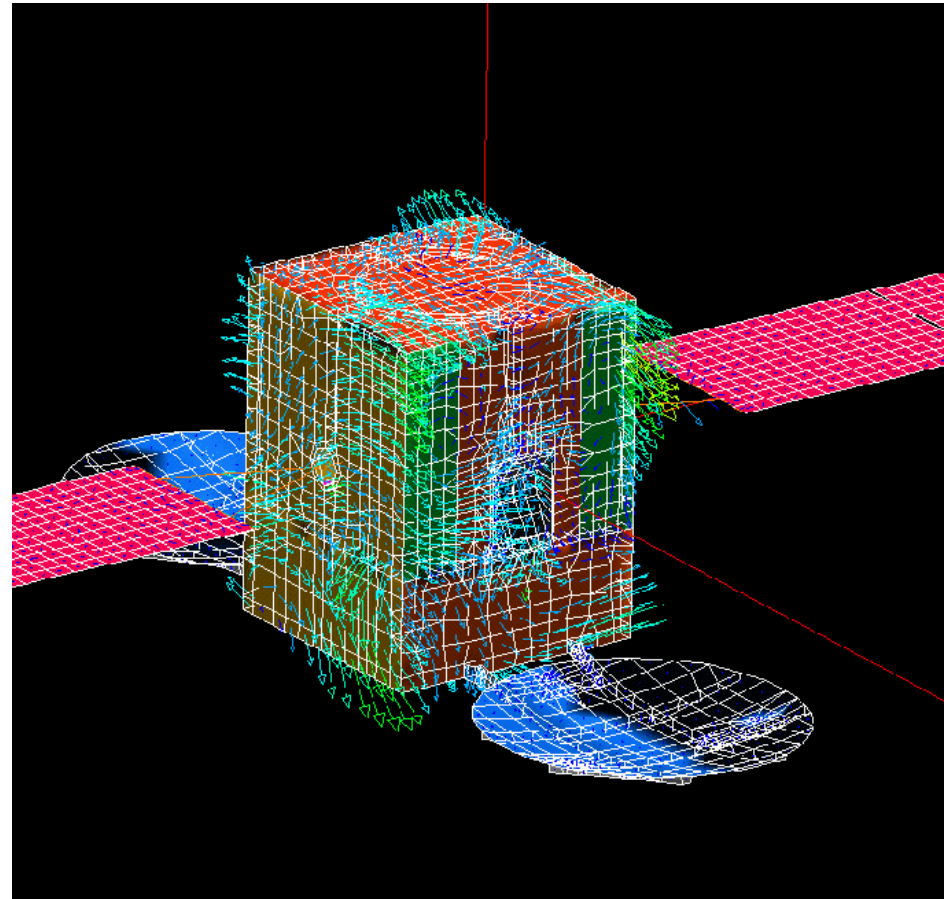


START WITH A GOOD MODEL

Accurately Capture:

- Physics
- Loads and boundary conditions
- Material properties
- Geometry

Remember **“All models are wrong.
Some are useful.”** J. Box



Modeling Processes:

- **In Analysis Software**
 - NASTRAN, Ansys, STAR-CD, Dyna, etc.
- **In CAD Software translated to Analysis Model**
 - Catia/UG/Pro-E/... to Hypermesh/Patran/...
- **Multi-Disciplinary Process Model Mapping**
 - iSight/ModFrontier/ModelCenter/....

Results Processing/Visualization

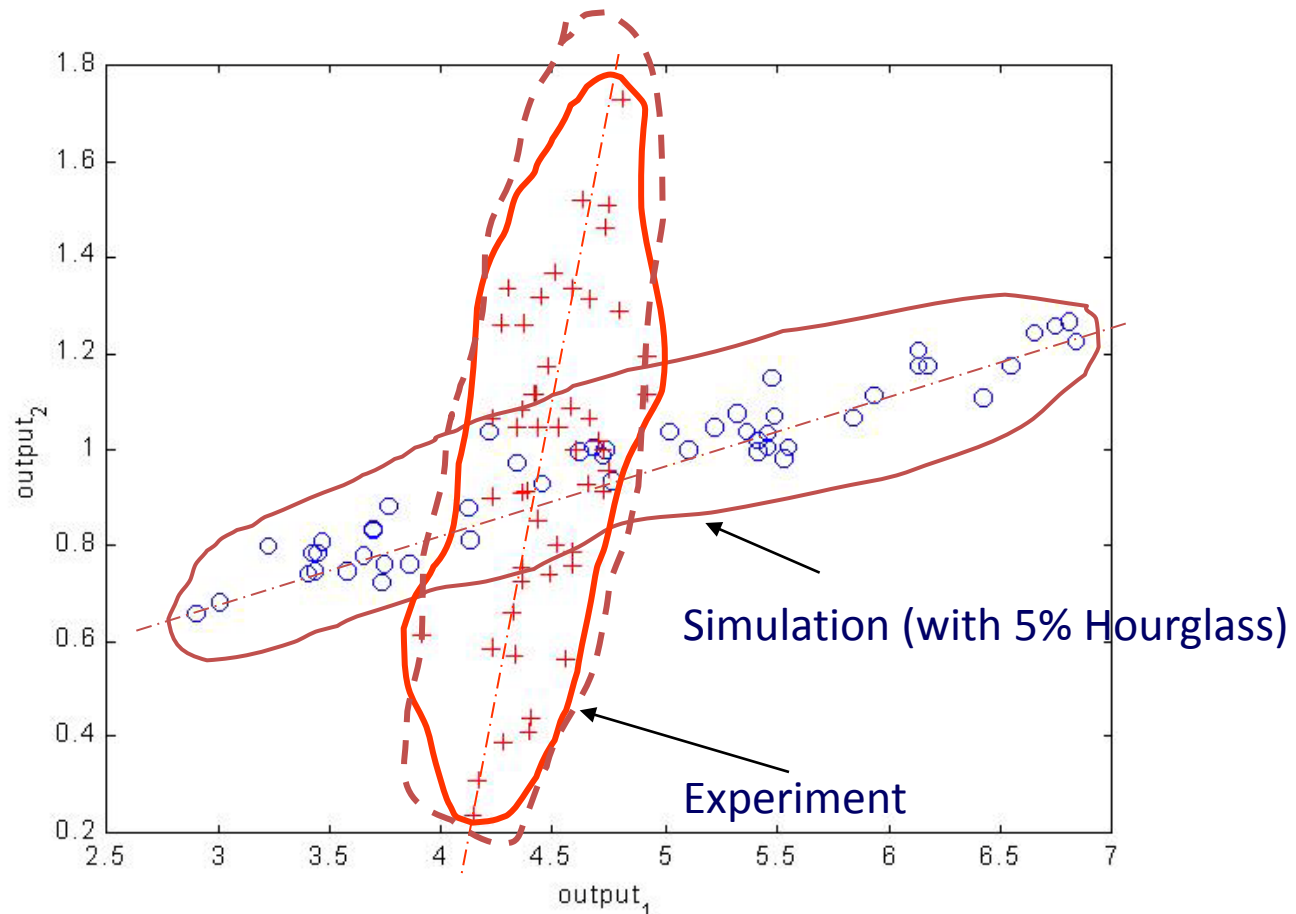
Remember **"All models are wrong. Some are useful."** J. Box

Model Verification

- Make sure the math is correct
- Model checking with probabilistic analyses
 - If solver runs 100 times the model is likely valid
- Good CAE models exist
 - Primarily done for forensic analysis
 - Represents one instance of reality
 - Stochastic analysis can provide information

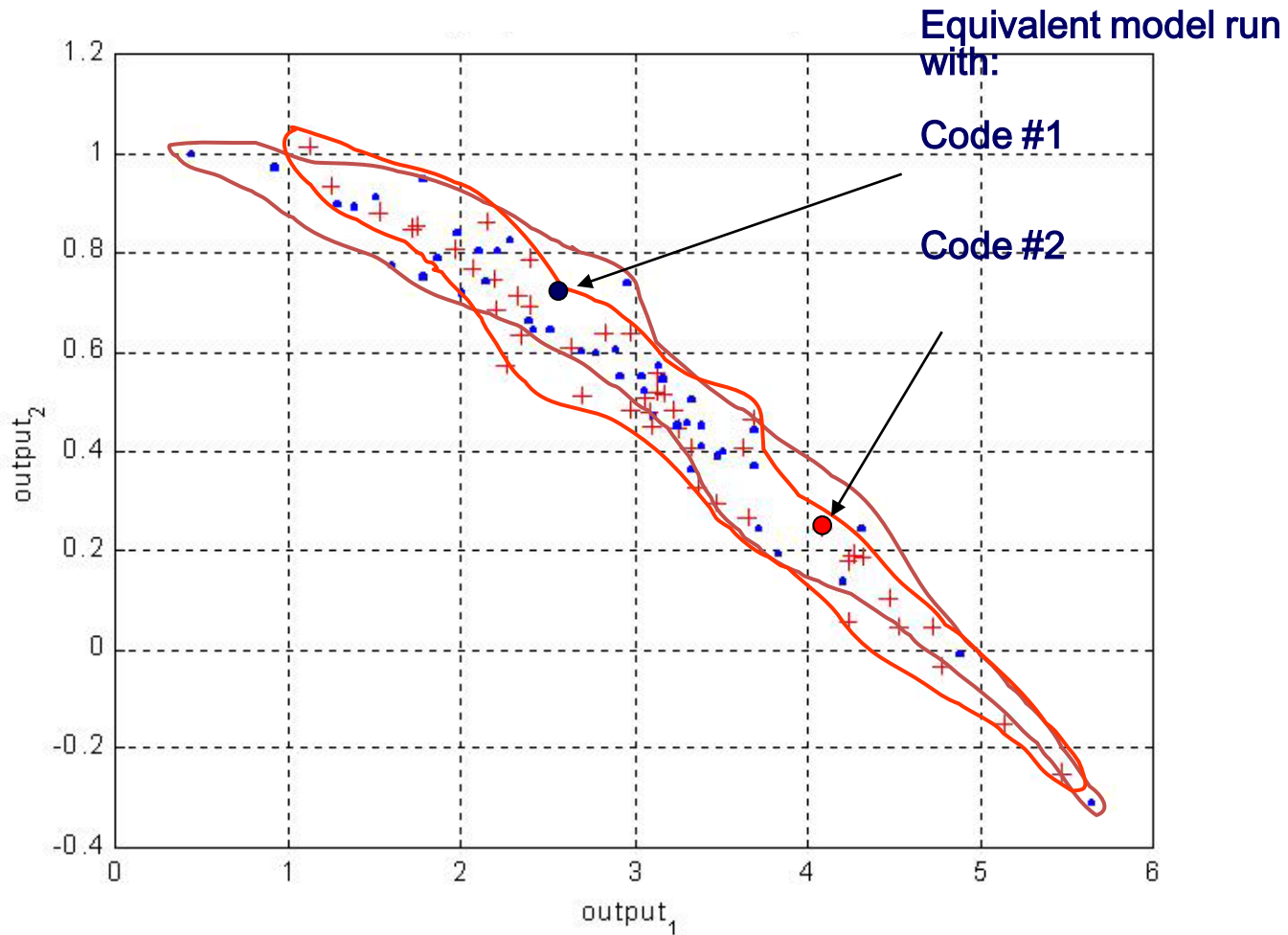
Remember **“All models are wrong. Some are useful.”** J. Box

Quantifying model confidence



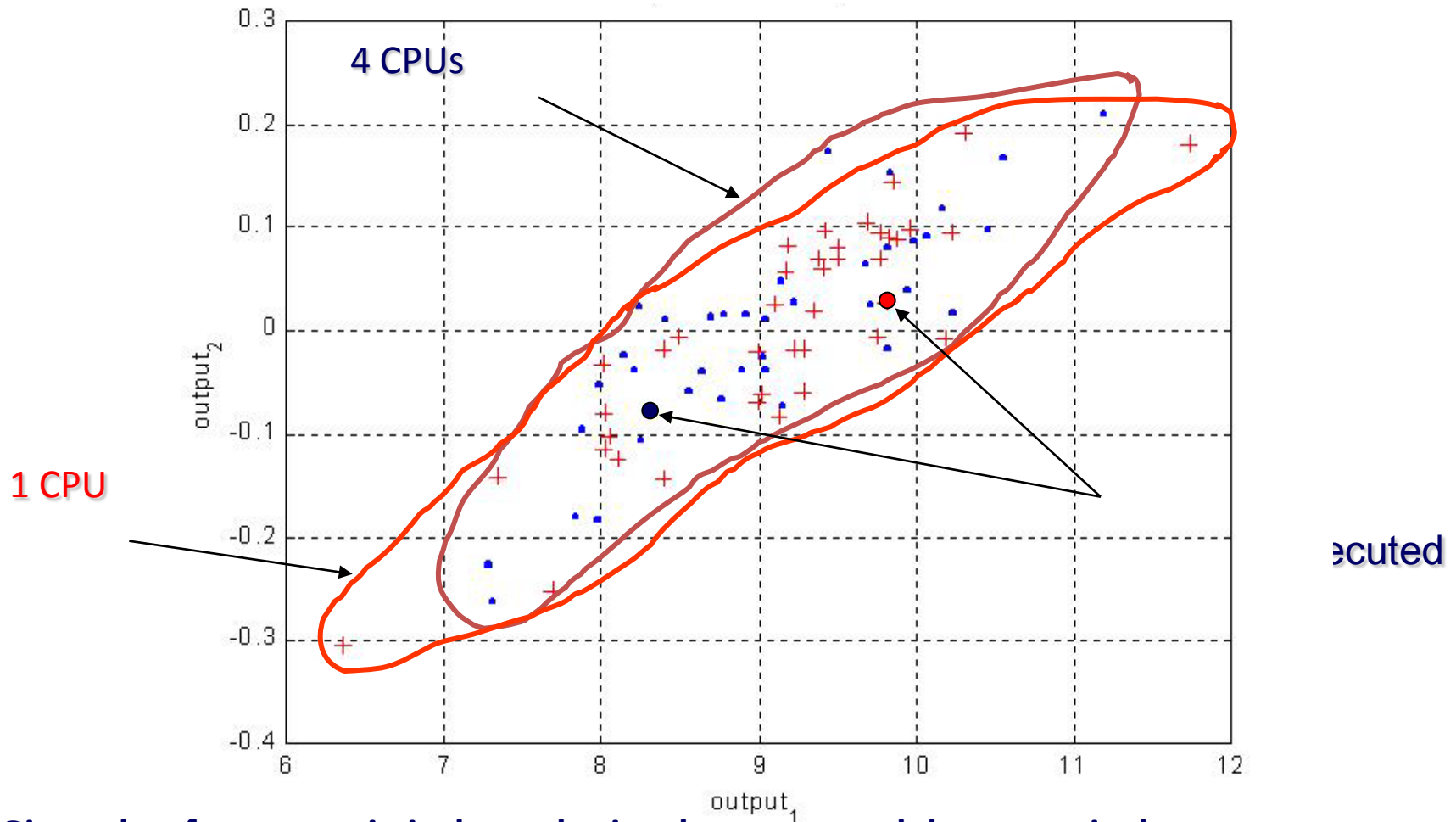
The two meta-models show excellent statistical equivalence (shape, aspect ratio, cog position). The difference in orientation has been found to be due to 5% HG energy in the FE model.

Which crash code?



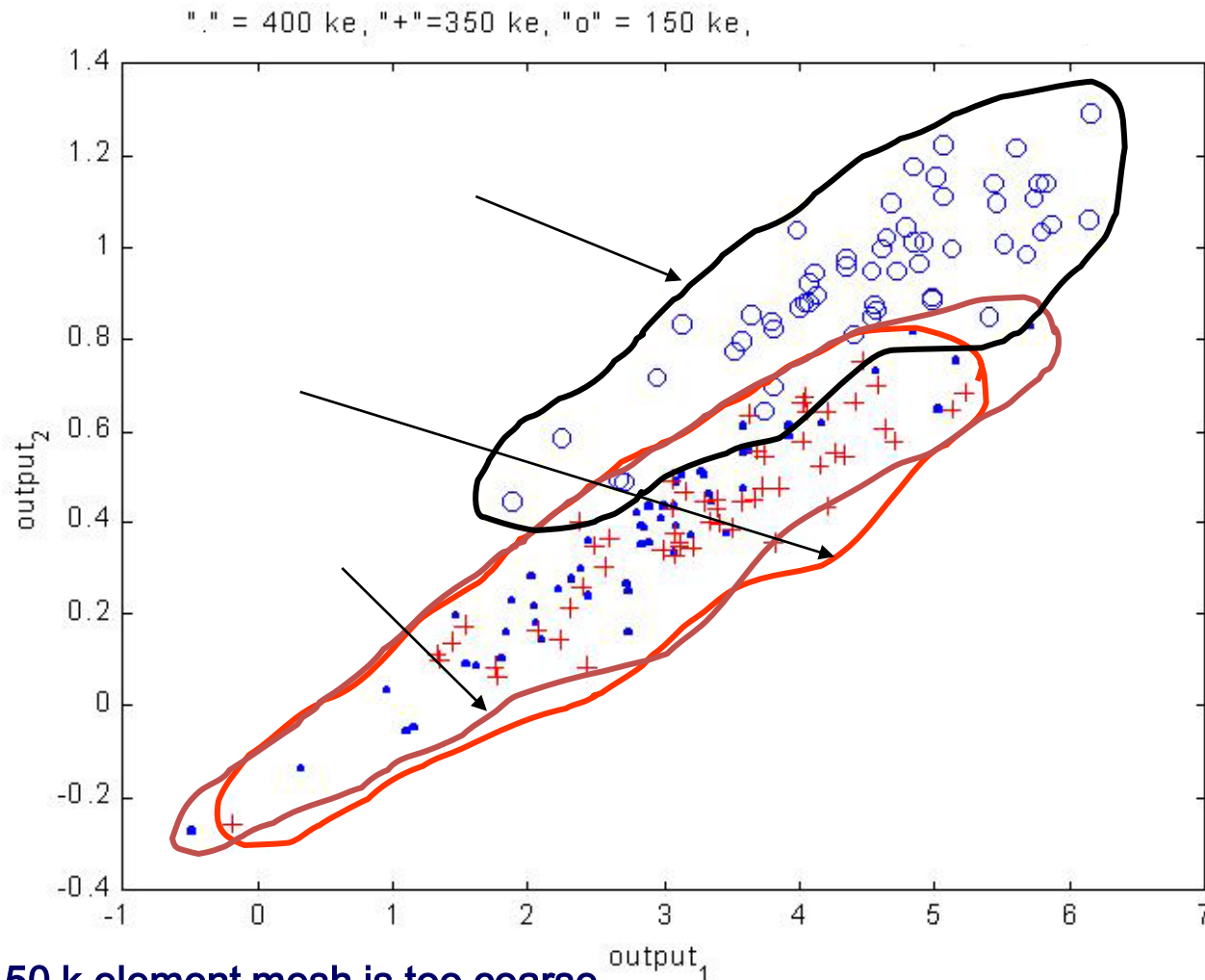
From a statistical point of view, the two codes are equivalent.

Must Analyses be Repeatable?



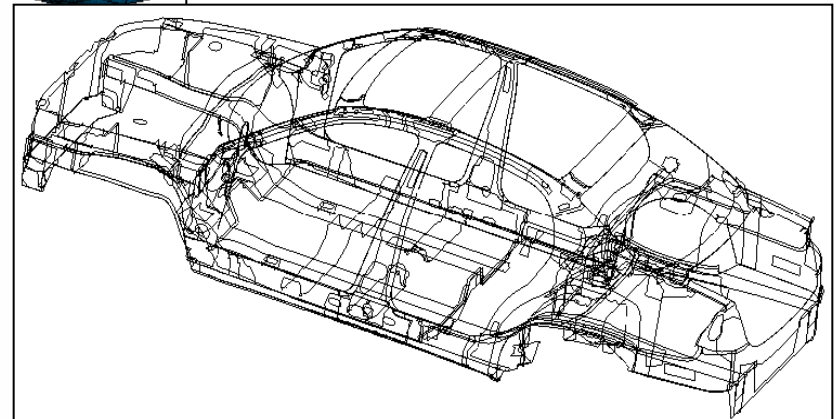
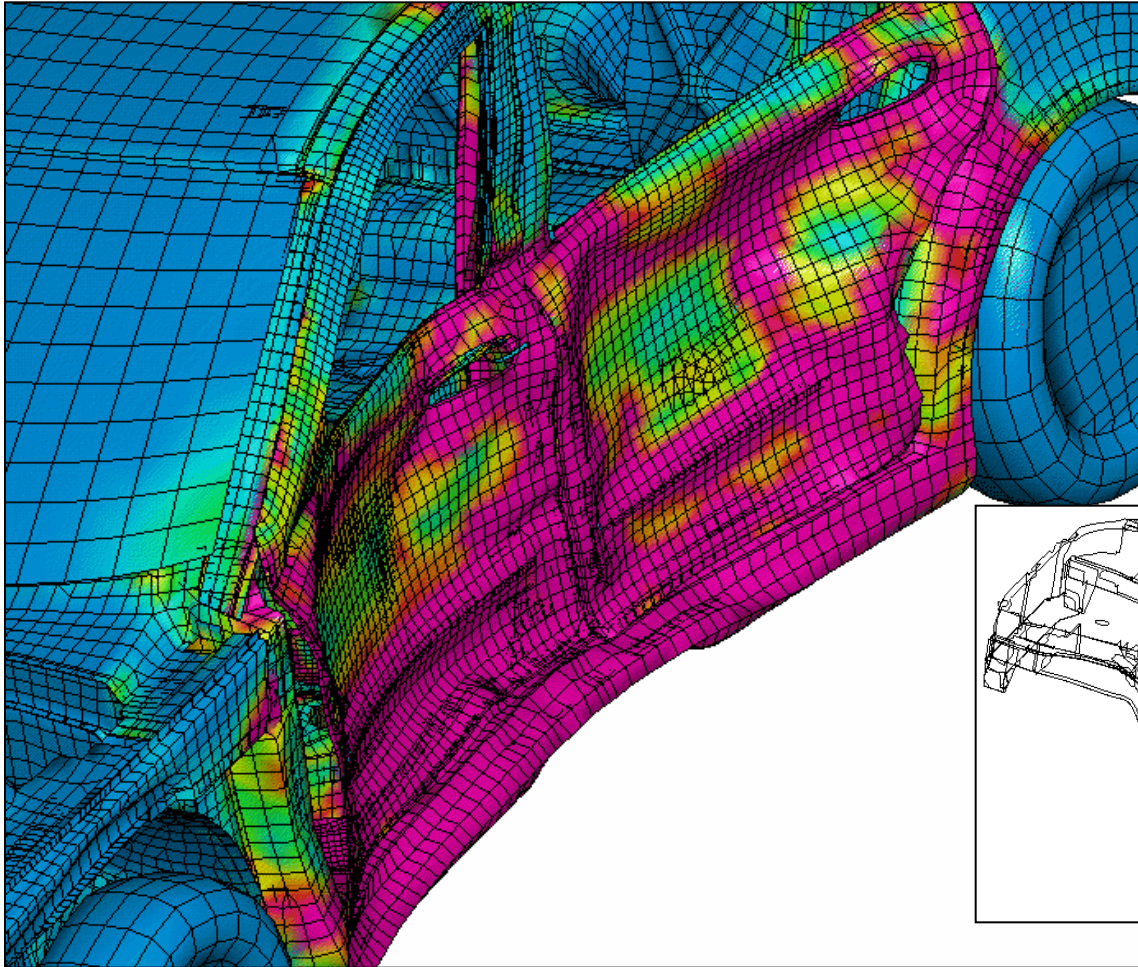
Given that from a statistical standpoint the meta-models are equivalent, the number of processors is irrelevant.

Models and number of elements

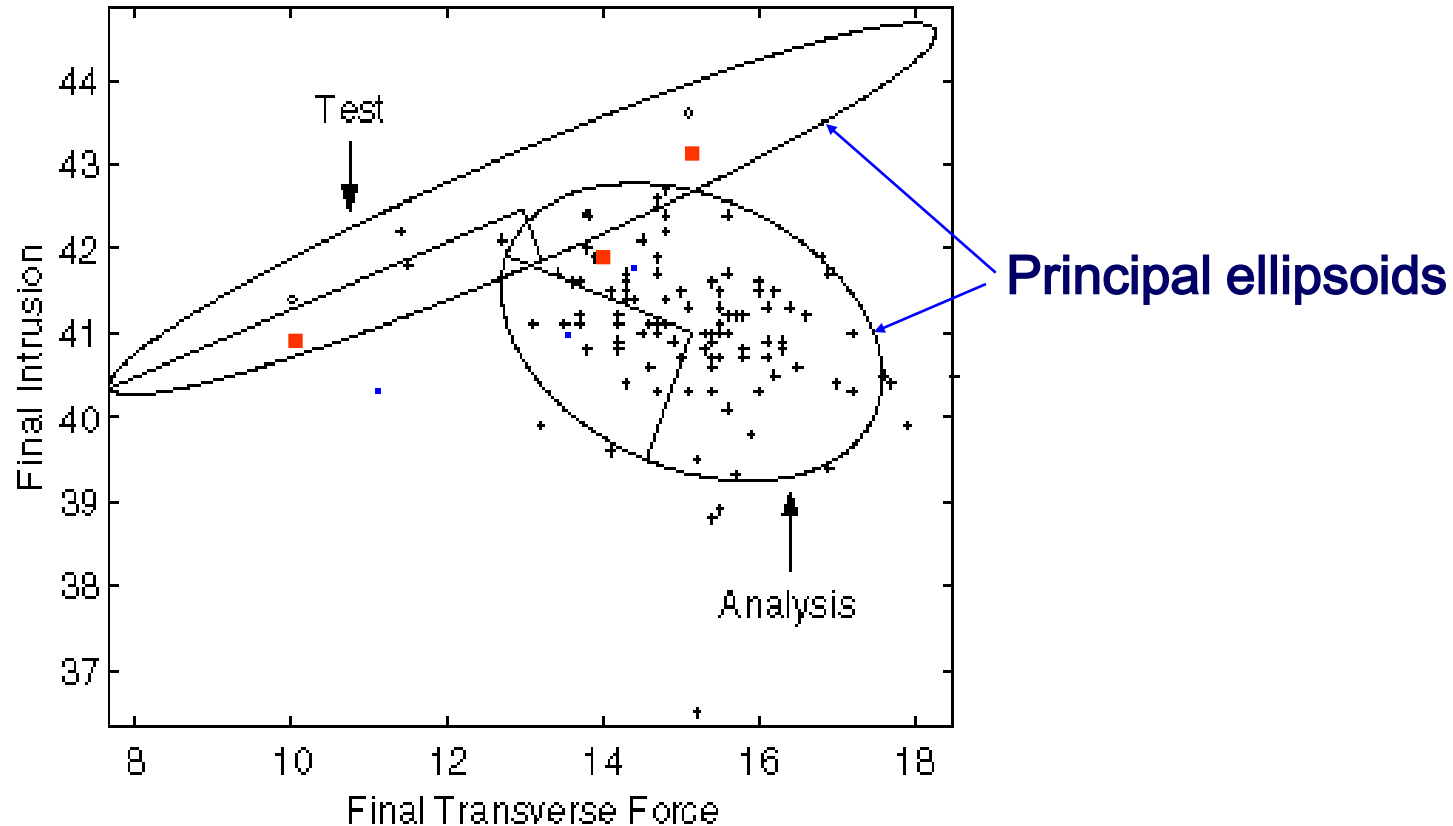


- 150 k element mesh is too coarse
- Other two meshes are essentially equivalent (i.e. no need for more than 350 k)
- Meshes of more than 350 k elements are too detailed

Model Validation - B-Pillar example



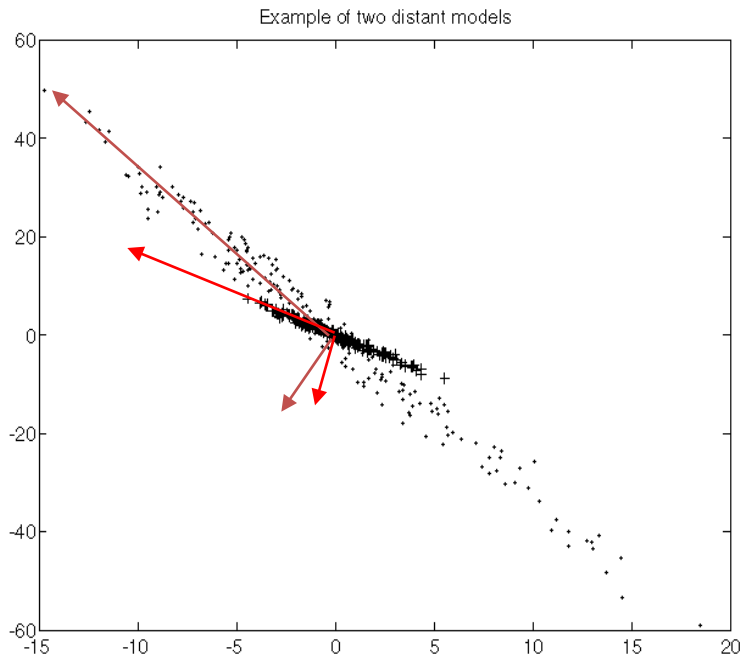
B-Pillar Model Validation



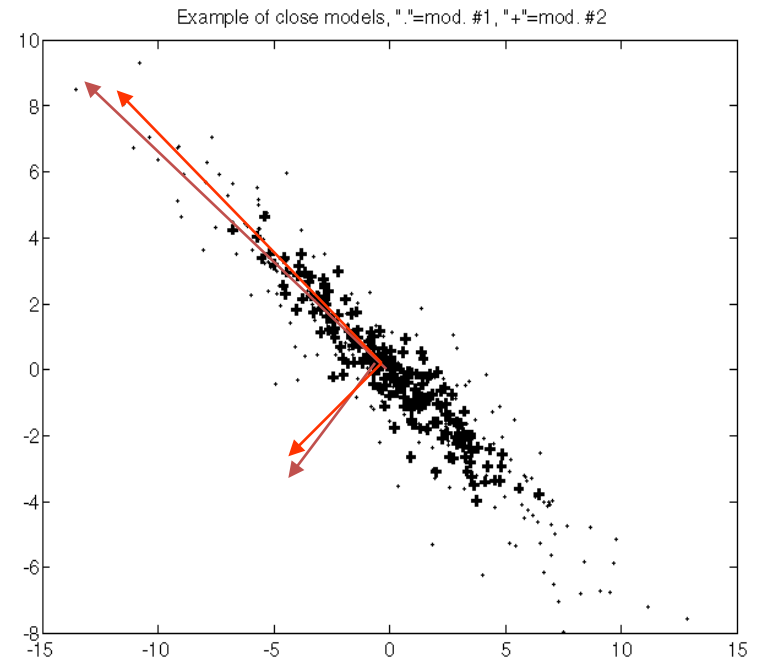
- The model, in its current configuration, is not valid.
- Three tests are insufficient to make any statements as to the model's validity.
- A single experiment cannot validate a model, it can merely verify it (or falsify it!).
- Validation requires multiple experiments and multiple calculations.

What Does Validation Really Mean

It is matching the covariance matrices of test and simulation meta-models



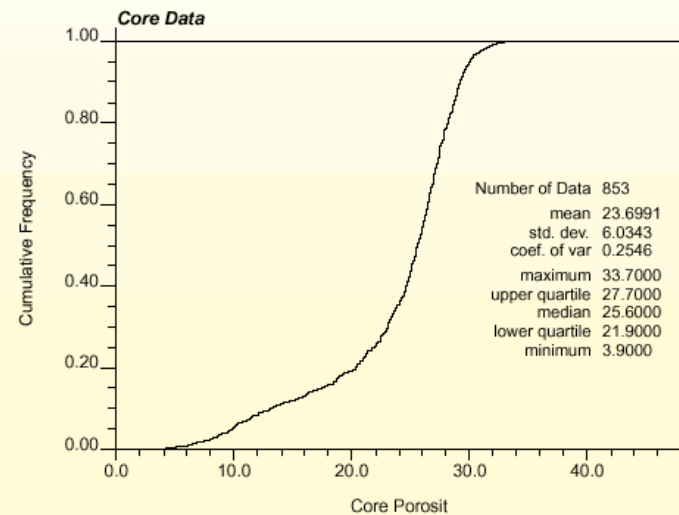
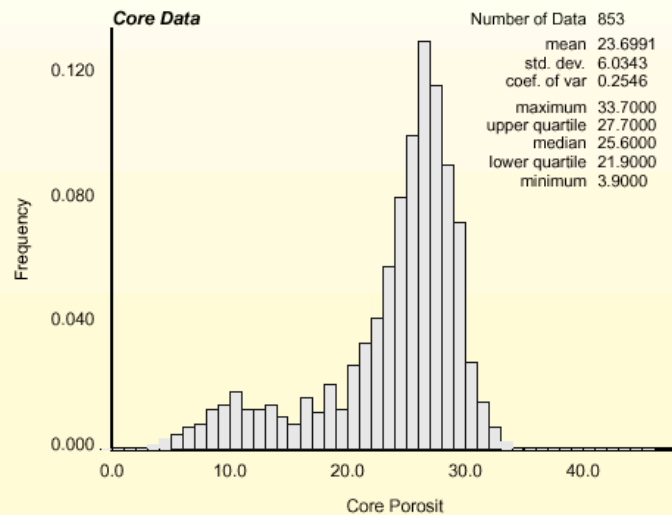
Means OK but differences in covariance and scatter



Means and covariance OK but not scatter (eigenvalues)

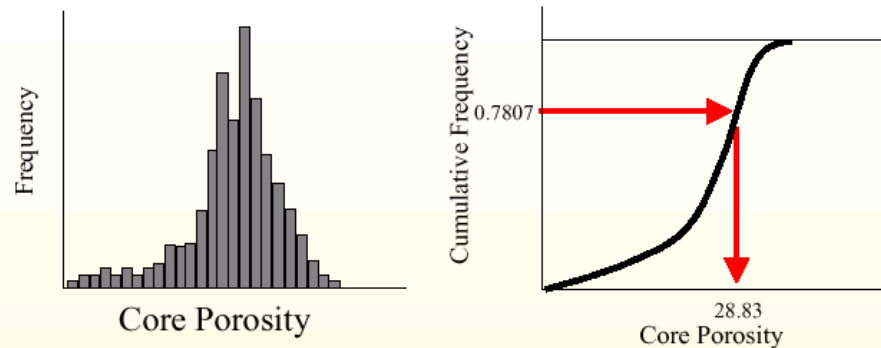
Monte Carlo Simulation

- Monte Carlo Simulation proceeds by reading quantiles from a cumulative distribution
- The procedure:
 - generate a random number between 0 and 1
 - read the quantile associated to that random number



Monte Carlo Simulation

Example: simulate core porosity from its cdf.



- Monte Carlo Simulation / Stochastic Simulation / Random Drawing proceed by reading quantiles from a cumulative distribution

The procedure:

- generate a random number between 0 and 1 (calculator, table, program, ...)
- read the quantile associated to that random number

For Example:

Random Number	Simulated Number
0.7807	28.83
0.1562	
0.6587	
0.8934	

...

Cumulative Distribution Function

- Cumulative distribution function cdf defined as:

$$F(z) = \text{Prob}\{Z \leq z\} \in [0,1]$$

This formula gives the area under the pdf of the RV Z , and is the probability that the RV Z is less than or equal to a threshold value of z .

- The probability of exceeding any of the threshold values of z can be written:

$$\text{Prob}\{Z > z\} = 1 - F(z)$$

- Properties of the cdf:
 - $F(z)$ non decreasing
 - $F(z) \in [0,1]$
 - $F(-\infty) = 0$ and $F(\infty) = 1$

SIMULATION-SUPPORTED ENGINEERING

Cumulative Distribution Function (CDF) and Probability Distribution Function (PDF)

- The probability of Z occurring in an interval from a to b (where $b > a$) is the difference in the cdf values evaluated at points b and a :

$$\text{Prob}\{Z \in [a, b]\} = F(b) - F(a)$$

- Probability density function (pdf) is the derivative of the cdf, if it is differentiable:

$$f(z) = F'(z) = \lim_{dz \rightarrow 0} \frac{F(z + dz) - F(z)}{dz}$$

- The cdf can be obtained from integrating the pdf:

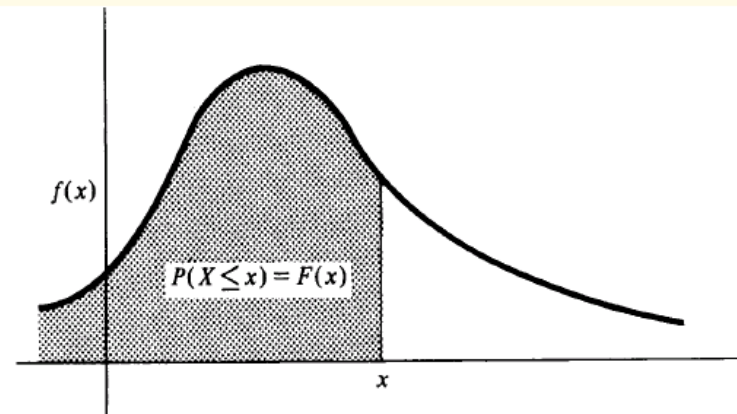
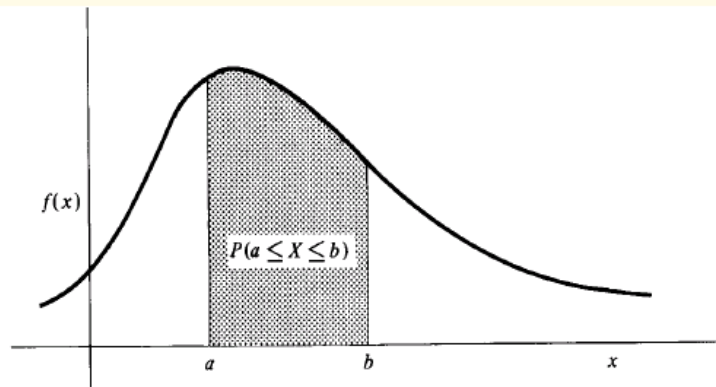
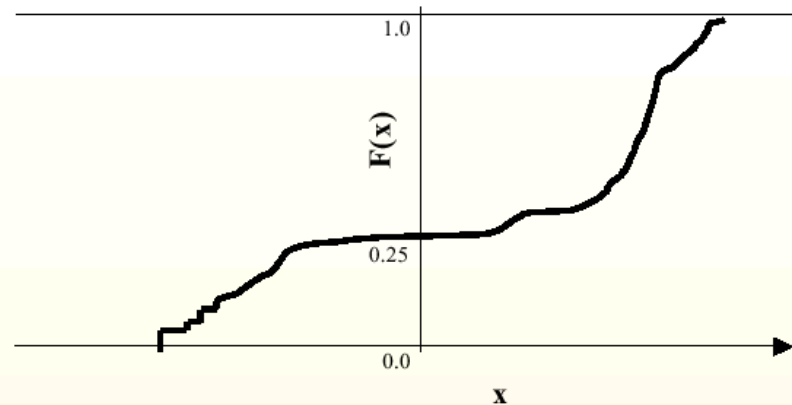
$$F(z) = \int_{-\infty}^z f(z) dz$$

CDF and PDF

- Properties of pdf:

$$f(z) \geq 0$$

$$\int_{-\infty}^{\infty} f(z) dz = 1$$



Where Does the PDF come from?

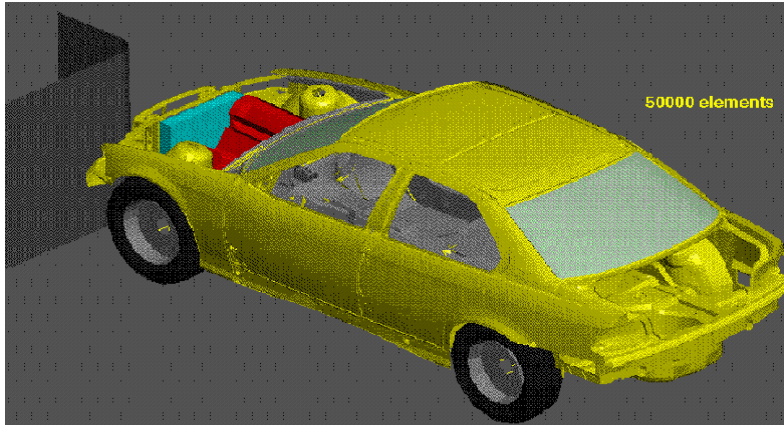
GOOD ENGINEERING

- **We know from experience that the world is not discrete**
- **Replace all discrete values with ranges and a distribution**

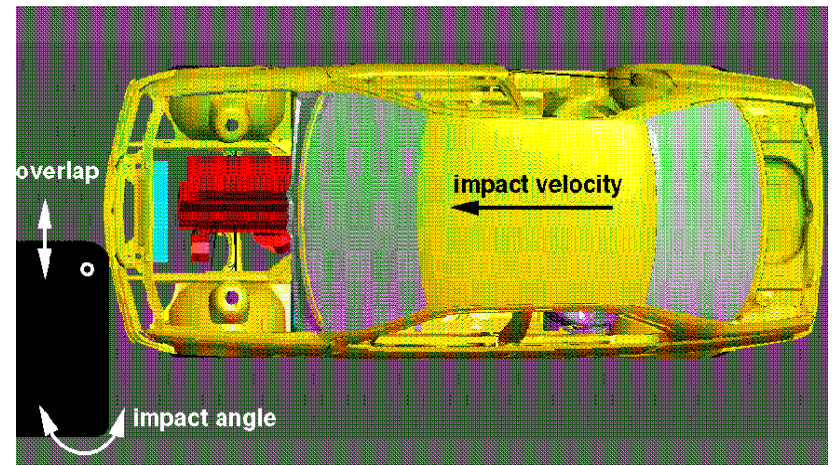
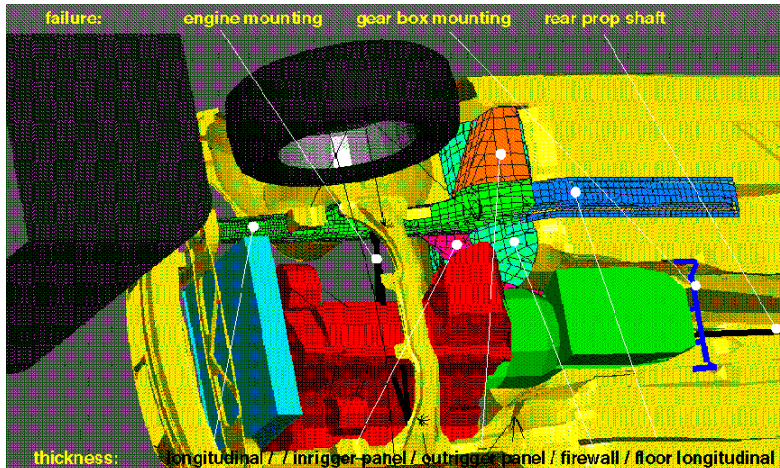
What is the real density of water?

First World-wide Stochastic Crash

(BMW-CASA, August 1997)



- Stochastic material properties, thicknesses and stiffnesses (70 variables), initial and boundary conditions (angle, velocity and offset).
- 128 Monte Carlo samples on Cray T3E/512 (Stuttgart Univ.)
- 1 week-end of execution time.



Method 1 – ESA-LFU Load-Coupled Dynamic Analysis

<i>Element/Material Type</i>	<i>Property</i>	<i>C.o.V. (σ/μ)</i>
Isotropic Material	Young's modulus	8%
	Poisson's Ratio	10%
	Shear modulus	12%
	Mass density	4%
Orthotropic Shell Element Material	Young's Modulus	8%
	Shear Modulus	12%
Solid Element An-Isotropic Material	Material Property	12%
	Matrix	4%
	Mass Density	
Simple Beam	Section dimension	5%
Layered Composite Material	Non-Structural Mass	8%
	Thickness of Plies	12%
	Orientation Fibre	1.5°
	Angle	
Spring Element	Stiffness	8%
Shell Element	Membrane thickness	4%
	Non-Structural Mass	
Concentrated Mass	Mass	3%
Damping	Modal Damping	40%
	Structural Damping	25%
# of Random Variables ≈ 1300		

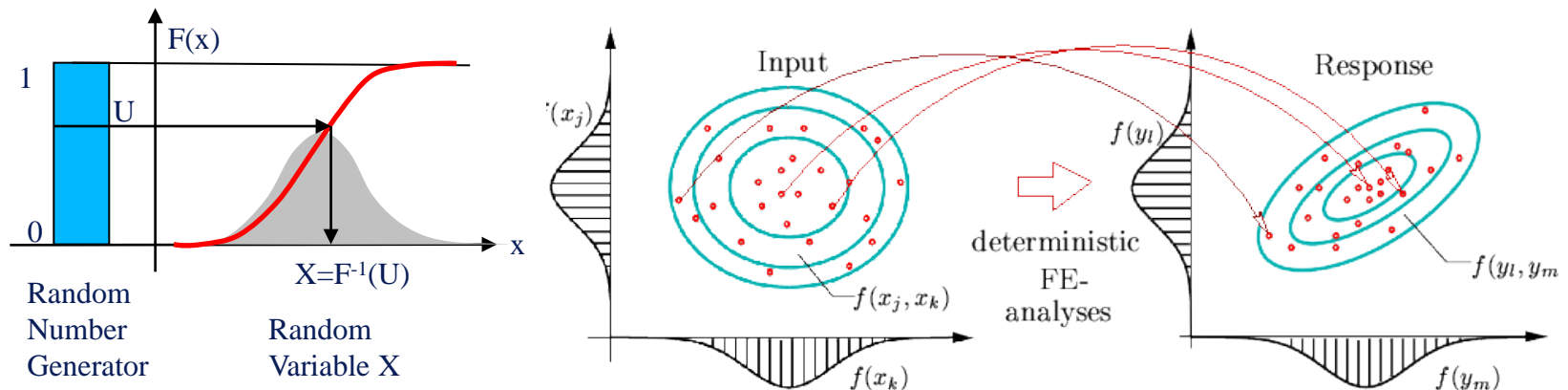
Gaussian

Log-Normal

Types of uncertainties: Material Properties, Geometrical Properties

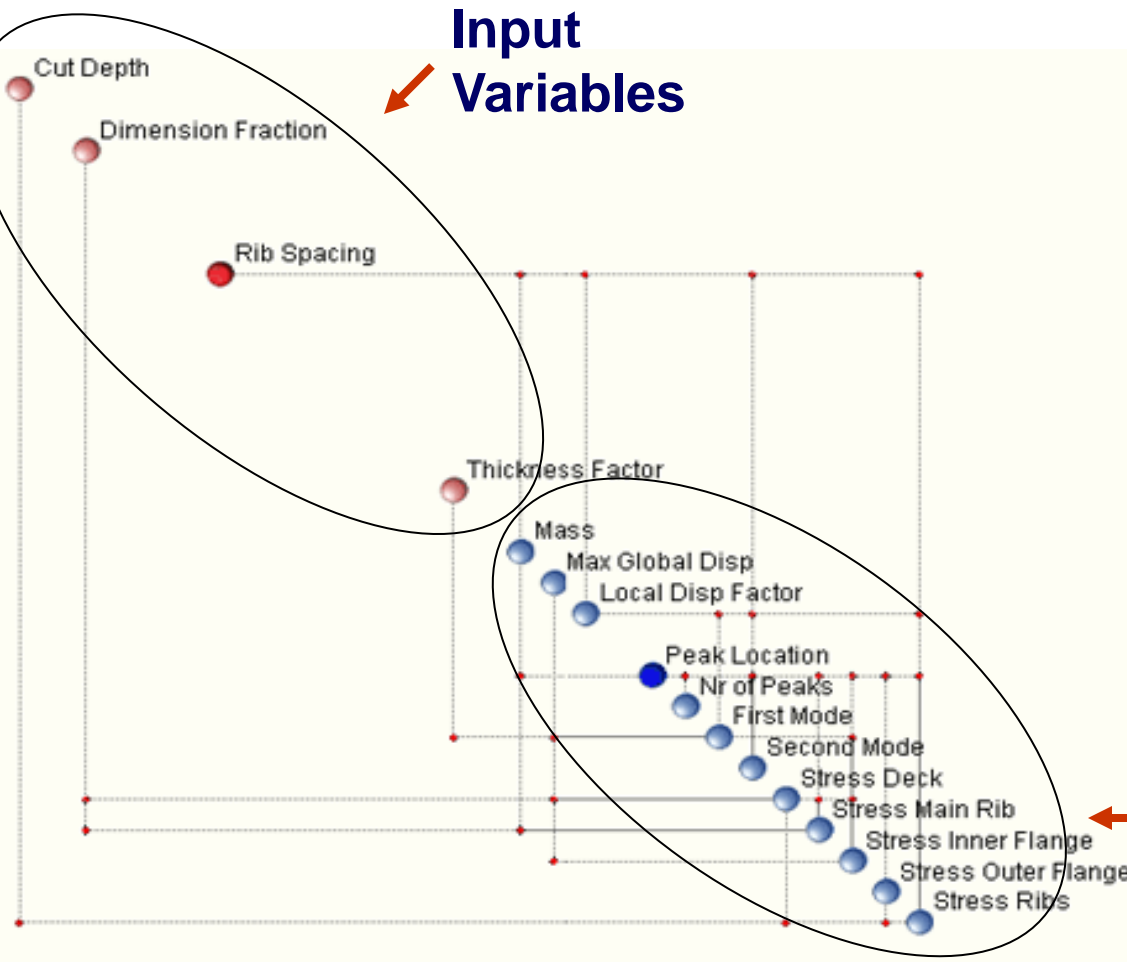
Efficient Monte Carlo Simulation

MCS is the most general and versatile method to process uncertainties



As few as 25-50 simulations provide information on the robustness and variability of the response due to uncertainties of the input parameters

Correlation Maps – Filter Complexity while Modeling Reality



Ranks input variables and output responses by correlation level

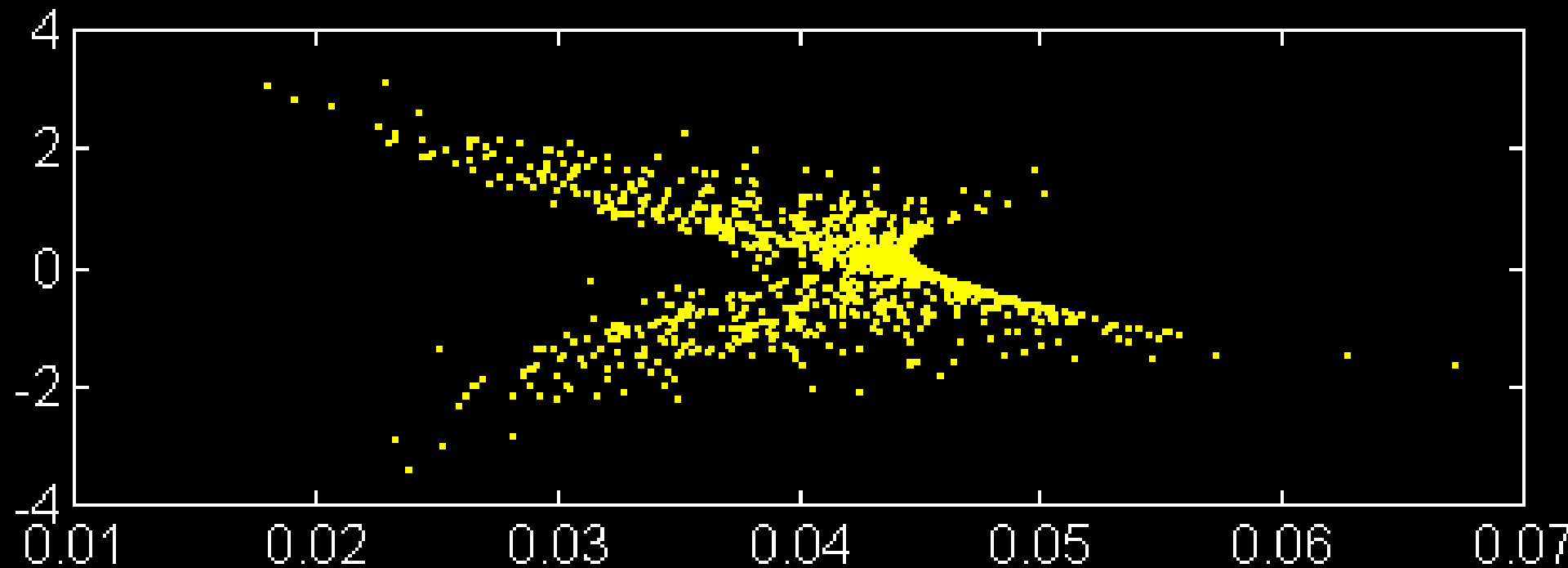
Follows MIT-developed Design Structure Matrix model format

Filters Variables Based on Correlation Level

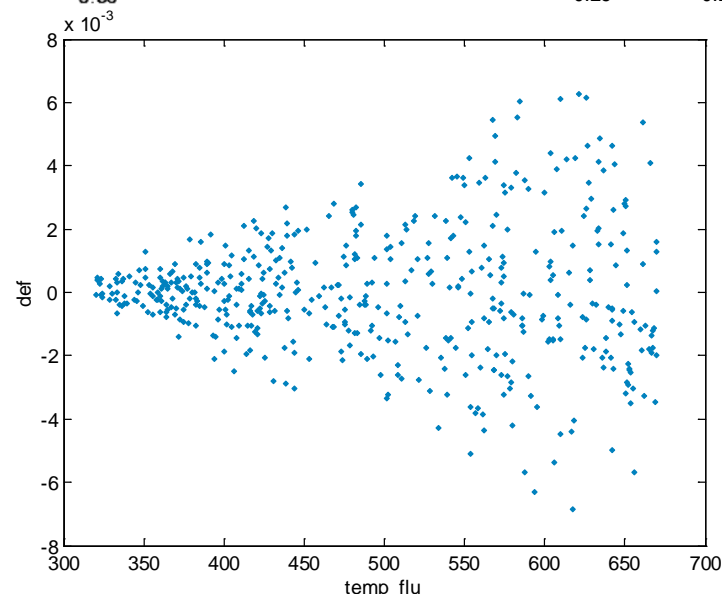
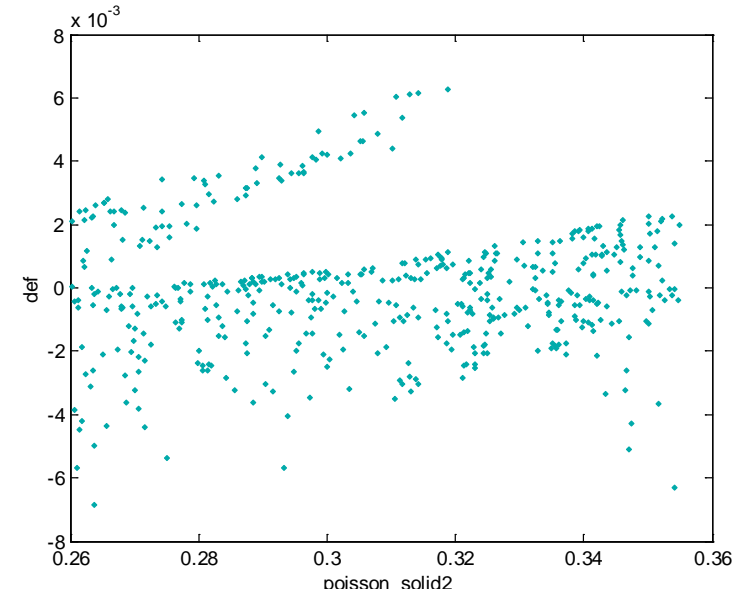
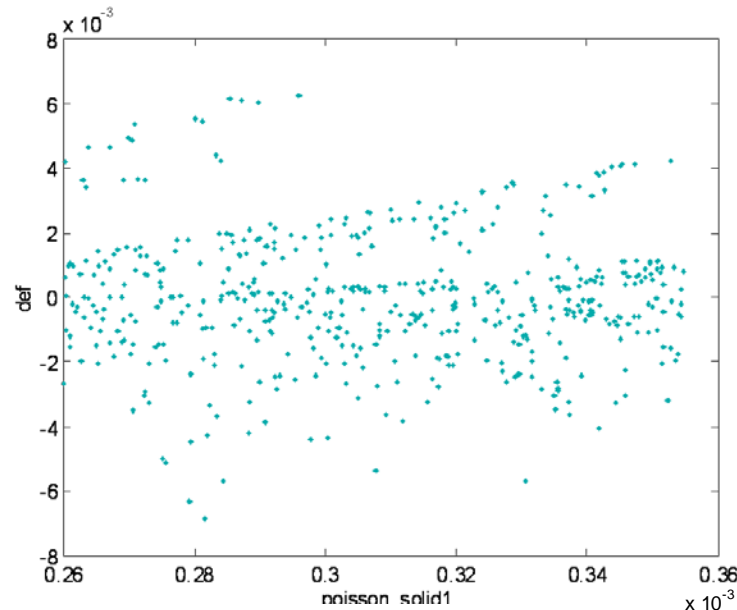
Understand How Things Work

Output Variables

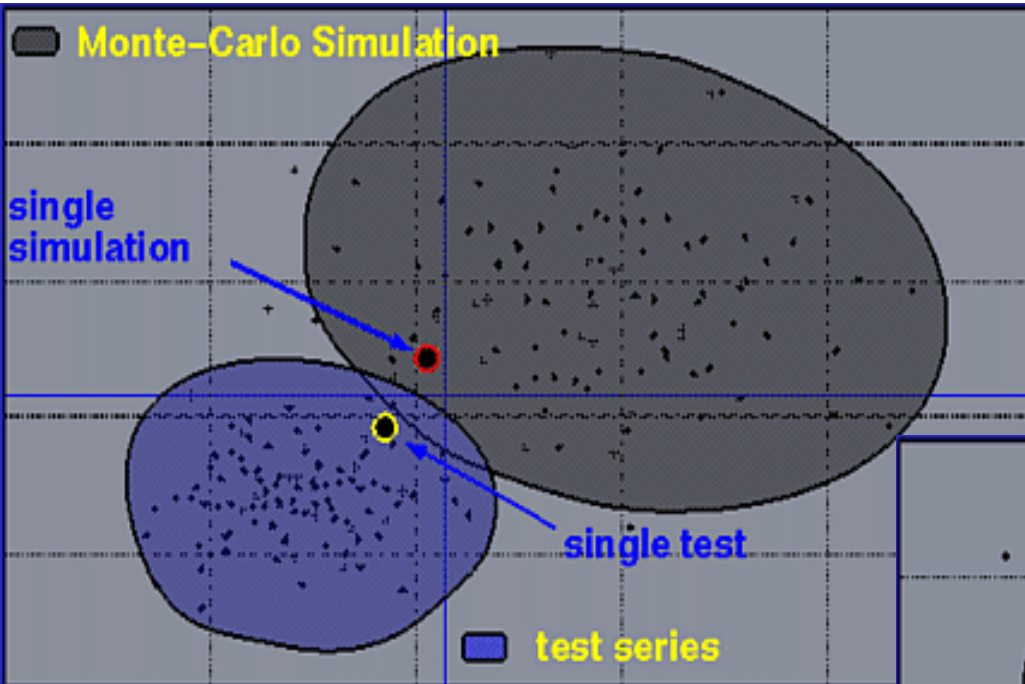
Design Exploration with Fitness Landscapes



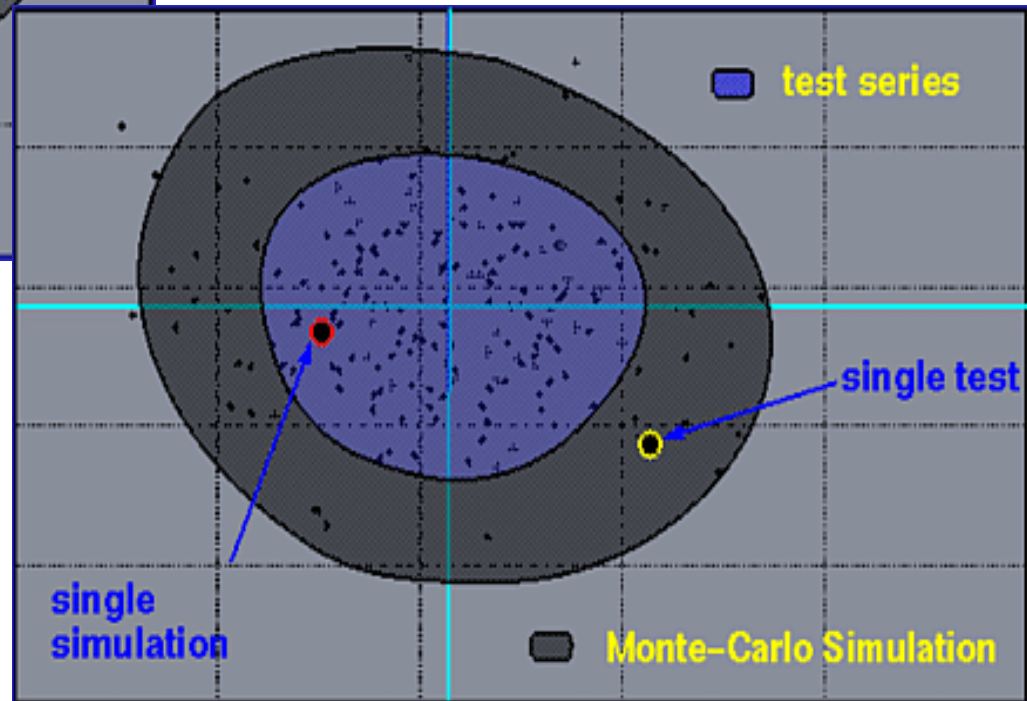
Design Exploration with Fitness Landscapes



Simulation Design Improvement



Validation of simulation models



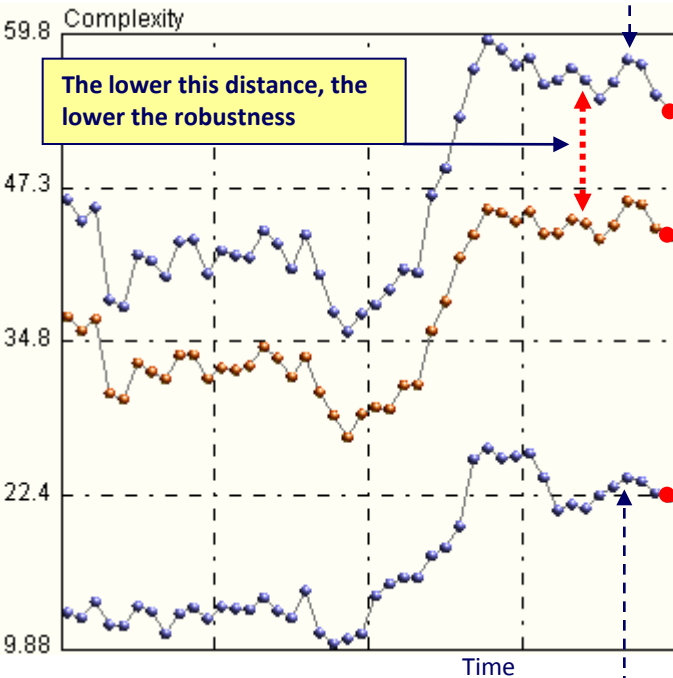
Courtesy of BMW AG

What is Complexity?

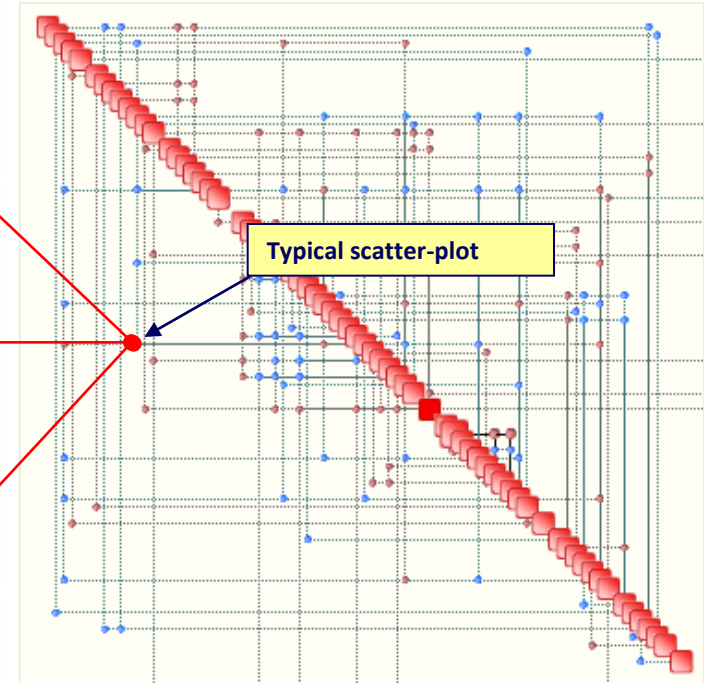
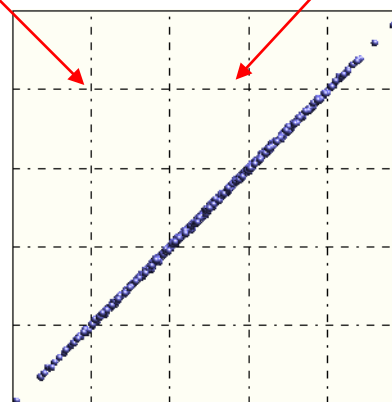
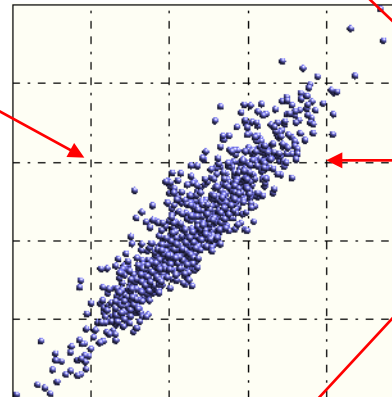
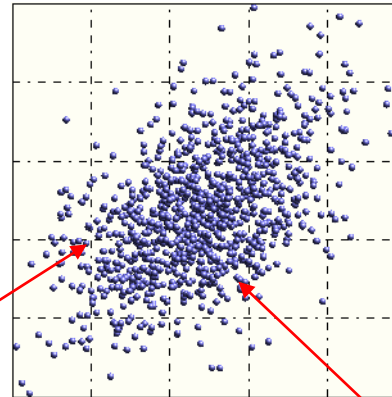
- Complexity is an **attribute** which characterizes every system, just like energy or momentum. It can be measured, and therefore managed.
- However, complexity cannot grow indefinitely and has a maximum. Close to this maximum, called **critical complexity**, the system becomes fragile and vulnerable.
- Critically complex systems are very difficult to manage and can easily run out of hand.
- The **risk exposure** of any dynamical system can be measured and understood in an innovative way via complexity.

Complexity and Robustness

Upper Critical Complexity
Catastrophic collapse



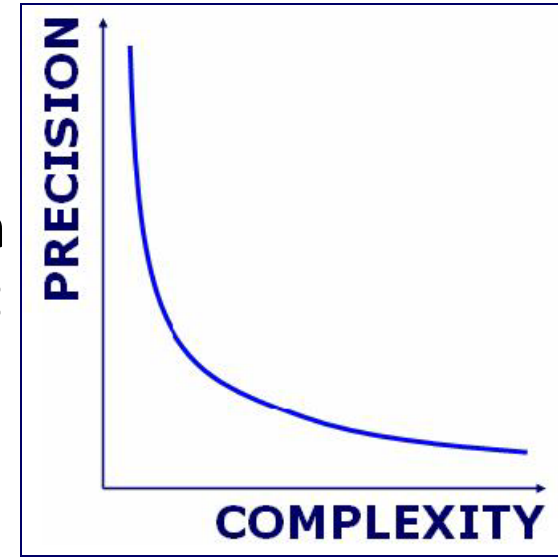
Lower Critical Complexity
System is deterministic



Systems close to their upper critical complexity are less robust as numerous links between variables are weak (fuzzy) and are close to breaking and losing functionality.

Complexity Principles

- **Principle of Complexity:**
When the complexity and uncertainty of an engineering system increase, our ability to predict its behavior diminishes until a threshold is reached beyond which accuracy and significance become almost mutually exclusive.
- **Principle of Incompatibility:**
High precision is incompatible with high complexity.



L. Zadeh, UCLA

Complexity x Uncertainty = Fragility

- When uncertainty meets high complexity, the result is **fragility**. Simple systems cope better with uncertainty than highly complex systems.
- Highly complex systems are more exposed to the effects of uncertainty because of the countless ways they can process information. They can **fail in many ways**, often due to apparently innocent causes.
- Uncertainty in the environment cannot be avoided. We must learn to live with it. Hence the need to manage complexity.
- Fragility is a prelude to risk, **holistic risk management** can be accomplished via complexity management.



Complexity x Uncertainty = Fragility

$$C_{\text{design}} \times (U_{\text{manufacturing}} + U_{\text{environment}}) = F_{\text{product}}$$

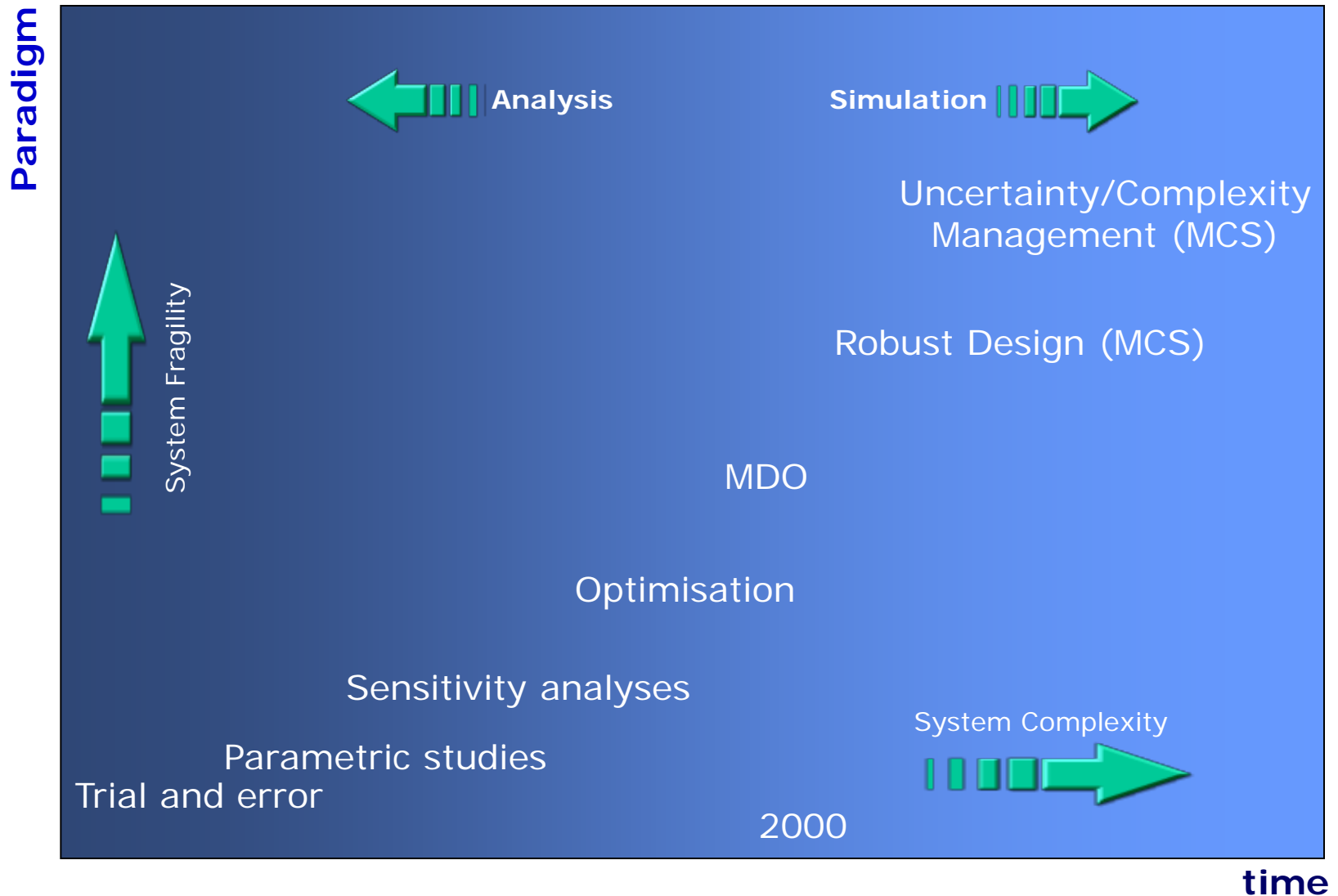
- A highly sophisticated design will result in a fragile product if:
 - The manufacturing process is of poor quality
 - The environment is very “turbulent”
- Hence, a more robust product requires:
 - A high-quality manufacturing process, or
 - A less severe environment in which to function, or
 - A less “ambitious” initial design

Complexity-Based Design

A less complex solution is generally:

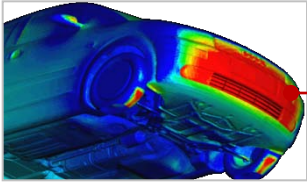
- **Less expensive to design and engineer**
- **Less expensive to manufacture**
- **Less expensive to service (replace broken components, etc.)**
- **Cheaper**
- **Easier to operate**
- **Less fragile. This means:**
 - **Less warranty costs**
 - **Less recalls**
 - **Less law-suits**

Evolution of CAE Paradigms

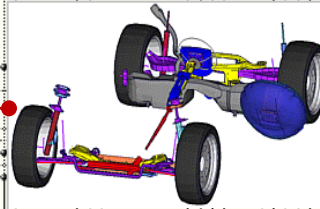


Holistic CAE

Aerodynamics



Power & Transmission



NVH & handling

Safety



Crashworthiness



Process Maps which gives users an integrated and holistic view of:

- Interaction between disciplines
- Degrees of coupling
- Critical variables
- Global robustness measures
- Failure modes
- Complexity

Compute power should be invested in getting the big picture and not in hair-splitting.

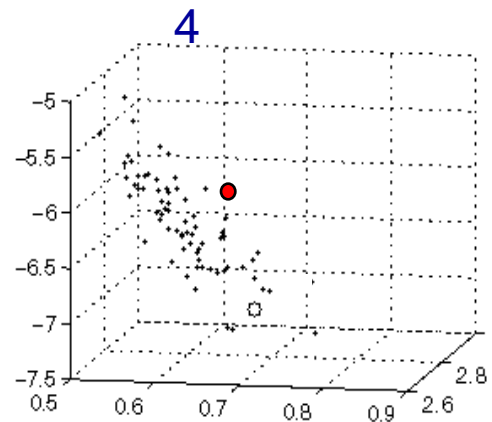
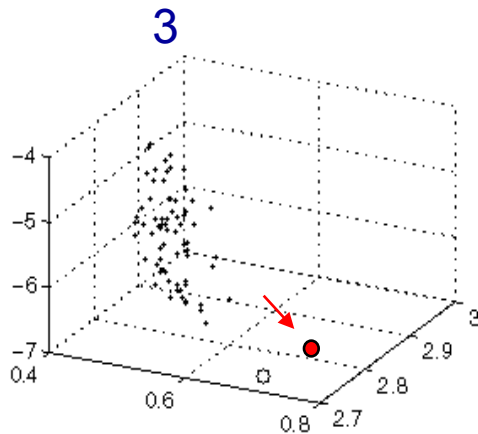
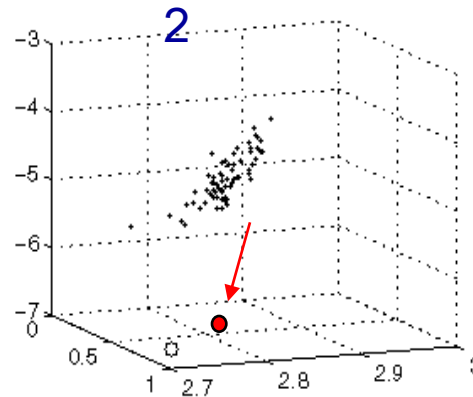
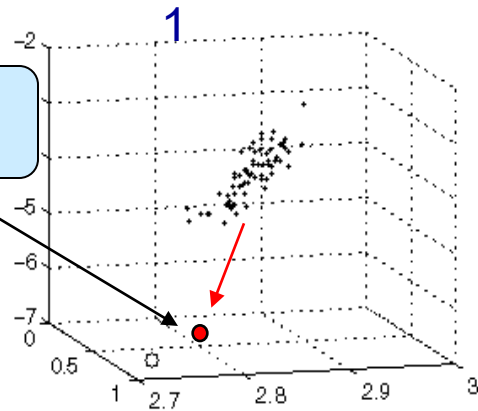
Future Trends in CAE

- No surrogates – FE Models are already surrogates. Why work with models of models?
- Move from (slow & expensive) pursuit of optimal solutions to (fast & cheap) identification of **acceptable compromises**.
- Go **holistic**: Less local details more global patterns – Nature works like that!
- Measure **robustness**.
- Measure **model credibility** – the success of CAE hinges on it!

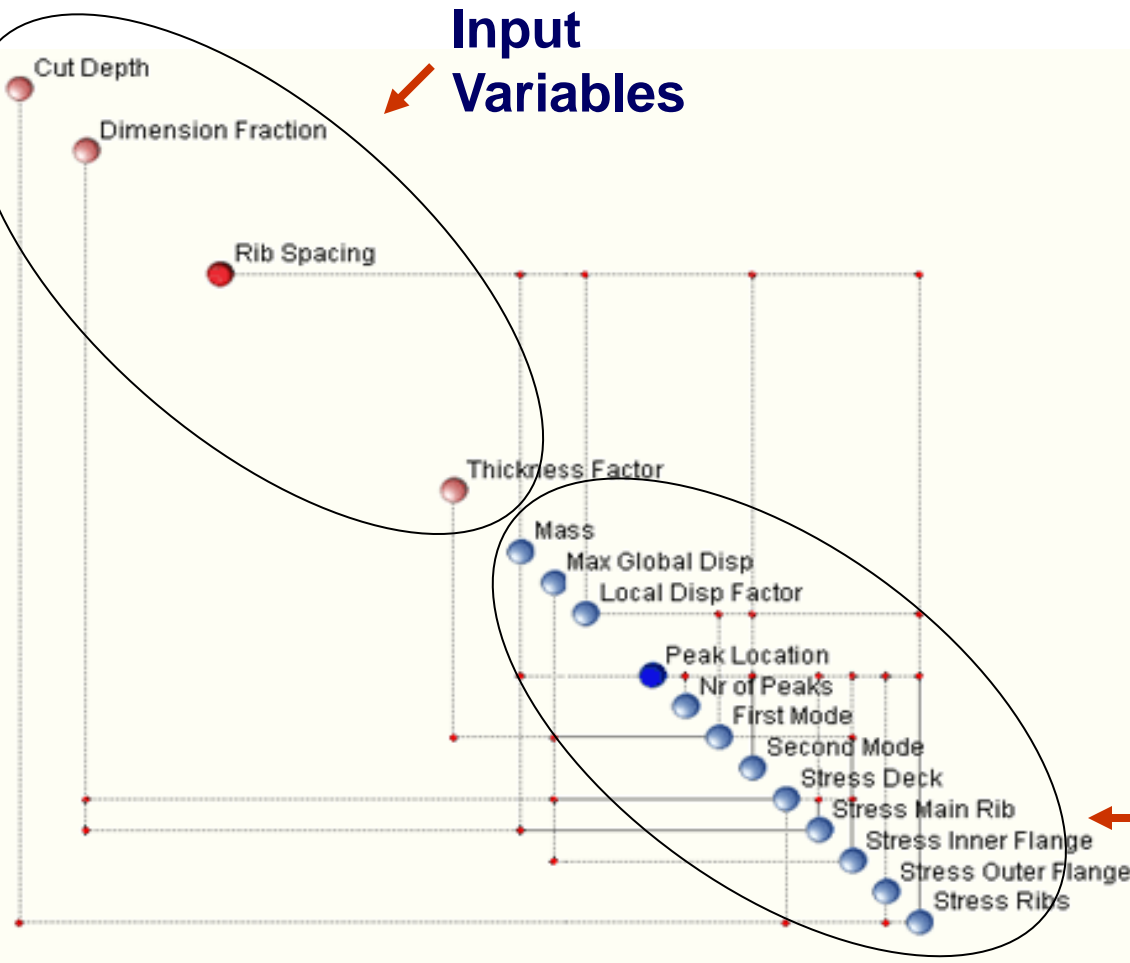
Simulation Design Improvement Process – march cloud to target

Iteration

Target
Performance



Correlation Maps – Filter Complexity while Modeling Reality



Ranks input variables and output responses by correlation level

Follows MIT-developed Design Structure Matrix model format

Filters Variables Based on Correlation Level

Understand How Things Work

Output Variables

Correlation Maps: Tools for Understanding

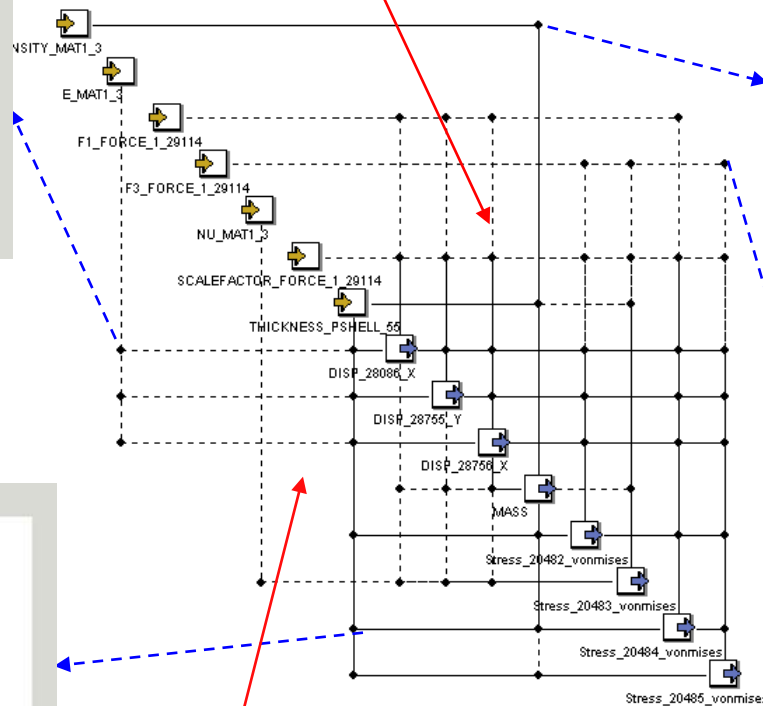
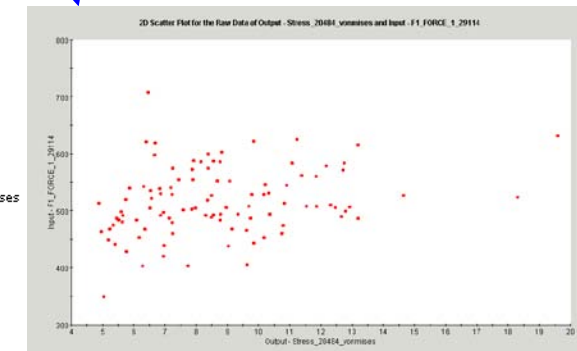
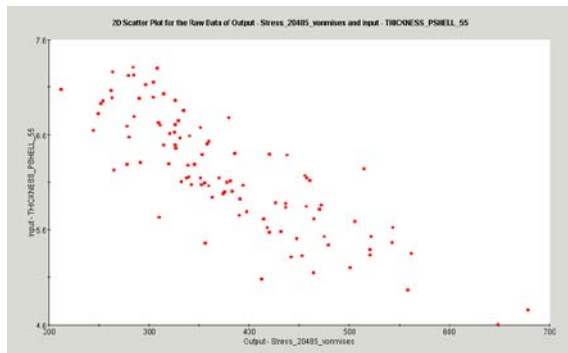
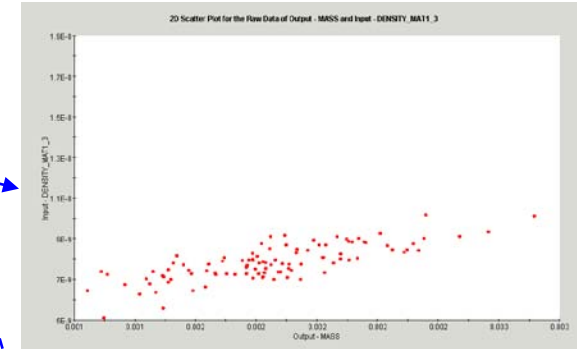
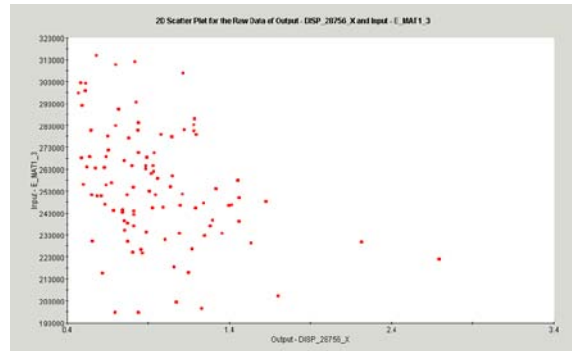
- Displays condensed information from hundreds of analysis runs.
- **Correlation Map = Structured Information = Knowledge**
- A Correlation Map helps an engineer:
 - **Understand** how a system works.
 - How information flows within the system.
 - how variables and components correlate.
 - **Make decisions** on how a design may be improved.
 - Identify dominant design variables.
 - Use as input for stochastic design improvement.
 - Find the **weak points** in a system.
 - Find **redundancies** in a design.
 - Identify **rules** that govern the performance (“if A and B then C”).

There are NO algorithms to learn. The engineer concentrates on engineering, not on numerical analysis.

A Correlation Map

Upper right –
positive correlation

Lower left –
negative correlation



Correlation

- **Correlation supersedes sensitivity.**
- **Correlation** between two variables **expresses the strength of the relationship** between these variables **while taking account of the scatter in ALL the other variables** in the system.
- It is possible to compute correlations between any pair of variables (input-output, output-output, etc., where input is a design or noise variable, and output is a performance, like stress or frequency).
- **Knowledge of the correlations in a system is equivalent to understanding how that system works.**

Pearson and Spearman Correlation

The Pearson, or linear correlation is given by:

$$r_{XY} = \frac{\sum_{k=1}^N (X_k - \bar{X})(Y_k - \bar{Y})}{\sqrt{\sum_{k=1}^N (X_k - \bar{X})^2} \sqrt{\sum_{k=1}^N (Y_k - \bar{Y})^2}},$$

The Spearman, or rank correlation is given by:

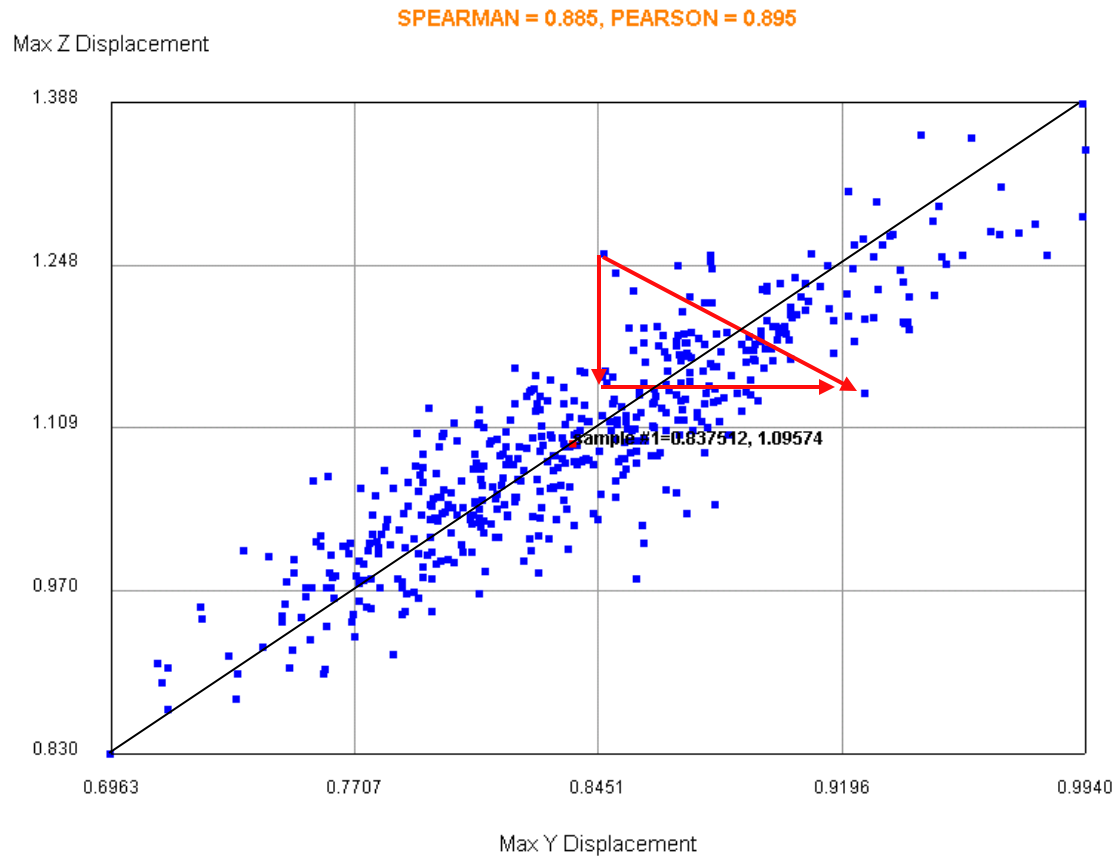
$$s_{XY} = \frac{\sum_{k=1}^N (R_k - \bar{R})(S_k - \bar{S})}{\sqrt{\sum_{k=1}^N (R_k - \bar{R})^2} \sqrt{\sum_{k=1}^N (S_k - \bar{S})^2}},$$

In the Spearman correlation, variable values are replaced with the corresponding ranks.

Correlation

- **Positive.** When one variable increases the other increases too.
- **Negative.** When one variable increases, the other decreases.
- **Linear** Correlation (or Pearson correlation) – means that scatter plot (also known as ant-hill plot) is “cigar shaped” (elliptical).
- **Non-linear** Correlation (or Spearman correlation) – means that scatter plot is irregular (e.g. has clusters).
- If the Spearman and Pearson correlations are not similar in terms of magnitude, then you can be sure that the input-output transfer properties of a system are non-linear.

Correlation

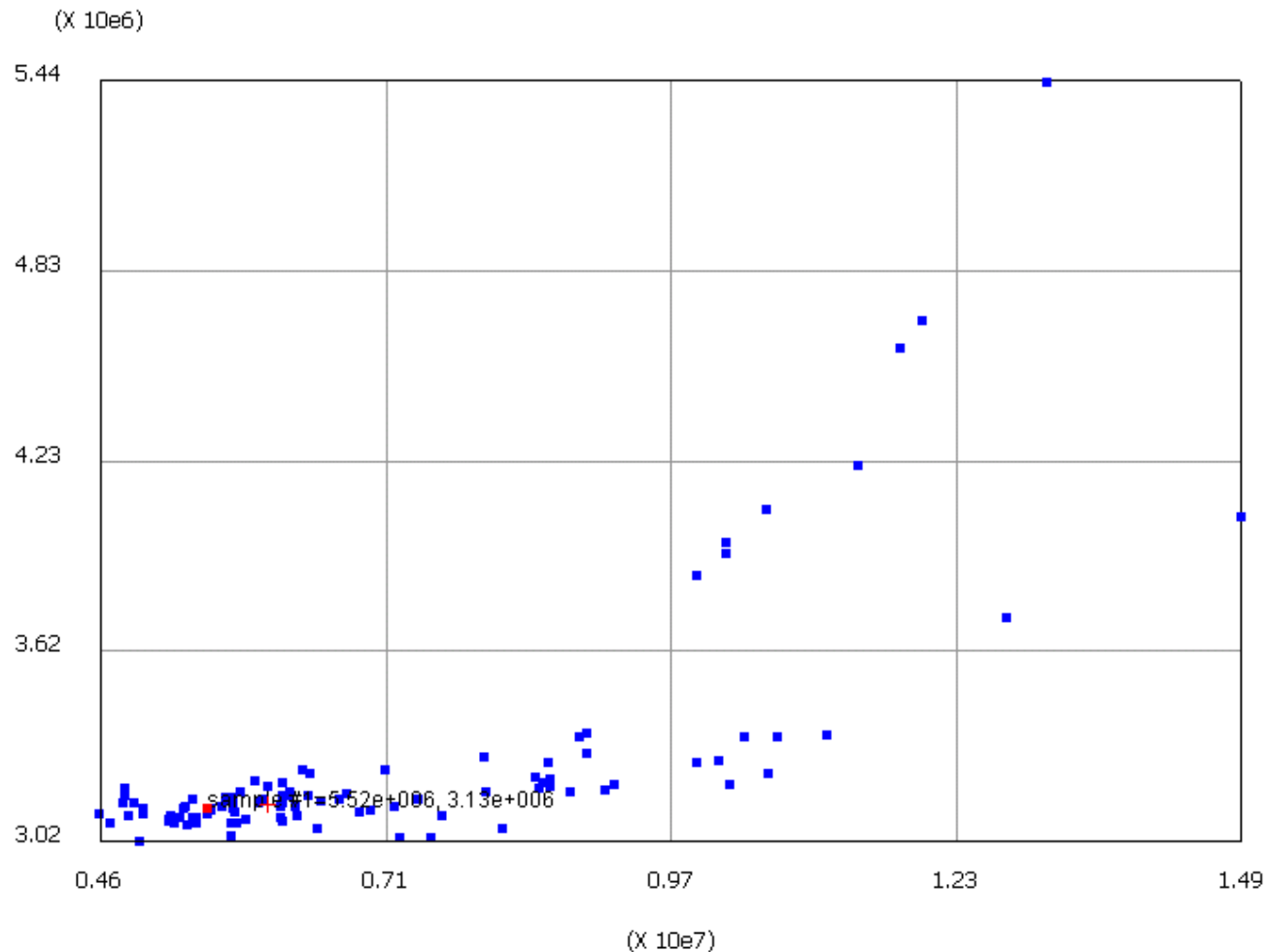


- A large value of correlation doesn't guarantee that a variable will increase if the other increases by a small amount - (as in the above case).
- A correlation is only an indication of a general trend, that can be verified only over large intervals.
- Handle with care!

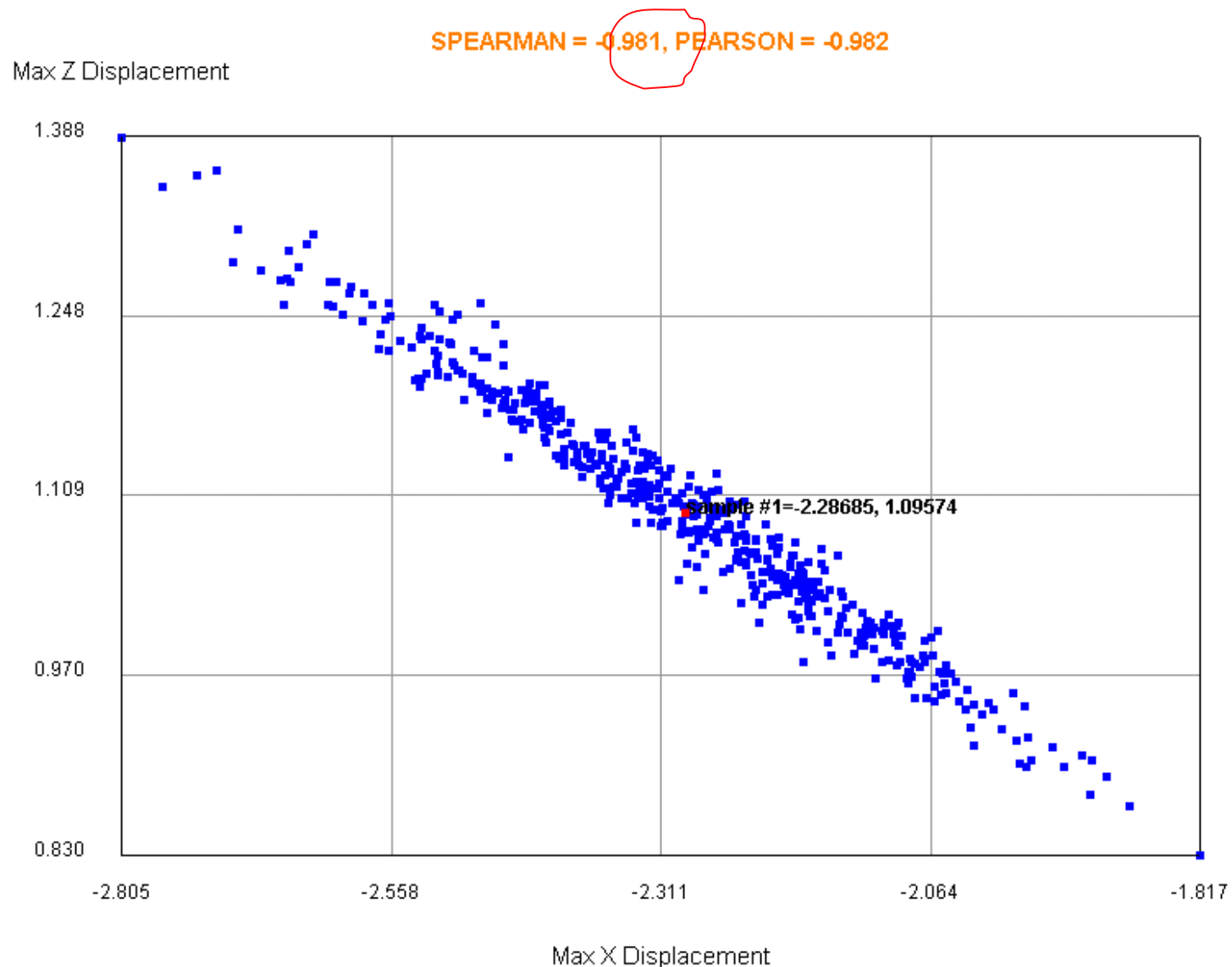
Non-linear Correlation

Non-linear corr.= 0.706, Linear corr.= 0.728

SPC Forces Max Y Component



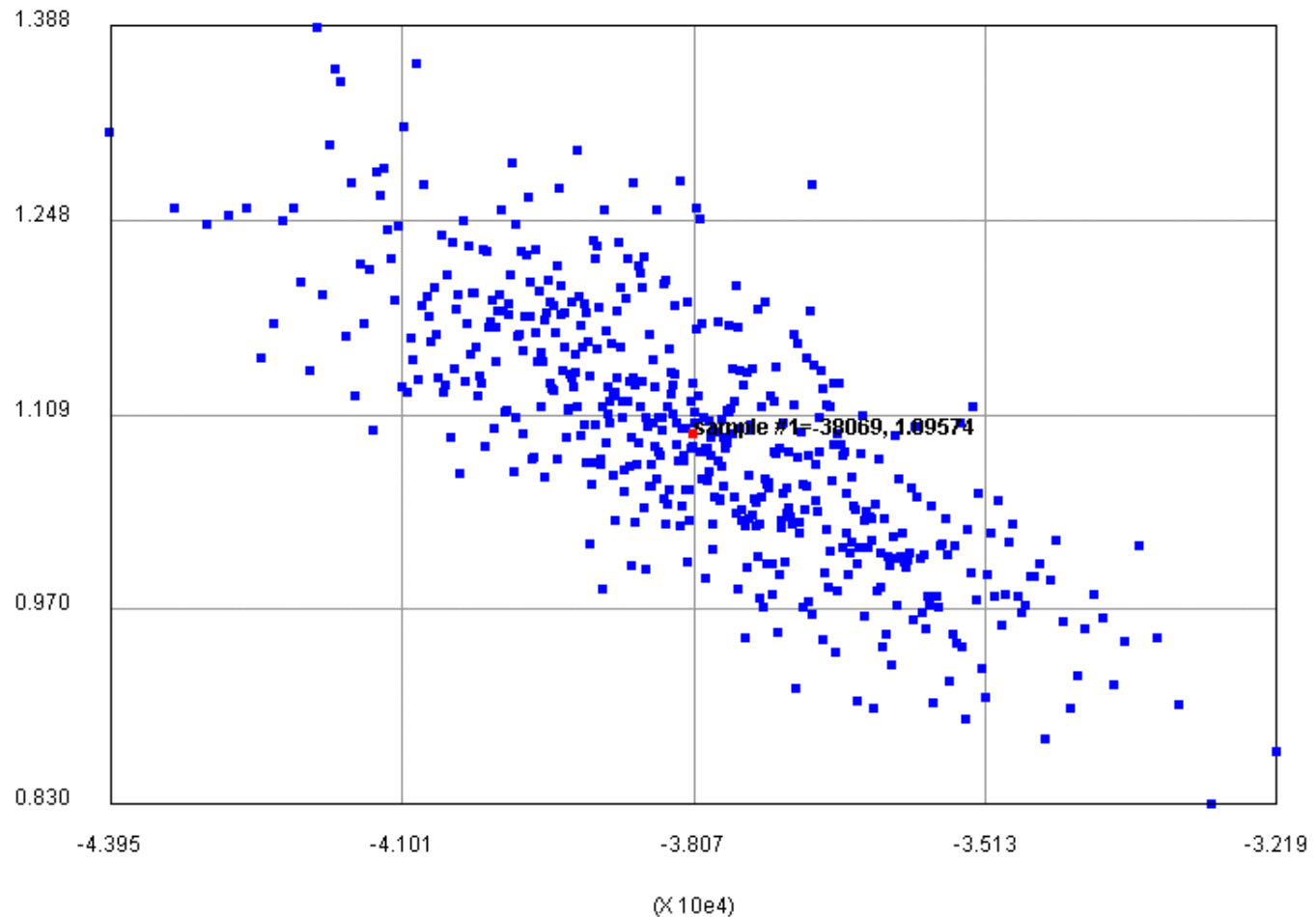
Large Negative (Linear) Correlation



Medium Negative Correlation

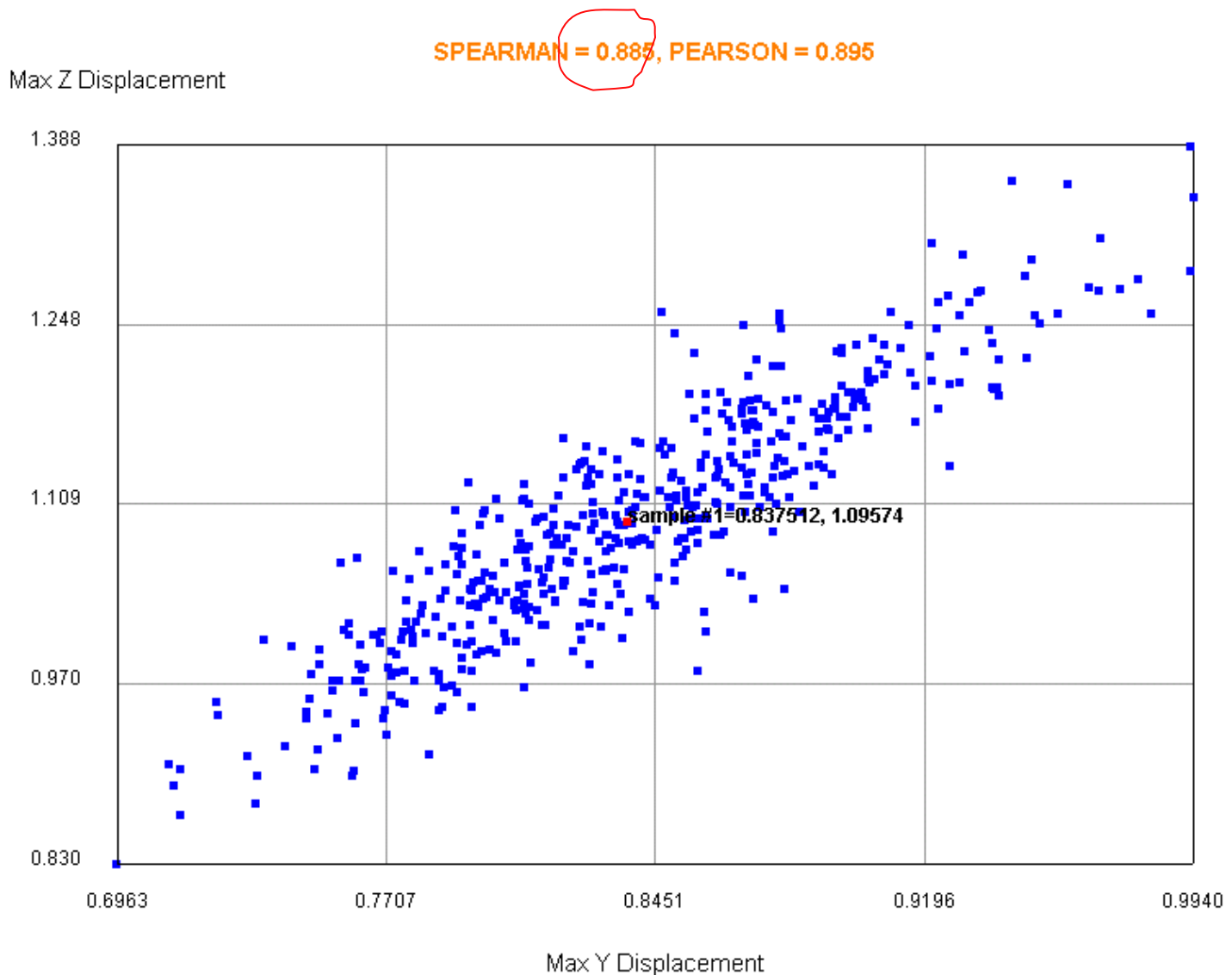
SPEARMAN = -0.771, PEARSON = -0.772

Max Z Displacement



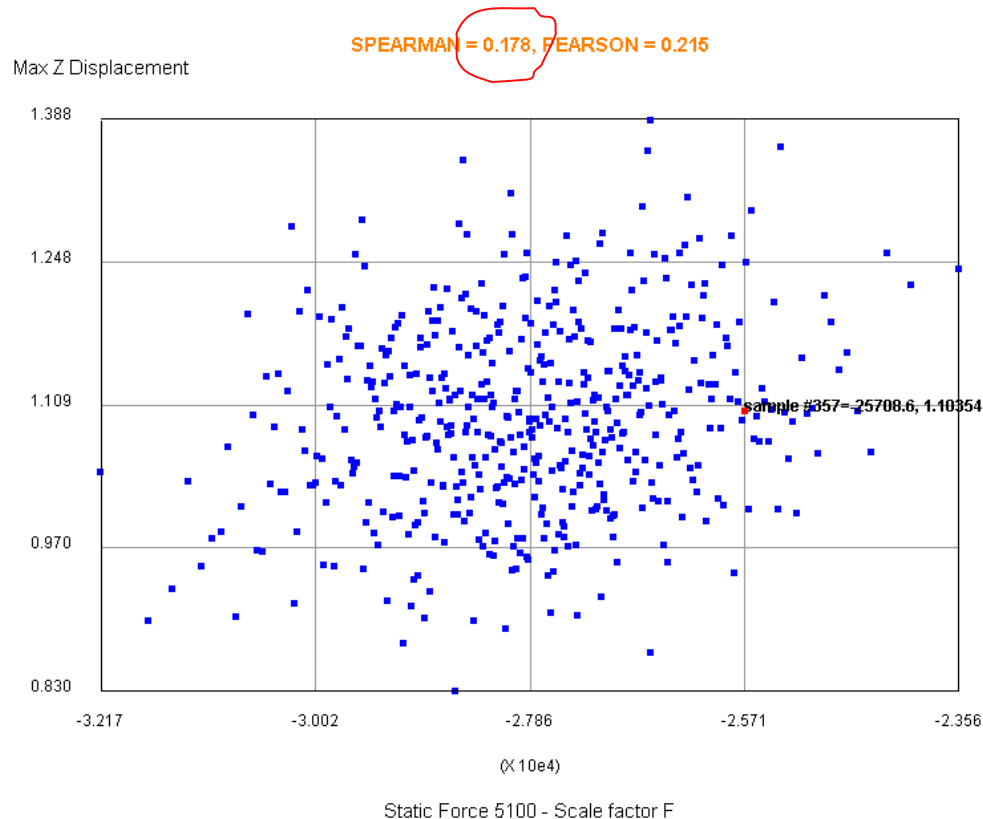
Static Force 4004 - Scale factor F

Large Positive Correlation



Correlation

- Correlation values below 0.5 may be neglected, as they represent meaningless (chaotic) relationships between variables. In these cases, the scatter in the other variables masks the relationship between the two in question.

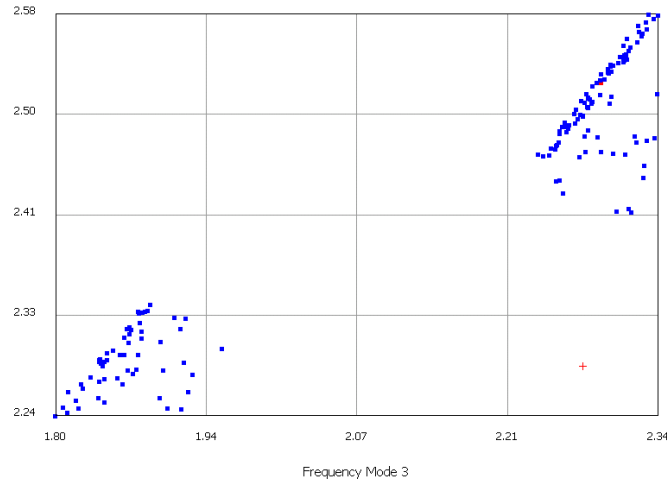


Clustering (Bifurcations)

SPEARMAN = 0.526, PEARSON = 0.366

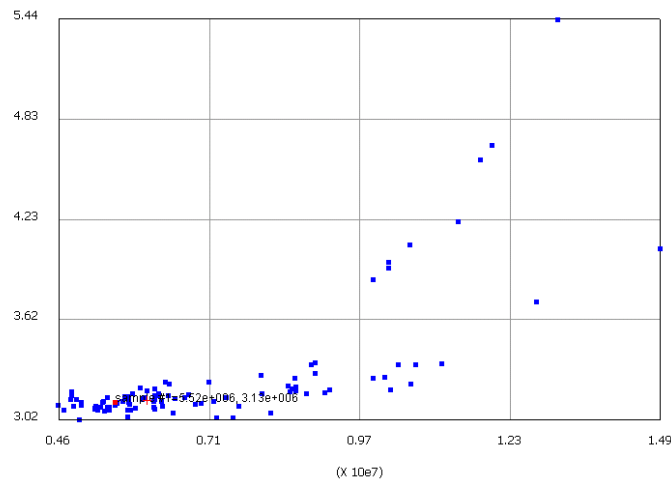
Frequency 17

Frequency Mode 4



SPC Forces Max Y Component

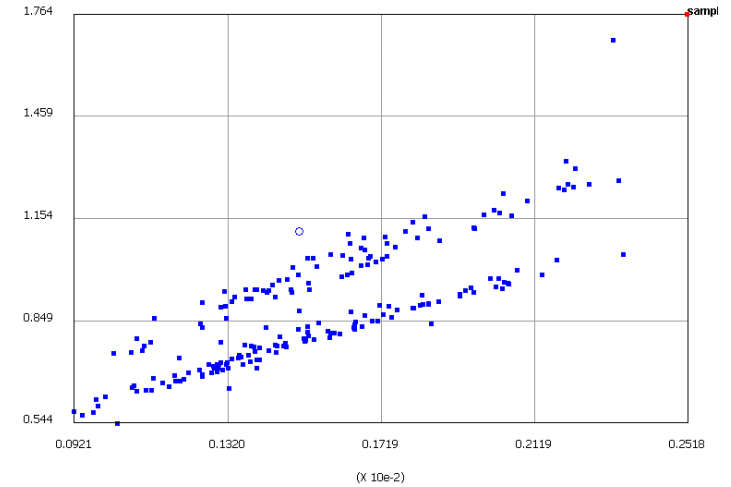
(X 10e6)



1st Principal Stress

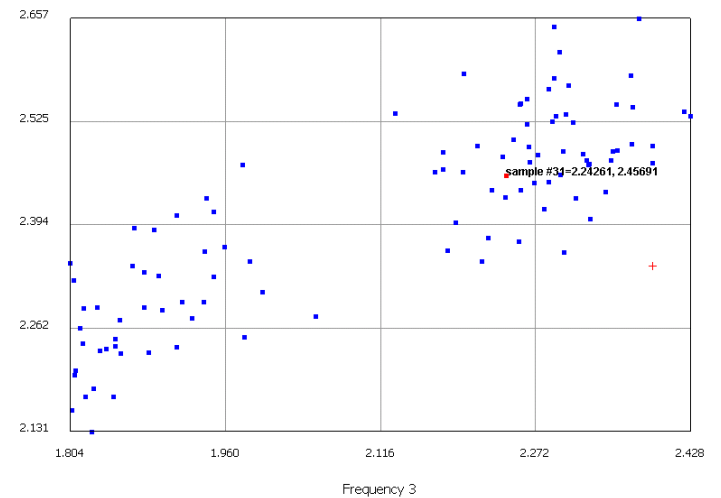
SPEARMAN = 0.819, PEARSON = 0.824

(X 10e9)

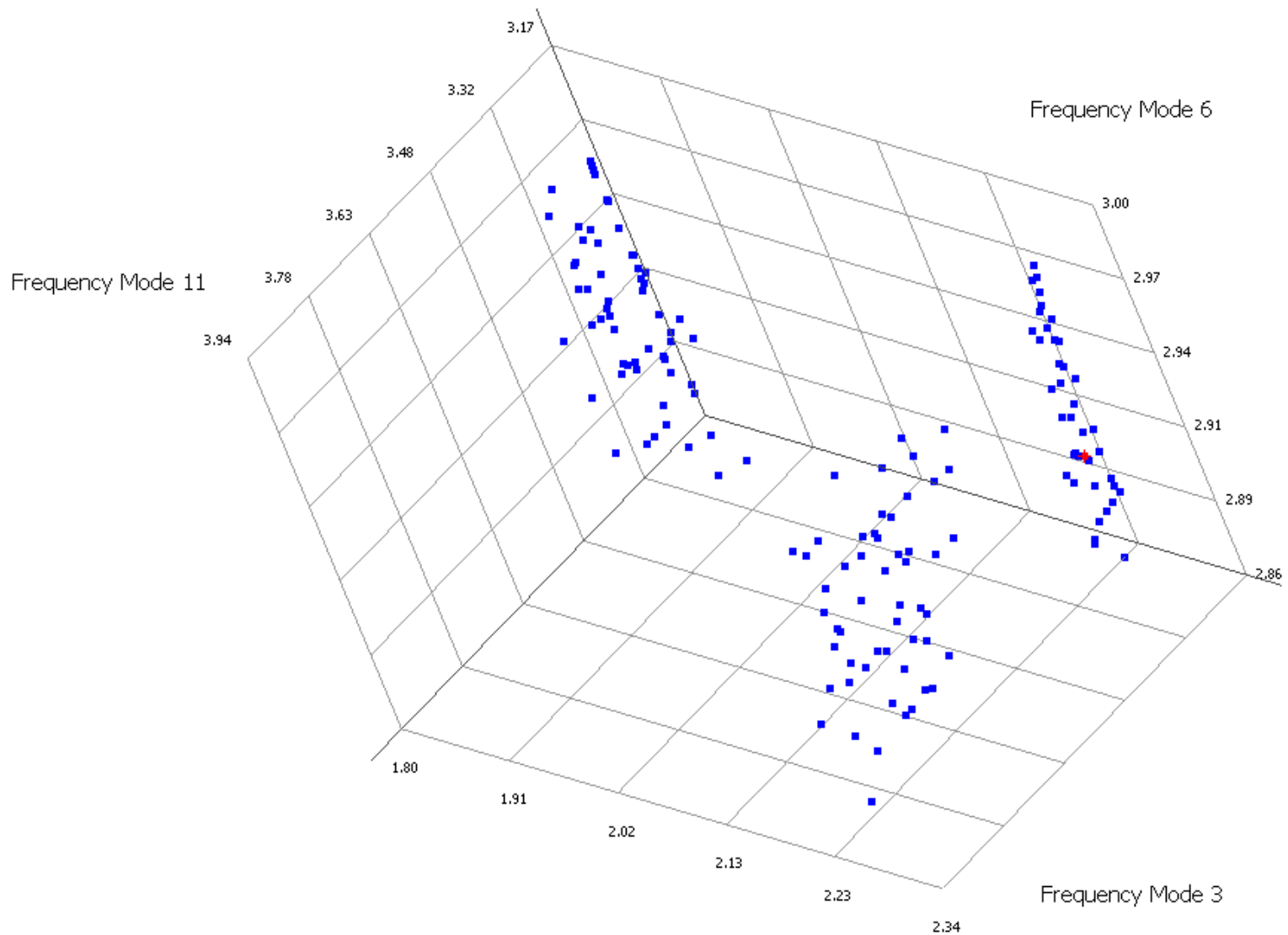


Frequency 4

SPEARMAN = 0.807, PEARSON = 0.845



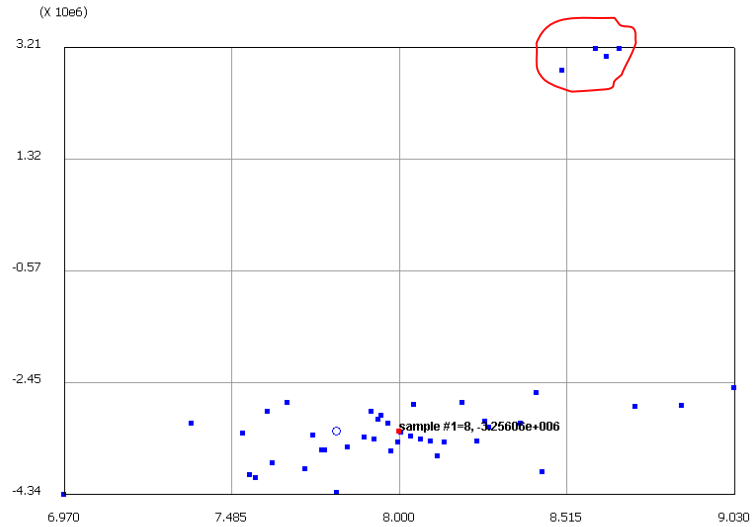
Clustering (Bifurcations)



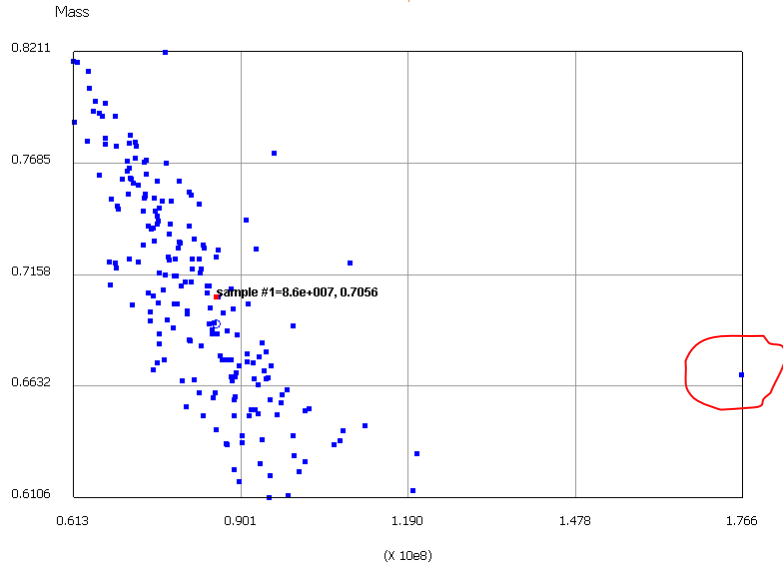
Outliers

Max Z Displacement

SPEARMAN = 0.547, PEARSON = 0.532

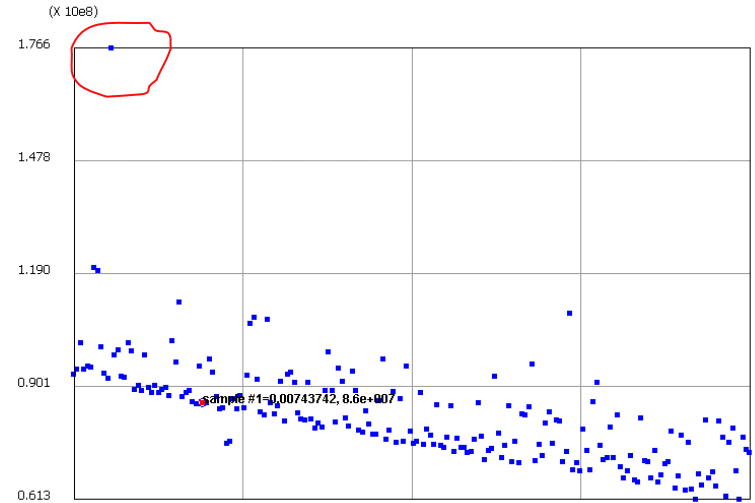


SPEARMAN = -0.809, PEARSON = -0.705



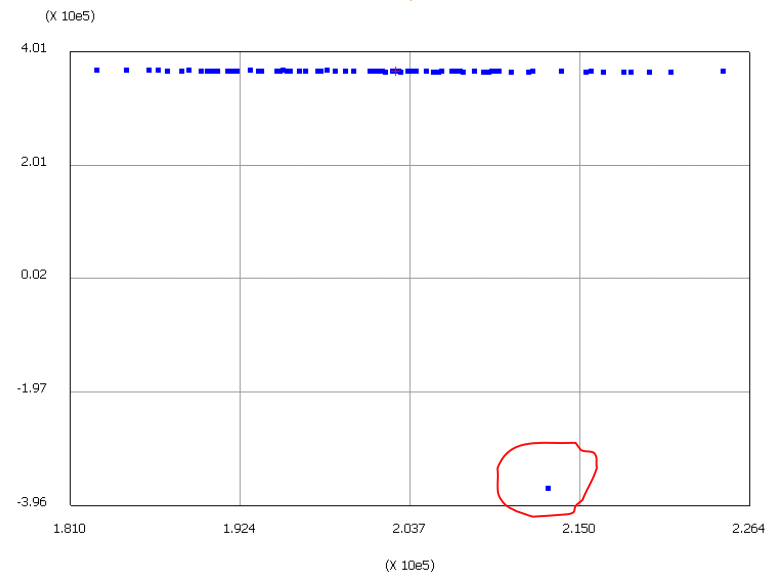
Sigma XY

SPEARMAN = -0.784, PEARSON = -0.693

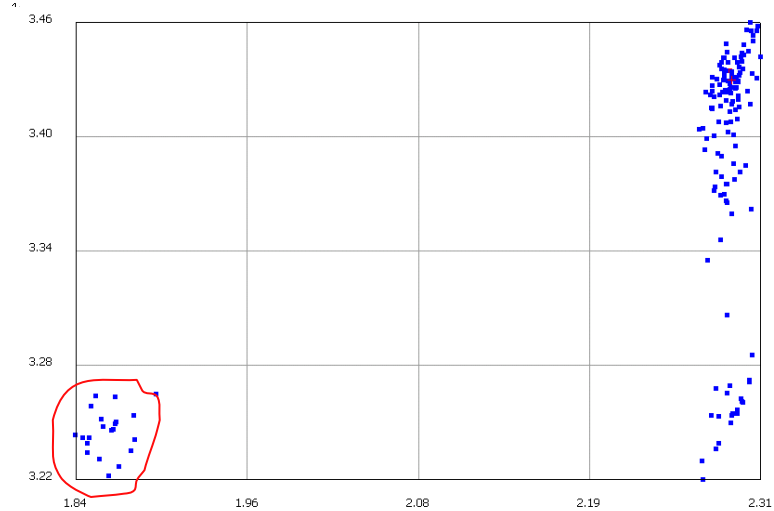
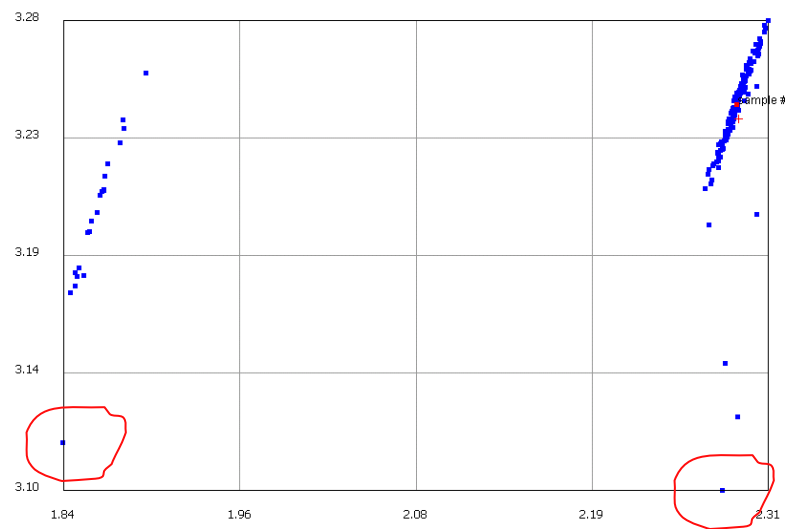
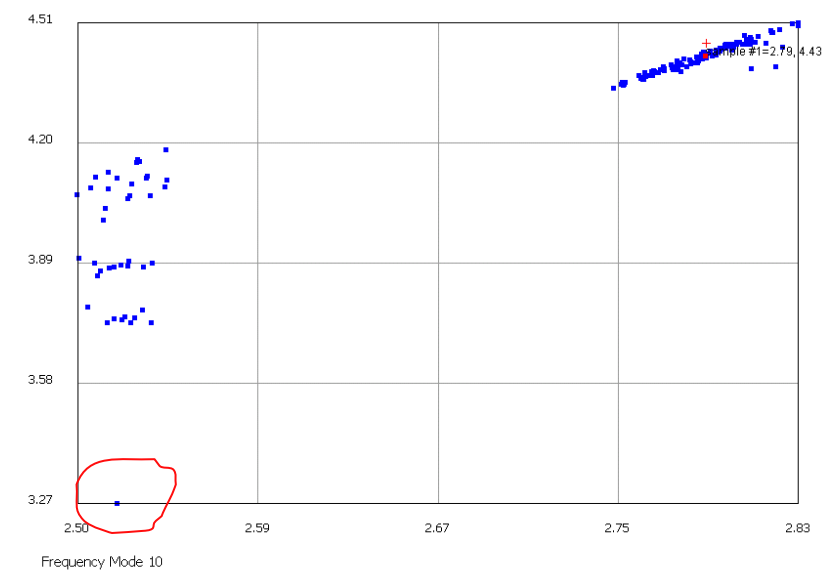
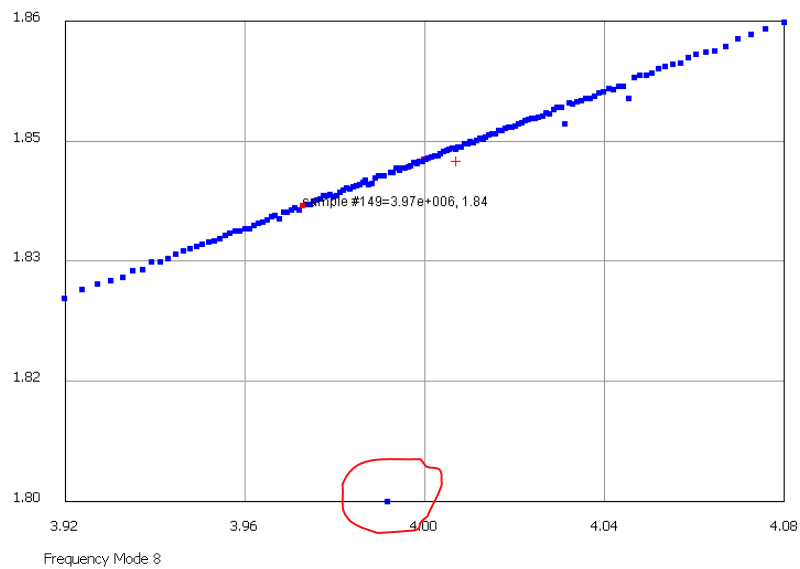


Max Z Displacement

SPEARMAN = -0.658, PEARSON = -0.147



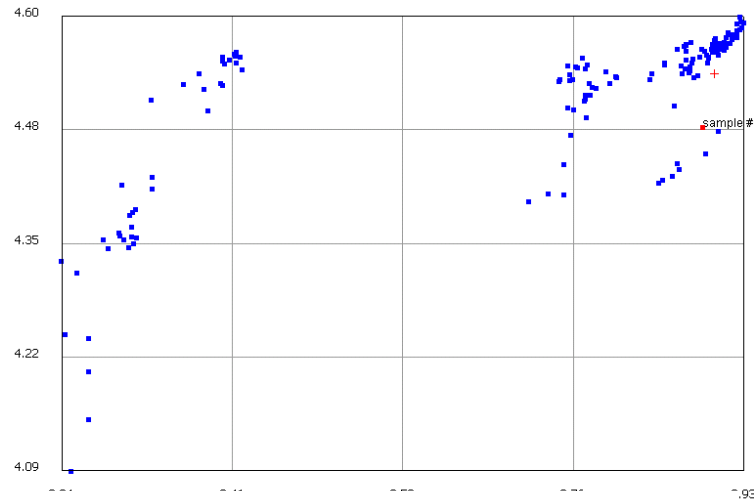
Outliers



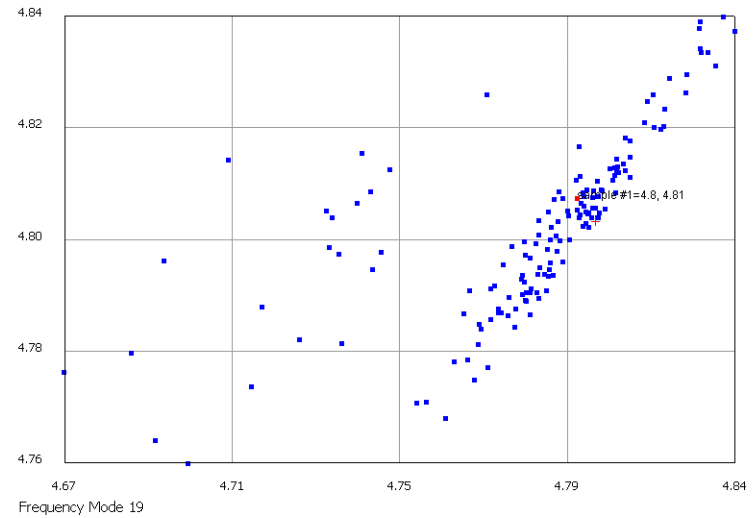


Other Pathologies

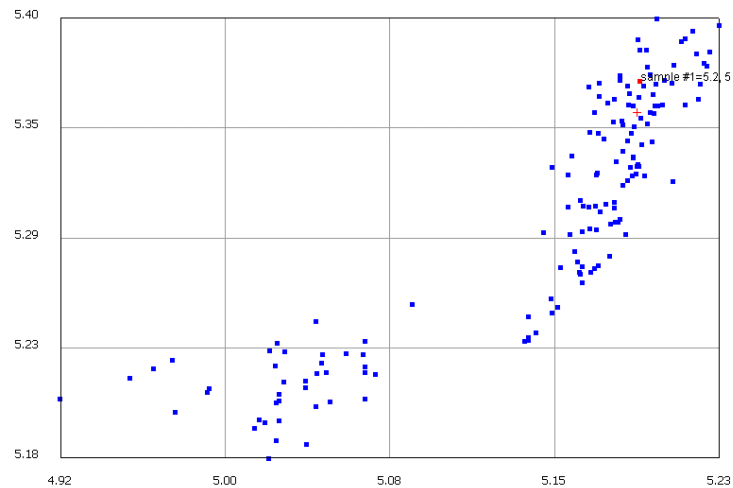
Frequency Mode 13



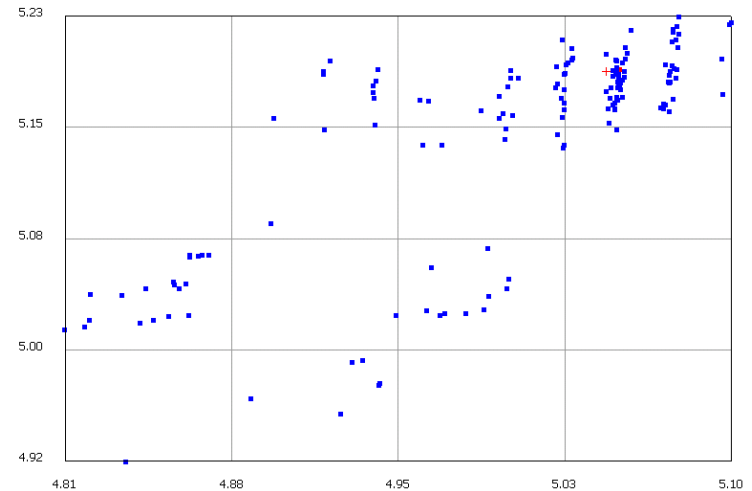
Frequency Mode 17



Frequency Mode 20



Frequency Mode 19

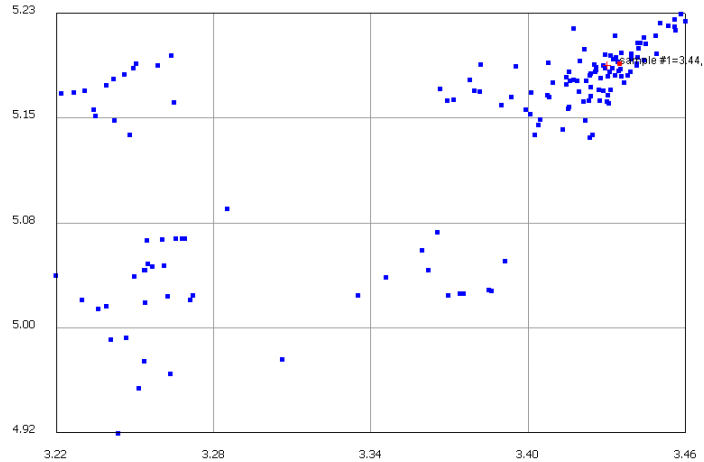


Frequency Mode 18

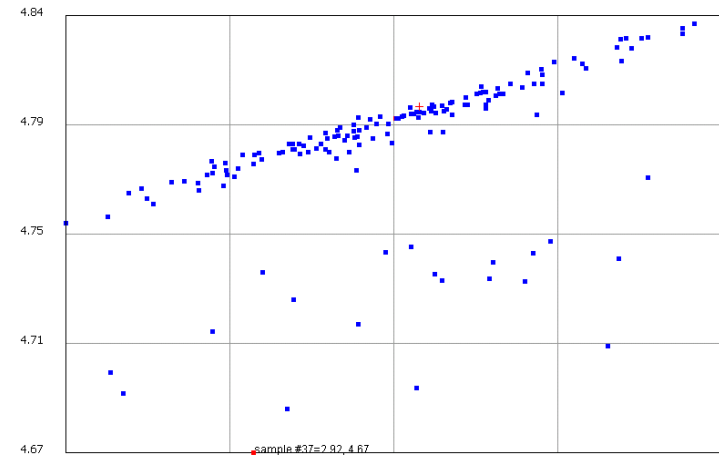
Frequency Mode 18

More pathologies

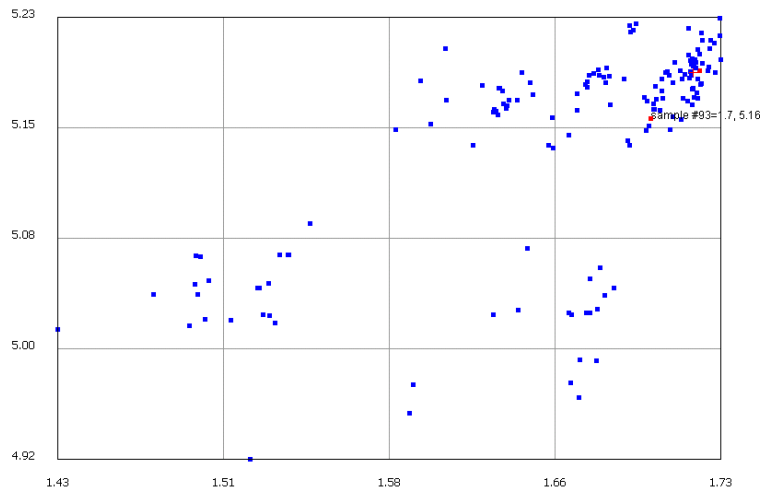
Frequency Mode 19



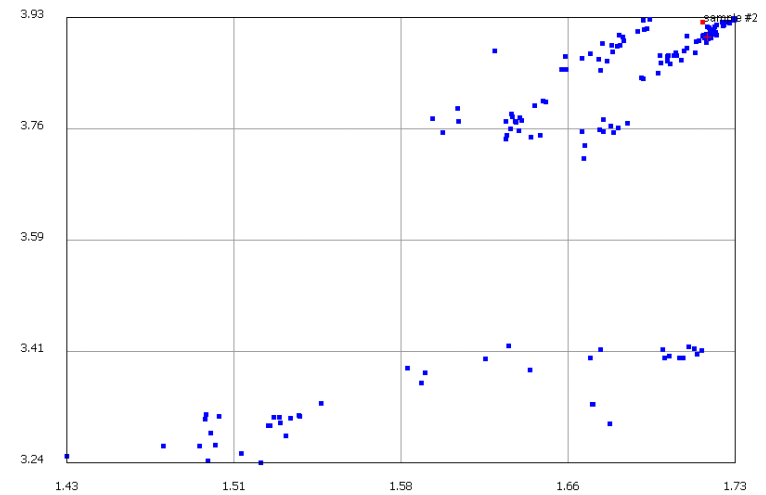
Frequency Mode 16



Frequency Mode 19



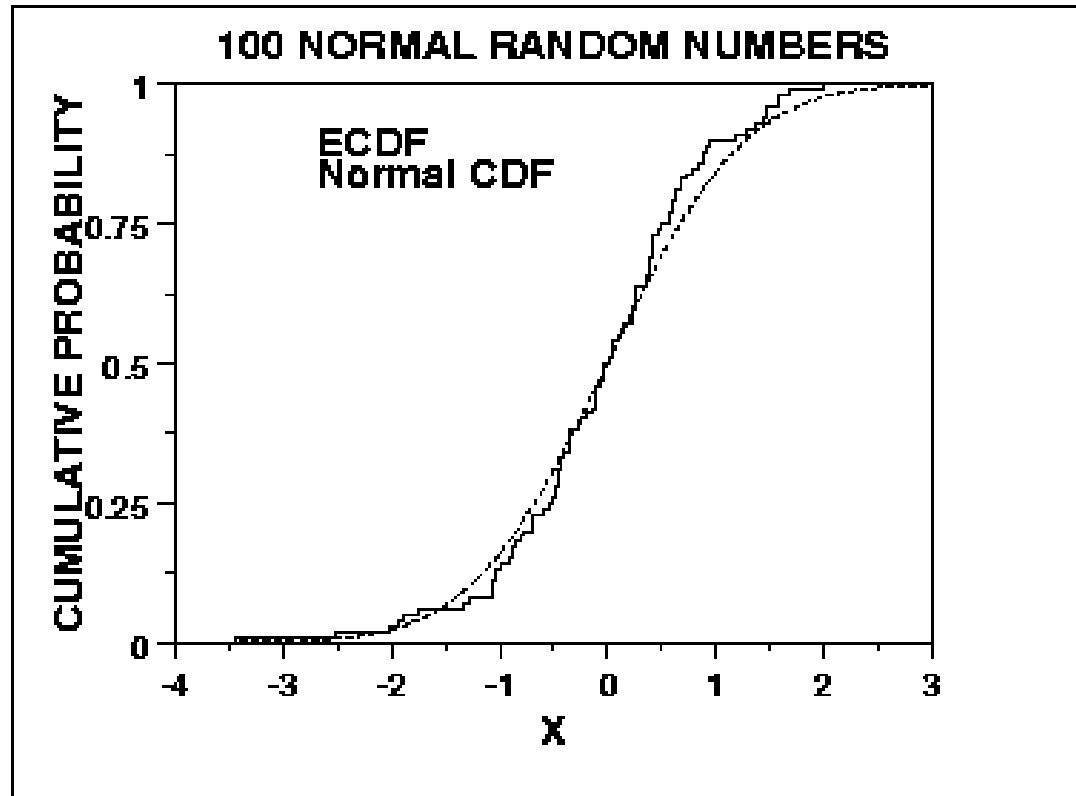
Frequency Mode 11



Relationship Robustness

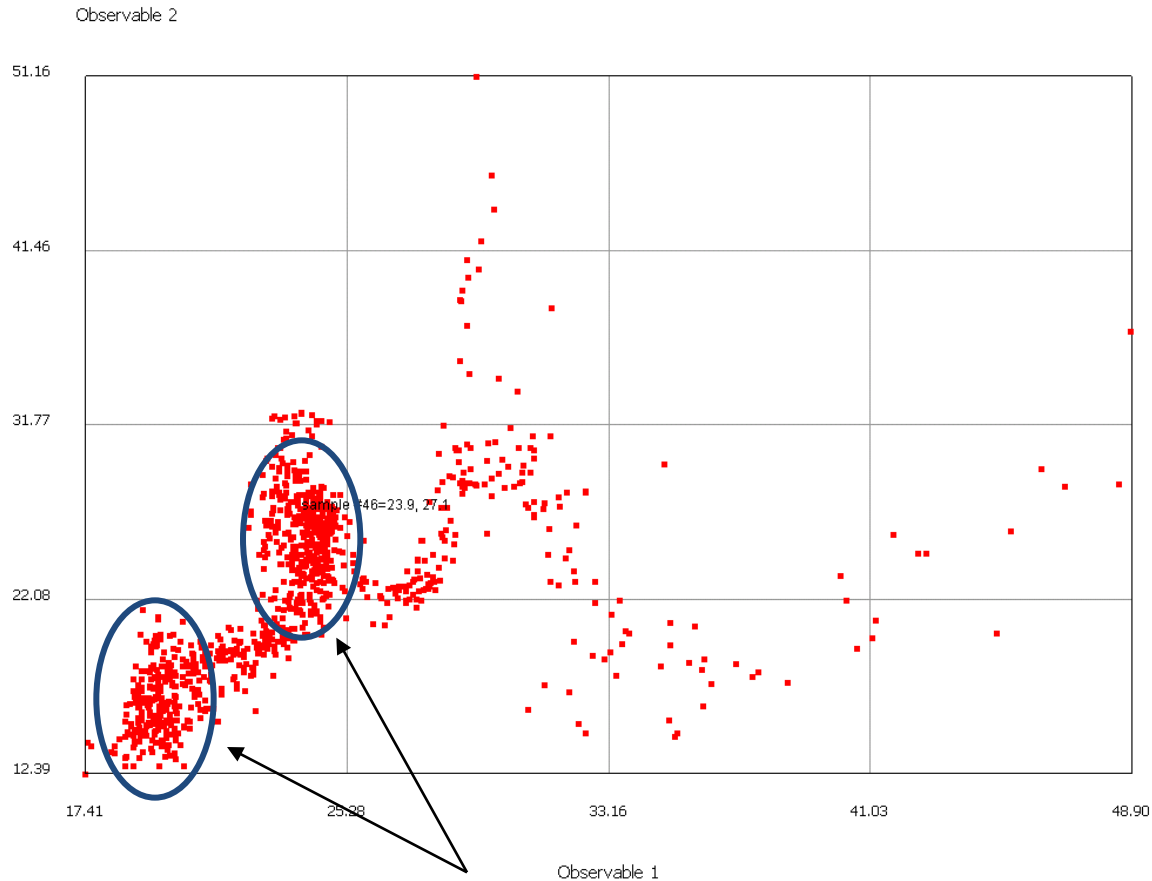
- The following forms of non-robustness exist:
 - Outliers
 - Clustering (multi-modal systems)
 - Discontinuities (jumps) in CDFs – high skewness
 - Any other pathology in ant-hills
- A good measure of robustness is the K-S distance (Kolmogorv-Smirnov) between the actual Cumulative Distribution Function (CDF) and the one corresponding to an equivalent Gaussian CDF.
- Another good measure of robustness is the CONVEXITY of the corresponding meta-model. Non robust systems are non-convex.
- An easy way to detect potential non-robustness is to check for large differences in the linear and non-linear correlation coefficients.
- Large scatter does not imply low robustness.

Kolmogorov-Smirnov (K-S) test



The Kolmogorov-Smirnov (K-S) test is based on the empirical distribution function (ECDF) compared to a normal cumulative distribution function. The K-S test is based on the maximum distance between these two curves.

Example of Non-Robust system

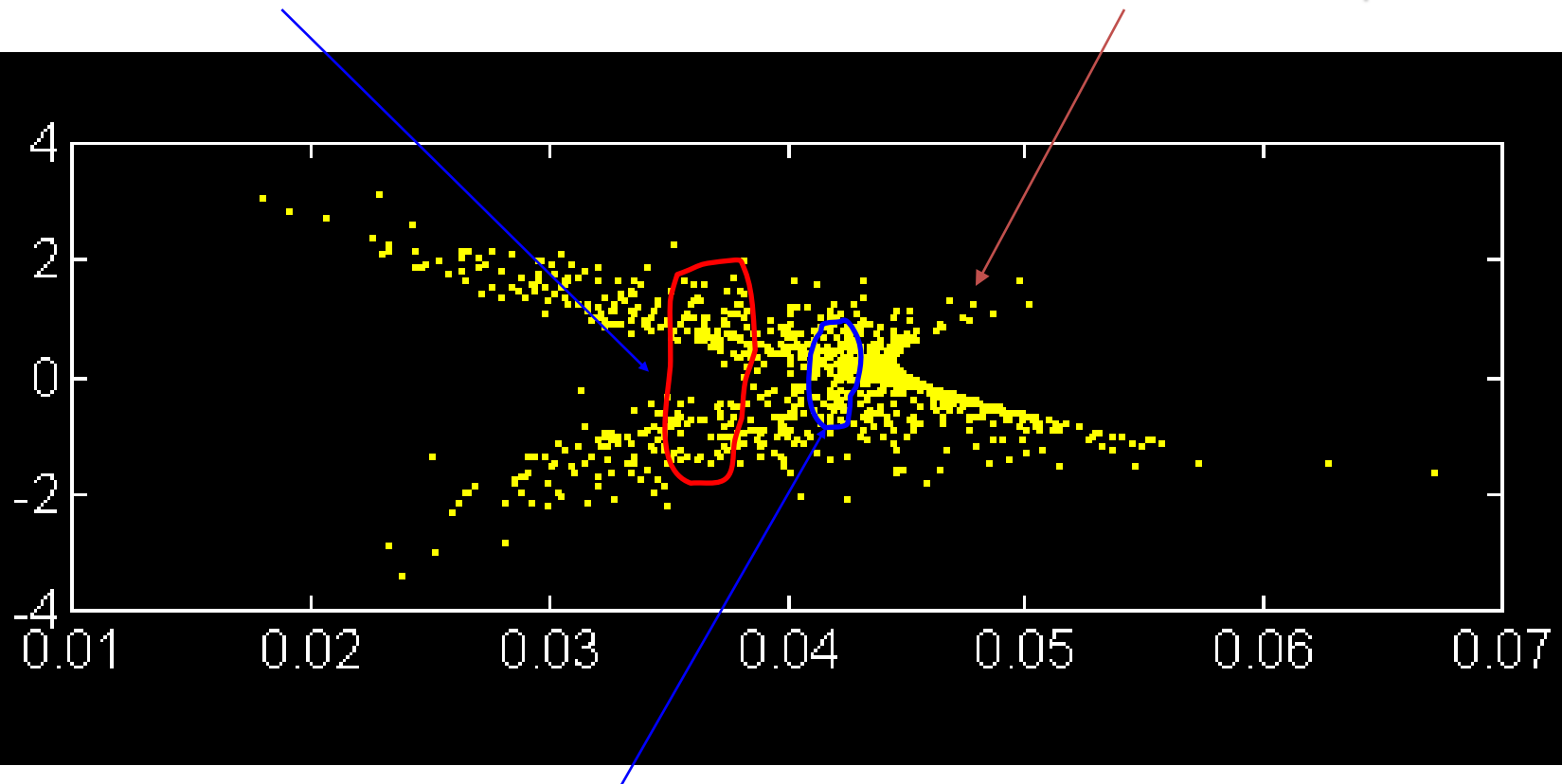


Most likely behavior (two possible modes)

Design Improvement and Robustness: Navigation of Fitness Landscapes

Initial design is non-robust (has two clusters, PDF is bi-modal). Must move cloud away from bifurcation.

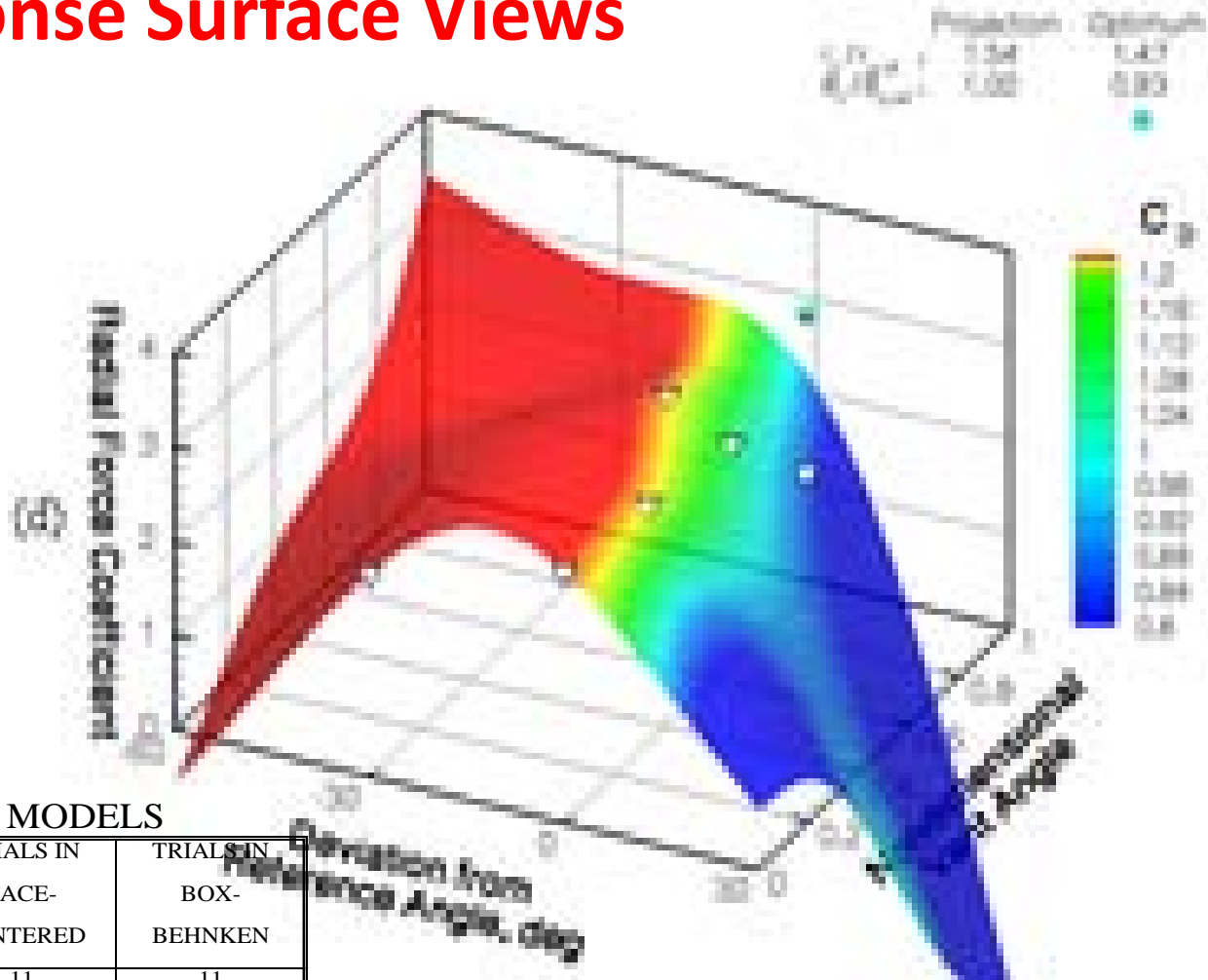
Fitness landscape



Robust design: one cluster (no bifurcations possible)

Response Surface Views

Assume Continuity

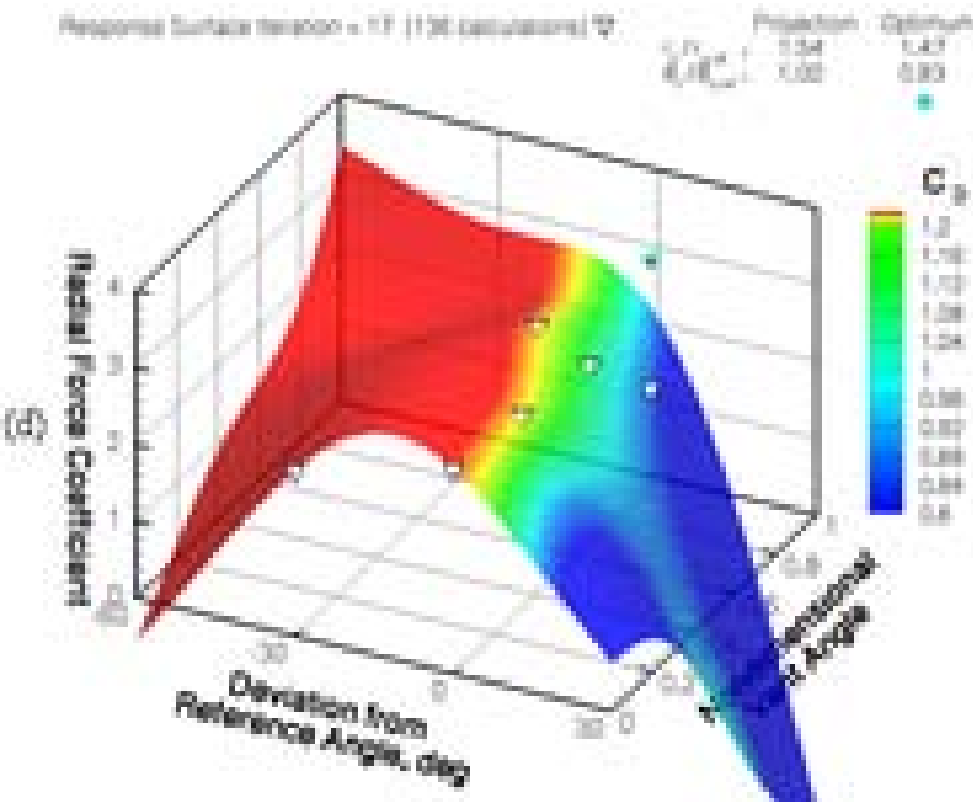


SIZE OF RESPONSE SURFACE MODELS

NUMBER OF FACTORS	RUNS IN 3 LEVEL FACT.	COEF. IN FULL QUAND	TRIALS IN FACE-CENTERED	TRIALS IN BOX-BEHNKEN
2	9	6	11	11
3	27	10	17	15
4	81	16	27	27
5	243	21	45	46
6	729	28	81	54
7	2187	36		62

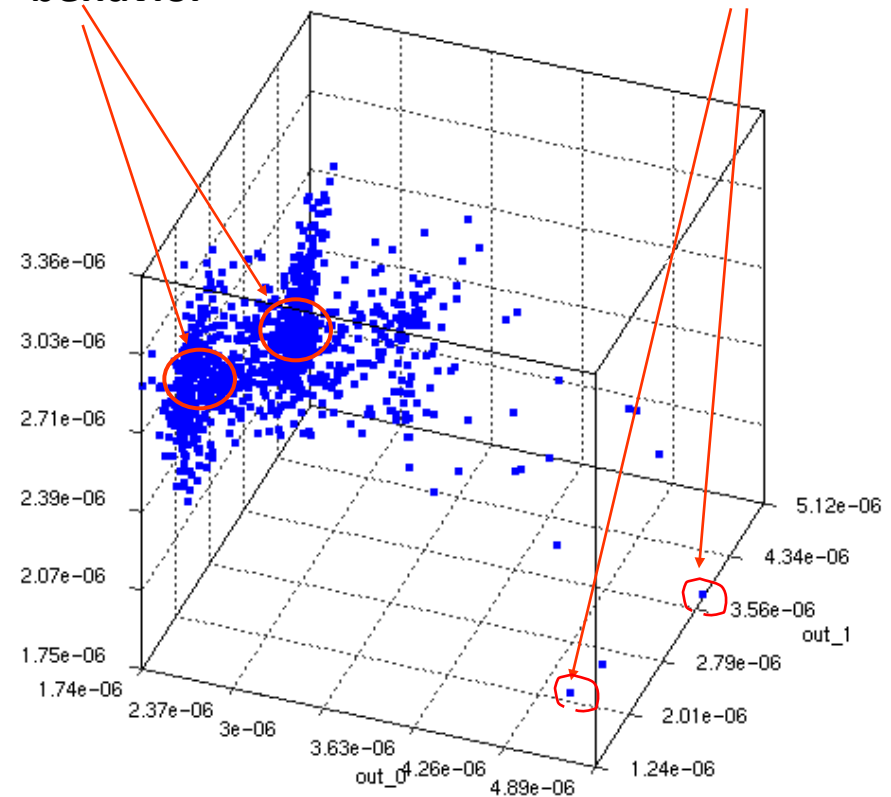
Sample Size a function of # of variables

Where is the Information?



Most likely
behavior

Outliers



Information from Correlation Maps

- Minimum use of surrogates – process uses the full analysis model and is unlimited in terms of number of variables.
- Helps **extract knowledge** that is embedded in their analysis models - leverages years of investment made in the FEM and CFD grids.
- Actually “computes knowledge” and presents it to the engineer in the form of the **Correlation Map**.
 - Knowledge is an organized set of related design rules
 - Precisely what a Correlation Map is.
- No need to be a specialist in numerical analysis to take full advantage of this capability.
- **Identifies what is IMPORTANT.**

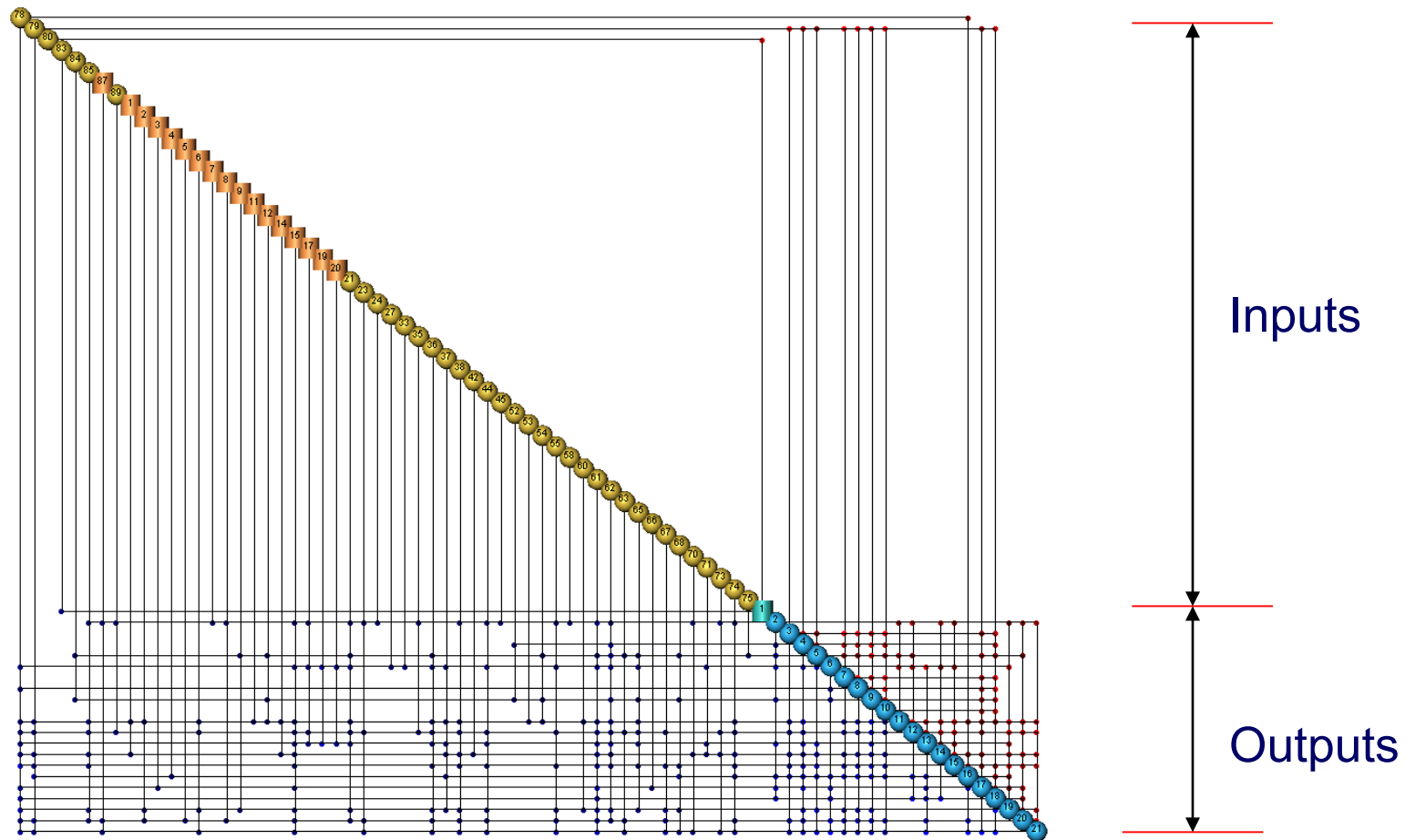
Correlation Map

- **A Correlation Map = Structured Information**
- **A Correlation Map helps an engineer:**
 - Understand how a system works (how information flows within the system, how variables and components correlate).
 - Make decisions as to how the design may be improved.
 - Find the weak points in a system.
 - Find redundancies in a design.
 - Identify rules that govern the performance (“if A and B then C”).
- **Correlation Maps help structure information better, to give it “topology” and a sense of dimension.**
- **Structured information (i.e. links between rules) is equivalent to knowledge.**
- **The following slides show an examples of Correlation Maps and their salient features.**

Design Structure Matrix

- **Format developed at MIT to maximize the data displayed in one view**
- **The Design Structure Matrix (DSM) has evolved into a tool to perform both the analysis and the management of complex systems.**
- **It enables the user to model, visualize, and analyze the dependencies among the entities of any system and derive suggestions for the improvement or synthesis of a system.**
- **Focus is on the visualization format**

Correlation Maps – Structured Information



Correlation Maps reflect how all system attributes (outputs) react to simultaneous changes in all of the input variables. It also shows relationships between outputs. Correlation maps can be very complex.